

PLANE GEOMETRY

Friday, June 10, 1910—9.15 a. m. to 12.15 p. m., only

Write at the top of the first page of your answer paper (a) the name of the school where you have studied, (b) the number of weeks and recitations a week that you have had in geometry.

Five recitations a week for a school year, in a recognized academic school, is the regular requirement, and any statement showing less or other than this should be accompanied by a satisfactory claim or explanation made by the candidate and certified by the principal; otherwise such paper will be returned.

Answer eight questions, selecting two from each group.

Group I 1 Prove that the sum of the interior angles of any triangle is equal to two right angles.

2 Prove that the angle between two tangents from a point to a circle is bisected by the line joining the point with the center of the circle.

3 Prove that the line which bisects one leg of a trapezoid and is parallel to the bases is equal to half of the sum of the bases.

Group II 4 Prove that the angle between two secants is measured by half the difference of the intercepted arcs.

5 Prove that the areas of two similar triangles are to each other as the squares of any two homologous sides.

6 Prove that the area of a circle is equal to the circumference multiplied by half the radius.

Group III 7 In a circle whose radius is 10 inches find the area of a segment of 60° .

8 The centers of two circles, whose radii are 8 inches and 3 inches respectively, are 13 inches apart; find the length of their common external tangent.

9 The sides of a triangle are 13 inches, 14 inches and 15 inches; find the altitude on the longest side.

Group IV 10 Prove that a circumference drawn on one side of an equilateral triangle as a diameter bisects the other two sides of the triangle.

11 Show how to construct a circle passing through a given point and tangent to a given circle at a given point.

12 Show how to construct a triangle having given two sides and the angle opposite one of them if the given angle is acute.