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## F.IF.A.3: Sequences 1

1 Given the following three sequences:
I. $2,4,6,8,10 \ldots$
II. $2,4,8,16,32 \ldots$
III. $a, a+2, a+4, a+6, a+8 \ldots$

Which ones are arithmetic sequences?

1) I and II, only
2) I and III, only
3) II and III, only
4) I, II, and III

2 What is the common difference of the arithmetic sequence $5,8,11,14$ ?

1) $\frac{8}{5}$
2) -3
3) 3
4) 9

3 The first term in a sequence is 5 and the fifth term is 17 . What is the common difference?

1) 2.4
2) 12
3) 3
4) 4

4 Determine the common difference of the arithmetic sequence in which $a_{1}=3$ and $a_{4}=15$.

5 Find the common difference in the arithmetic sequence, $a_{n}$, in which $a_{1}=16$ and $a_{9}=36$.

6 What is the common difference of the arithmetic sequence below?

$$
-7 x,-4 x,-x, 2 x, 5 x, \ldots
$$

1) -3
2) $-3 x$
3) 3
4) $3 x$

7 What is the common difference in the sequence
$2 a+1,4 a+4,6 a+7,8 a+10, \ldots$ ?

1) $2 a+3$
2) $-2 a-3$
3) $2 a+5$
4) $-2 a+5$

8 Given the sequence: $x,(x+y),(x+2 y), \ldots$
Which expression can be used to determine the common difference of this sequence?

1) $x-(x+y)$
2) $(x+2 y)-(x+y)$
3) $\frac{x}{(x+y)}$
4) $\frac{(x+2 y)}{(x+y)}$

9 Which arithmetic sequence has a common difference of 4 ?

1) $\{0,4 n, 8 n, 12 n, \ldots\}$
2) $\{n, 4 n, 16 n, 64 n, \ldots\}$
3) $\{n+1, n+5, n+9, n+13, \ldots\}$
4) $\{n+4, n+16, n+64, n+256, \ldots\}$

10 Consider the following patterns:

$$
\begin{array}{ll}
\text { I. } & 16,-12,9,-6.75, \ldots \\
\text { II. } & 1,4,9,16, \ldots \\
\text { III. } & 6,18,30,42, \ldots \\
\text { IV. } & \frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \ldots
\end{array}
$$

Which pattern is geometric?

1) $I$
2) II
3) III
4) IV

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11 Which situation could be modeled using a geometric sequence?

1) A cell phone company charges $\$ 30.00$ per month for 2 gigabytes of data and $\$ 12.50$ for each additional gigabyte of data.
2) The temperature in your car is $79^{\circ}$. You lower the temperature of your air conditioning by $2^{\circ}$ every 3 minutes in order to find a comfortable temperature.
3) David's parents have set a limit of 50 minutes per week that he may play online games during the school year. However, they will increase his time by $5 \%$ per week for the next ten weeks.
4) Sarah has $\$ 100.00$ in her piggy bank and saves an additional $\$ 15.00$ each week.

12 Determine and state whether the sequence $1,3,9,27, \ldots$ displays exponential behavior. Explain how you arrived at your decision.

13 What is the common ratio of the geometric sequence shown below?

$$
-2,4,-8,16, \ldots
$$

1) $-\frac{1}{2}$
2) 2
3) -2
4) -6

14 The common ratio of the sequence $-\frac{1}{2}, \frac{3}{4},-\frac{9}{8}$ is

1) $-\frac{3}{2}$
2) $-\frac{2}{3}$
3) $-\frac{1}{2}$
4) $-\frac{1}{4}$

Name: $\qquad$

15 If $x \neq 0$, then the common ratio of the sequence $x, 2 x^{2}, 4 x^{3}, 8 x^{4}, 16 x^{5}, \ldots$ is

1) $2 x$
2) 2
3) $x$
4) $\frac{1}{2} x$

16 What is the common ratio of the sequence $\frac{1}{64} a^{5} b^{3},-\frac{3}{32} a^{3} b^{4}, \frac{9}{16} a b^{5}, \ldots$ ?

1) $-\frac{3 b}{2 a^{2}}$
2) $-\frac{6 b}{a^{2}}$
3) $-\frac{3 a^{2}}{b}$
4) $-\frac{6 a^{2}}{b}$

17 What is a common ratio of the geometric sequence whose first term is 5 and third term is 245 ?

1) 7
2) 49
3) 120
4) 240

18 What is the common ratio of the geometric sequence whose first term is 27 and fourth term is 64 ?

1) $\frac{3}{4}$
2) $\frac{64}{81}$
3) $\frac{4}{3}$
4) $\frac{37}{3}$

## F.IF.A.3: Sequences 1

Answer Section
1 ANS: 2 REF: 061919ai
2 ANS: 3 REF: 061001a2
3 ANS: 3
$\frac{17-5}{5-1}=\frac{12}{4}=3$
REF: 062215ai
4 ANS:
$\frac{15-3}{4-1}=\frac{12}{3}=4$
REF: 012328ai
5 ANS:
$\frac{36-16}{9-1}=\frac{20}{8}=2.5$
REF: 081630a2
6 ANS: 4 REF: 061411a2
7 ANS: 1
$(4 a+4)-(2 a+1)=2 a+3$
REF: 011401a2
8 ANS: 2 REF: 011610a2
9 ANS: 3 REF: 011110a2
10 ANS: 1
$\frac{-12}{16}=\frac{9}{-12}=\frac{-6.75}{9}$
REF: 012017aii
11 ANS: 3 REF: 061910aii
12 ANS:
Yes, because the sequence has a common ratio, 3 .
REF: 081726ai
13 ANS: 3
$\frac{4}{-2}=-2$
REF: 011304a2

14 ANS: 1
$\frac{\frac{3}{4}}{-\frac{1}{2}}=-\frac{3}{2}$

REF: 011508a2
15 ANS: 1
$\frac{2 x^{2}}{x}=2 x$
REF: 082202ai
16 ANS: 2
$\frac{-\frac{3}{32} a^{3} b^{4}}{\frac{1}{64} a^{5} b^{3}}=-\frac{6 b}{a^{2}}$
REF: 061326a2
17 ANS: 1

$$
\begin{array}{rlrl}
5 r=a_{2} & a_{2} r=245 & 5 r & =\frac{245}{r} \\
a_{2}=\frac{245}{r} & 5 r^{2} & =245 \\
r^{2} & =49 \\
r & = \pm 7
\end{array}
$$

REF: 081924ai
18 ANS: 3
$27 r^{4-1}=64$
$r^{3}=\frac{64}{27}$

$$
r=\frac{4}{3}
$$

REF: 081025a2

