Regents Exam Questions G.CO.C.11: Trapezoids 1 www.jmap.org

## G.CO.C.11: Trapezoids 1

1 If the diagonals of a quadrilateral do not bisect each other, then the quadrilateral could be a

1) rectangle 2 ) rhombus 3 ) square
2) trapezoid

2 In trapezoid $R S T V$ with bases $\overline{R S}$ and $\overline{V T}$, diagonals $\overline{R T}$ and $\overline{S V}$ intersect at $Q$.


If trapezoid $R S T V$ is not isosceles, which triangle is equal in area to $\triangle R S V$ ?

1) $\triangle R Q V$
2) $\triangle R S T$
3) $\triangle R V T$
4) $\triangle S V T$

3 In the diagram below of isosceles trapezoid STAR, diagonals $\overline{A S}$ and $\overline{R T}$ intersect at $O$ and $\overline{S T} \| \overline{R A}$, with nonparallel sides $\overline{S R}$ and $\overline{T A}$.


Which pair of triangles are not always similar?

1) $\triangle S T O$ and $\triangle A R O$ 2) $\triangle S O R$ and $\triangle T O A$
2) $\triangle S R A$ and $\triangle A T S$
3) $\triangle S R T$ and $\triangle T A S$

4 Isosceles trapezoid $A B C D$ has diagonals $\overline{A C}$ and $\overline{B D}$. If $A C=5 x+13$ and $B D=11 x-5$, what is the value of $x$ ?

1) 28
2) $10 \frac{3}{4}$
3) 3
4) $\frac{1}{2}$

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8 In trapezoid $L M N O$ below, median $\overline{P Q}$ is drawn.


If $L M=x+7, O N=3 x+11$, and $P Q=25$, what is the value of $x$ ?

1) 1.75
2) 3.5
3) 8
4) 17

9 In the diagram below, $L A T E$ is an isosceles trapezoid with $\overline{L E} \cong \overline{A T}, L A=24, E T=40$, and $A T=10$. Altitudes $\overline{L F}$ and $\overline{A G}$ are drawn.


What is the length of $\overline{L F}$ ?

1) 62$) 83) 344$

10 In the diagram below of isosceles trapezoid $A B C D$, $A B=C D=25, A D=26$, and $B C=12$.


What is the length of an altitude of the trapezoid? 1) 7 2) 143$) 194) 24$

11 In isosceles trapezoid $A B C D, \overline{A B} \cong \overline{C D}$. If $B C=20, A D=36$, and $A B=17$, what is the length of the altitude of the trapezoid?

1) $\left.\begin{array}{lllll}10 & 2) & 12 & 3) & 15 \\ 4\end{array}\right) \quad 16$

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12 In the diagram below, $\overline{A B}$ and $\overline{C D}$ are bases of trapezoid $A B C D$.

(Not drawn to scale)
If $\mathrm{m} \angle B=123$ and $\mathrm{m} \angle D=75$, what is $\mathrm{m} \angle C$ ? 1) $57 \quad$ 2) $75 \quad 3) 105 \quad 4) 123$

13 In the diagram of trapezoid $A B C D$ below, $\overline{A B} \| \overline{D C}, \overline{A D} \cong \overline{B C}, \mathrm{~m} \angle A=4 x+20$, and $\mathrm{m} \angle C=3 x-15$.


What is $\mathrm{m} \angle D$ ?

1) 25 2) 35
2) 604$) 90$

14 In isosceles trapezoid $Q R S T$ shown below, $\overline{Q R}$ and $\overline{T S}$ are bases.


If $\mathrm{m} \angle Q=5 x+3$ and $\mathrm{m} \angle R=7 x-15$, what is $\mathrm{m} \angle Q$ ?

1) 83
2) 48
3) 16
4) 9

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15 In the diagram below of isosceles trapezoid $D E F G$, $\overline{D E} \| \overline{G F}, D E=4 x-2, E F=3 x+2, F G=5 x-3$, and $G D=2 x+5$. Find the value of $x$.


16 The cross section of an attic is in the shape of an isosceles trapezoid, as shown in the accompanying figure. If the height of the attic is 9 feet, $B C=12$ feet, and $A D=28$ feet, find the length of $A B$ to the nearest foot.


17 The accompanying diagram shows ramp $\overline{R A}$ leading to level platform $\overline{A M}$, forming an angle of $45^{\circ}$ with level ground. If platform $\overline{A M}$ measures 2 feet and is 6 feet above the ground, explain why the exact length of ramp $\overline{R A}$ is $6 \sqrt{2}$ feet.


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18 The diagram below shows isosceles trapezoid $A B C D$ with $\overline{A B} \| \overline{D C}$ and $\overline{A D} \cong \overline{B C}$. If $\mathrm{m} \angle B A D=2 x$ and $\mathrm{m} \angle B C D=3 x+5$, find $\mathrm{m} \angle B A D$.


19 Trapezoid $T R A P$, with median $\overline{M Q}$, is shown in the diagram below. Solve algebraically for $x$ and $y$.


## G.CO.C.11: Trapezoids 1

## Answer Section

1 ANS: 4
REF: 061008ge
2 ANS: 2
Isosceles or not, $\triangle R S V$ and $\triangle R S T$ have a common base, and since $\overline{R S}$ and $\overline{V T}$ are bases, congruent altitudes.
REF: 061301ge
3 ANS: 3 REF: 062323geo
4 ANS: 3
The diagonals of an isosceles trapezoid are congruent. $5 x+3=11 x-5$.

$$
\begin{aligned}
6 x & =18 \\
x & =3
\end{aligned}
$$

REF: fall0801ge
5 ANS: 3
$\frac{6.5}{10.5}=\frac{5.2}{x}$
$x=8.4$
REF: 012006geo
6 ANS: 1
The length of the midsegment of a trapezoid is the average of the lengths of its bases. $\frac{x+3+5 x-9}{2}=2 x+2$.

$$
\begin{aligned}
6 x-6 & =4 x+4 \\
2 x & =10 \\
x & =5
\end{aligned}
$$

REF: 081221ge
7 ANS: 2
The length of the midsegment of a trapezoid is the average of the lengths of its bases. $\frac{x+30}{2}=44$.

$$
\begin{aligned}
x+30 & =88 \\
x & =58
\end{aligned}
$$

REF: 011001ge

8 ANS: 3

$$
\begin{aligned}
\frac{x+7+3 x+11}{2} & =25 \\
4 x+18 & =50 \\
4 x & =32 \\
x & =8
\end{aligned}
$$

REF: 011608ge
9 ANS: 1
$\frac{40-24}{2}=8 . \sqrt{10^{2}-8^{2}}=6$.


REF: 061204ge
10 ANS: 4
$\sqrt{25^{2}-\left(\frac{26-12}{2}\right)^{2}}=24$

REF: 011219ge
11 ANS: 3


REF: 061016 ge
12 ANS: 1
$180-123=57$
REF: 061419ge
13 ANS: 3

$$
\begin{aligned}
2(4 x+20)+2(3 x-15) & =360 . \quad \angle D=3(25)-15=60 \\
8 x+40+6 x-30 & =360 \\
14 x+10 & =360 \\
14 x & =350 \\
x & =25
\end{aligned}
$$

REF: 011321ge

14 ANS: 2
$5 x+3=7 x-15 \quad 5(9)+3=48$
$18=2 x$

$$
9=x
$$

REF: 011515ge
15 ANS:
3. The non-parallel sides of an isosceles trapezoid are congruent. $2 x+5=3 x+2$

$$
x=3
$$

REF: 080929ge
16 ANS:
12. Because the shape is an isosceles trapezoid, $\overline{A E}=\frac{28-12}{2}=8$. Using Pythagoras, $\begin{aligned} 8^{2}+9^{2} & =c^{2} \\ c & \approx 12\end{aligned}$

REF: 069933a
17 ANS:
Draw a line perpendicular to $\overline{R P}$ at $T$ to $A . \triangle R A T$ is an isosceles right triangle with legs of $6.6^{2}+6^{2}=c^{2}$

$$
\begin{aligned}
72 & =c^{2} \\
\sqrt{72} & =c \\
6 \sqrt{2} & =c
\end{aligned}
$$

REF: 080726b
18 ANS:
70. $3 x+5+3 x+5+2 x+2 x=180$

$$
\begin{aligned}
10 x+10 & =360 \\
10 x & =350 \\
x & =35 \\
2 x & =70
\end{aligned}
$$

REF: 081029ge
19 ANS:

$$
\begin{array}{rlrl}
12 x-4+7 x+13 & =180 . & 16 y+1 & =\frac{12 y+1+18 y+6}{2} \\
19 x+9 & =180 & 32 y+2 & =30 y+7 \\
19 x & =171 & 2 y & =5 \\
x & =9 & y & =\frac{5}{2}
\end{array}
$$

REF: 081337ge

