

PLANE GEOMETRY

Tuesday, September 9, 1919—9.15 a. m. to 12.15 p. m., only

Answer eight questions. Papers entitled to less than 75 credits will not be accepted.

1 Prove that if the opposite sides of a quadrilateral are equal, the figure is a parallelogram.

2 Prove that two parallel chords of a circle intercept equal arcs.

3 Prove that if the angles of two triangles are respectively equal to each other, the triangles are similar.

4 Prove that the area of a triangle is equal to half the product of its base and its altitude.

5 Prove that two regular polygons of the same number of sides are similar.

6 From the point in which the altitudes drawn to the legs of an isosceles triangle intersect, a line is drawn to the vertex. Prove that the line bisects the angle at the vertex.

7 A triangle ABC is inscribed in a circle; the angle B is 35° and the minor arc AB is 120° . A tangent drawn at A meets BC produced at D . Draw the figure and mark the value of all the angles in the figure.

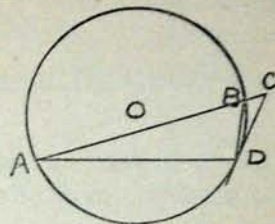
8 Construct a circle which shall be tangent to a given line AB at M and shall pass through a given point P .

9 The upper base of an isosceles trapezoid is $8''$, each leg is $5''$ and the projection of each leg on the base is $4''$. If the legs of the trapezoid are produced till they meet, find the altitudes of the two triangles thus formed.

10 Given AB a diameter of a circle, and AD and BC tangents, AC and BD intersecting at a point F on the circle. Prove that AB is the mean proportional between the lines AD and BC .

11 A semicircular field has an area of 77 square yards; find the perimeter of the field.

8 In the figure, CD is tangent to the circle, angle $C=42^\circ$, arc $BD=32^\circ$. Find in degrees the value of each of the angles of the triangle ABD . [12½]



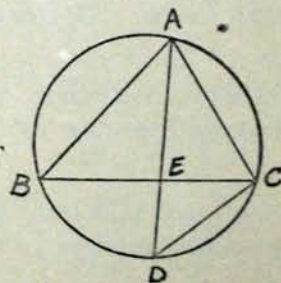
9 The diagonals of an equilateral parallelogram (rhombus) are 24 inches and 70 inches. Find (a) the area, (b) the perimeter, (c) the altitude. [12½]

10 Given a , b and c , lines of unequal length. Construct a fourth line x such that $x = \frac{ac}{b}$. Give proof. [12½]

11 a Construct a quadrilateral three of whose angles are 150° , 90° and 60° . [10½]

b How many degrees are there in the remaining angle? Why? [2]

12 Given a circle circumscribed about triangle ABC . D is the mid point of arc BC . AD and DC are drawn.



To prove $AB \times AC = \overline{AE}^2 + BE \times EC$

Assign a reason for each of the following statements:

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| 1 | $\angle BAD$ is measured by $\frac{1}{2}$ arc BD | [1] |
| | $\angle CAD$ is measured by $\frac{1}{2}$ arc CD | [1] |
| 2 | $\angle BAD = \angle CAD$ | [2] |
| 3 | $\angle B = \angle D$ | [2] |
| 4 | $\triangle BAE$ is similar to $\triangle DAC$ | [2] |
| 5 | $\frac{AB}{AE+ED} = \frac{AE}{AC}$ | [2] |
| 6 | $AB \times AC = \overline{AE}^2 + AE \times ED$ | [1] |
| 7 | $AE \times ED = BE \times EC$ | [2] |
| 8 | $AB \times AC = \overline{AE}^2 + BE \times EC$ | [2] |