# The University of the State of New York <br> 304th High School Examination <br> TRIGONOMETRY 

Wednesday, August 25, 1948-12 m. to 3 p. m., only

## Instructions

Part I is to be done first and the maximum time allowed for it is one and one half hours. At the end of that time, this part of the examination must be detached and will be collected by the teacher. If you finish part I before the signal to stop is given, you may begin part II.

Write at top of first page of answer paper to parts II, III and IV (a) names of schools where you have studied, (b) number of weeks and recitations a week in trigonometry previous to entering summer high school, (c) number of recitations in this subject attended in summer high school of 1948 or number and length in minutes of lessons taken in the summer of 1948 under a tutor licensed in the subject and supervised by the principal of the school you last attended.

The minimum time requirement is four or five recitations a week for half a school year. The summer school session will be considered the equivalent of one semester's work during the regular session (four or five recitations a week for half a school year).

For those who have met the time requirement, the minimum passing mark is 65 credits; for all others 75 credits.

For admission to this examination attendance on at least 30 recitations in this subject in a registered summer high school in 1948 or an equivalent program of tutoring approved in advance by the Department is required.

Answer five questions from parts II, III and IV, including at least one question from each part.

## Part II

Answer at least one question from part II.
$21 a$ Solve the equation $\cos ^{2} x+2 \sin x+2=0$ for $x$ between $0^{\circ}$ and $360^{\circ}$.
$b$ Is the equation $2 \sin ^{2} 2 x=1-\cos 4 x$ true for all values of $x$ ? [Answer yes or no.] [2]
22 Derive the law of cosines for plane triangles. Consider only the case in which the triangle is acute. [10]
$23 a$ Sketch the graph of $y=\cos x$ from $-\pi$ to $+\pi$. [5]
$b$ On the set of axes used in answer to $a$, sketch the graph of $y=\tan x$ from $-\pi$ to $+\pi$. [4]
$c$ On the graphs made in answer to $a$ and $b$, mark the points whose abscissas are solutions of the equation $\tan x-\cos x=0 \quad$ [1]
$24 a$ Given an isosceles triangle one of whose equal sides is $s$ and one of whose base angles is $A$. Show that the area of the triangle is $\frac{1}{2} s^{2} \sin 2 A$. [8]
$b$ If $s$ is a constant, for what value of $A$ will the area of the triangle given in $a$ be a maximum? [2]

## Trigonometry

## Part III

Answer at least one question from part III.
25 Two forces of 29.5 lb and 54.2 lb act on a body. The angle between the lines of action of the forces is $95^{\circ} 40^{\prime}$. Find to the nearest minute the angle that the resultant makes with the larger force. [10]

26 Find to the nearest square foot the area of a triangular plot of ground whose sides are 22.3 ft , 40.5 ft and 32.8 ft . [10]

27 Using the values indicated in the figure, solve for $x$ to the nearest integer. [10]


## Part IV <br> Answer at least one question from part IV.

28 Find to the nearest 10 nautical miles the distance from Greenwich (Lat. $51^{\circ} 29^{\prime} \mathrm{N}$, Long. $0^{\circ} \mathrm{W}$ ), to Galapagos Islands (Lat. $1^{\circ} \mathrm{N}$, Long. $90^{\circ} \mathrm{W}$ ). [10]

29 Given spherical triangle $A B C$ in which $b=48^{\circ} 20^{\prime}, c=82^{\circ} 30^{\prime}, A=54^{\circ} 20^{\prime}$. Find $a$ to the nearest 10 minutes. [10]

## Trigonometry

Fill in the following lines:

Name of pupil.
Name of school.

## Part I

Answer all questions in part I. Each correct answer will receive $21 / 2$ credits. No partial credit will be allowed. Each answer must be reduced to its simplest form.

1 Find the logarithm of 2.718
2 Find $\log \cos 59^{\circ} 13^{\prime}$
3 Find to the nearest minute the acute angle $A$ if $\tan A=1.9375$
4 Find the value of $\sin \frac{11 \pi}{6}$
5 Express $\tan x$ in terms of $\cos x$ if $x$ is an angle in the first quadrant.
6 Express $\tan \left(x-45^{\circ}\right)$ in terms of $a$ if $\tan x=a$
7 Express $\cos \left(x+30^{\circ}\right)$ in terms of $\sin x$ and $\cos x$.
8 Find the positive value of $\sin \frac{x}{2}$ if $\cos x=\frac{1}{9}$
9 Express $\log \cot x$ in terms of $\log \sin x$ and $\log \cos x$.
10 In triangle $A B C, A=30^{\circ}$ and $B=45^{\circ}$. What is the value of the ratio $a: b$ ? [Answer may be left in radical form.]

11 In triangle $A B C, A=75^{\circ}$ and $B=15^{\circ}$. What is the value of the ratio $(a-b):(a+b)$ ? [Answer may be left in radical form.]

12 In triangle $A B C, a=2, b=3, c=4$. What is the value of $\cos B$ ?
13 Point $B$ bears $\mathrm{N} 60^{\circ} \mathrm{E}$ from point $A$, and distance $A B$ is 2 miles. How far north is $B$ from $A$ ?

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11..................
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Directions (questions 14-17) - Indicate the correct answer to each question by writing on the line at the right the letter $a, b$ or $c$.
14 The number of degrees in one radian is
(a) less than 60
(b) equal to 60 (c) greater than 60
14......

15 Using the data $a=5, b=8$ and $A=50^{\circ}$, it is possible to construct (a) two triangles (b) only one triangle (c) no triangle
15.

16 In spherical triangle $A B C$ in which $C$ equals $90^{\circ}$ and $c$ is greater than $90^{\circ}$
(a) both $a$ and $b$ are greater than $90^{\circ} \quad$ (b) both $a$ and $b$ are less than $90^{\circ}$
(c) either $a$ or $b$ is greater than $90^{\circ}$
(a) 2
(b) 3
(c) 6
17 The maximum value of $2 \sin 3 x$ is
16.

17
18 Find the value of the positive acute angle which satisfies the equation $4 \cos ^{2} x-3=0$
18. $\qquad$
19 If $\sin x$ is positive and decreases as $x$ increases, then $\cos x$ decreases. [Answer true or false.]
19.

20 Given spherical triangle $A B C$, in which $C$ is $90^{\circ}, a$ and $b$ are known and $A$ is to be found; write the formula involving $a, b$ and $A$.

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