

University of the State of New York

## Examinations Department

79th examination

### PLANE GEOMETRY

Wednesday, Jan. 27, 1892—9:15 a. m. to 12:15 p. m., only

40 credits, necessary to pass, 30

NOTE.—Draw carefully and neatly each figure in construction or proof, using letters instead of numerals. Arrange work logically.

1. Define and illustrate (a) oblique angle; (b) a third proportional; (c) tangent circles. 6
2. An exterior angle of a regular polygon equals one-fifth of a right angle; find the number of sides of the polygon. 4
3. Prove that a straight line perpendicular to a radius at its extremity is tangent to the circle. 4
4. Prove that if in a right triangle a perpendicular is drawn from the vertex of the right angle to the hypotenuse: I. The perpendicular is a mean proportional between the segments of the hypotenuse. II. Each side about the right angle is a mean proportional between the hypotenuse and the adjacent segment. 6
5. Prove that two regular polygons of the same number of sides are similar. 4
6. Solve the following and prove the correctness of each construction: (a) Through a given point to draw a tangent to a given circle. (Two cases.) 6
- (b) At a given point in a given line to construct an angle of  $30^\circ$ . 4
7. The sides of a rectangle inscribed in a circle are  $m$  and  $n$ ; find (a) the circumference of the circle; (b) its area. 6