

# University of the State of New York.

36TH ACADEMIC EXAMINATION.

## PLANE TRIGONOMETRY.

THURSDAY, Jan. 23, 1890—Time, 9:30 A. M. to 12:30 P. M., only.

36 credits, necessary to pass, 27.

1. Explain the difference between the characteristic and mantissa of the logarithm of a whole number and that of a decimal fraction ..... 4
2. The logarithm of 199 is 2.298853. Find the logarithm of the fourth power of 199, and also of its cube root and state the principles employed..... 4
3. Draw a figure of the fourth quadrant and upon it indicate the following functions of  $300^\circ$ ; sine, cosine, cotangent, secant ... 4
4. State and demonstrate the theorem employed in computing the remaining angles of a triangle when two sides and the included angle are given ..... 4
5. Given the versed sine =  $\frac{2}{3}$ , find the values of the sine, cosine, and tangent..... 3
6. Prove that  $\cos(a-b) = \cos a \cos b + \sin a \sin b$ ..... 4
7. Assuming the value of the functions of the sum and of the difference of two arcs, prove that :
  - (a)  $\cos \frac{1}{2} a = \pm \sqrt{\frac{1 + \cos a}{2}}$ ..... 2
  - (b)  $\sin p - \sin q = 2 \sin \frac{1}{2} (p - q) \cos \frac{1}{2} (p + q)$ ..... 2
8. In a right-angled triangle given the hypotenuse and an acute angle; state the formulæ for finding the remaining parts..... 3
9. Explain, by means of a diagram, what measurements and what computations are necessary to determine, trigonometrically, the distance between two inaccessible objects, both of which can be seen from no one point ..... 6