

## High School Department

172D EXAMINATION

## TRIGONOMETRY

Thursday, January 30, 1902—9.15 a. m. to 12.15 p. m., only

Answer eight questions but no more. Include at least three from the third division if credit is desired for both plane and spheric trigonometry. If more than eight are answered only the first eight answers will be considered. Division of groups is not allowed.  $A$ ,  $B$  and  $C$  represent the angles of a triangle,  $a$ ,  $b$  and  $c$  the opposite sides. In a right triangle  $C$  represents the right angle. Each complete answer will receive  $12\frac{1}{2}$  credits. Papers entitled to 75 or more credits will be accepted.

Give special attention to arrangement of work.

**First division** 1 Perform the operations indicated in the following expressions, using logarithms where possible:  $2.18^6$ ,

$$\sqrt[5]{7776}, 21 \times 18 \times .05, \frac{45 \times 63}{14+13}$$

2 The two legs of a right triangle are 5 feet and 12 feet respectively; express as common fractions the values of *six* functions of the smaller angle of the triangle.

3 Write the algebraic sign of each of *six* functions of  $a$ ) an angle of  $175^\circ$ ,  $b$ ) an angle of  $225^\circ$ .

4 Assuming the values of  $\sin(A+B)$  and  $\cos(A+B)$ ; find the value of  $\tan 2A$  in terms of  $\tan A$ .

**Second division** 5 Prove that in any plane triangle  $\frac{c}{a+b} = \frac{a-b}{m-n}$ ,  $m$  and  $n$  being the segments of  $c$  made by a perpendicular from  $C$ .

6 In a right triangle  $c=128$  feet,  $A=37^\circ 30'$ ; find  $B$ ,  $a$  and  $b$ .

7-8 Given  $b=75$ ,  $c=64$ ,  $C=27^\circ 30'$ ; find *two* possible values for  $B$  and for  $a$ .

**Third division** 9 Write the four formulas known as Napier's analogies.  
10 Given in a spheric triangle  $a=174^\circ 13'$ ,  $b=94^\circ 8'$ ,  $c=90^\circ$ ; find the three angles.

11 Given  $a=52^\circ 45'$ ,  $b=71^\circ 12' 40''$ ,  $A=46^\circ 22'$ ; find *two* possible values for  $B$ .

12 Prove that in any spheric triangle  $\cos A = \sin B \sin C \cos a - \cos B \cos C$ .