### 1. 080101b, P.I. A2.A.38

Which relation is *not* a function?

[A] 
$$y = 2x + 4$$

[B] 
$$x = 3y - 2$$

[C] 
$$x = v^2 + 2x - 3$$
 [D]  $v = x^2 - 4x + 3$ 

[D] 
$$y = x^2 - 4x + 3$$

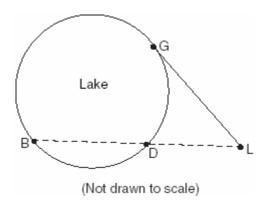
### 2. 080102b, P.I. A2.A.1

The solution set of |3x+2| < 1 contains

- [A] only positive real numbers
- [B] no real numbers
- [C] both positive and negative real numbers
- [D] only negative real numbers

#### 3. 080103b, P.I. G.G.53

In the accompanying diagram, cabins B and Gare located on the shore of a circular lake, and cabin L is located near the lake. Point D is a dock on the lake shore and is collinear with cabins B and L. The road between cabins G and L is 8 miles long and is tangent to the lake. The path between cabin L and dock D is 4 miles long.



What is the length, in miles, of  $\overline{BD}$ ?

- [A] 8
- [B] 12
- [C] 24
- [D] 4

## 4. 080104b, P.I. A2.A.22

The solution set of the equation  $\sqrt{x+6} = x$  is

- [A] { }
- [B] {-2}
- [C] {3}
- [D] {-2,3}

### 5. 080105b, P.I. G.G.61

Which transformation is a direct isometry?

- [A]  $D_{-2}$  [B]  $r_{v-axis}$  [C]  $D_2$  [D]  $T_{2.5}$

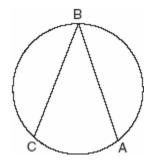
### **6.** 080106b, P.I. A2.A.2

The roots of the equation  $x^2 - 3x - 2 = 0$  are

- [A] real, rational, and unequal
- [B] real, rational, and equal
- [C] real, irrational, and unequal
- [D] imaginary

### 7. 080107b, P.I. G.G.53

The new corporate logo created by the design engineers at Magic Motors is shown in the accompanying diagram.



If chords  $\overline{BA}$  and  $\overline{BC}$  are congruent and  $\widehat{mBC} = 140$ , what is  $m \angle B$ ?

- [A] 40
- [B] 280
- [C] 80
- [D] 140

# 8. 080108b, P.I. A.A.44

At Mogul's Ski Resort, the beginner's slope is inclined at an angle of 12.3°, while the advanced slope is inclined at an angle of 26.4°. If Rudy skis 1,000 meters down the advanced slope while Valerie skis the same distance on the beginner's slope, how much longer was the horizontal distance that Valerie covered?

- [A] 895.7 m
- [B] 977.0 m
- [C] 231.6 m
- [D] 81.3 m

# 9. 080109b

A regular hexagon is inscribed in a circle. What is the ratio of the length of a side of the hexagon to the minor arc that it intercepts?

[A] 
$$\frac{3}{6}$$

[B] 
$$\frac{3}{\pi}$$

[C] 
$$\frac{6}{\pi}$$

[A] 
$$\frac{3}{6}$$
 [B]  $\frac{3}{\pi}$  [C]  $\frac{6}{\pi}$  [D]  $\frac{\pi}{6}$ 

# 10. 080110b, P.I. A2.A.19

If  $\log 5 = a$ , then  $\log 250$  can be expressed as

[C] 
$$10 + 2a$$

[D] 
$$2a + 1$$

## 11. 080111b, P.I. A.M.1

On a trip, a student drove 40 miles per hour for 2 hours and then drove 30 miles per hour for 3 hours. What is the student's average rate of speed, in miles per hour, for the whole trip?

### 12. 080112b, P.I. A.A.8

A ball is thrown straight up at an initial velocity of 54 feet per second. The height of the ball t seconds after it is thrown is given by the formula  $h(t) = 54t - 12t^2$ . How many seconds after the ball is thrown will it return to the ground?

#### 13. 080113b, P.I. A2.A.69

What is the period of the function  $y = 5 \sin 3x$ ?

[A] 
$$\frac{2\pi}{5}$$

[A] 
$$\frac{2\pi}{5}$$
 [B] 5 [C]  $\frac{2\pi}{3}$ 

## 14. 080114b, P.I. A.A.7

A cellular telephone company has two plans. Plan A charges \$11 a month and \$0.21 per minute. Plan B charges \$20 a month and \$0.10 per minute. After how much time, to the *nearest minute*, will the cost of plan A be equal to the cost of plan B?

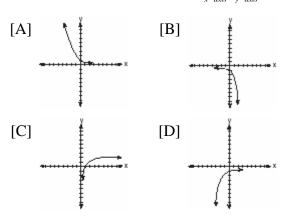
- [A] 1 hr 36 min
- [B] 81 hr 48 min
- [C] 1 hr 22 m
- [D] 81 hr 8 min

### 15. 080115b, P.I. G.G.61

The graph of f(x) is shown in the accompanying diagram.



Which graph represents  $f(x)_{r_{x-avis} \circ r_{y-avis}}$ ?



# 16. 080116b

A wedge-shaped piece is cut from a circular pizza. The radius of the pizza is 6 inches. The rounded edge of the crust of the piece measures 4.2 inches. To the nearest tenth, the angle of the pointed end of the piece of pizza, in radians, is

# 17. 080117b, P.I. A.A.18

If the length of a rectangular garden is represented by  $\frac{x^2 + 2x}{x^2 + 2x - 15}$  and its width is represented by  $\frac{2x-6}{2x+4}$ , which expression

represents the area of the garden?

[A] 
$$\frac{x}{x+5}$$

[B] 
$$x + 5$$

[D] 
$$\frac{x^2 + 2x}{2(x+5)}$$

# 18. 080118b, P.I. A2.A.27

Determine the value of x and y if  $2^y = 8^x$  and  $3^y = 3^{x+4}$ .

[A] 
$$x = 6$$
,  $y = 2$ 

[A] 
$$x = 6$$
,  $y = 2$  [B]  $x = -2$ ,  $y = -6$ 

[C] 
$$x = y$$

[D] 
$$x = 2, y = 6$$

# 19. 080119b, P.I. A.M.1

If Jamar can run  $\frac{3}{5}$  of a mile in 2 minutes 30 seconds, what is his rate in miles per minute?

[A] 
$$\frac{4}{5}$$

[A] 
$$\frac{4}{5}$$
 [B]  $3\frac{1}{10}$  [C]  $4\frac{1}{6}$  [D]  $\frac{6}{25}$ 

[C] 
$$4\frac{1}{6}$$

[D] 
$$\frac{6}{25}$$

### 20. 080120b, P.I. G.G.33

A box contains one 2-inch rod, one 3-inch rod, one 4-inch rod, and one 5-inch rod. What is the maximum number of different triangles that can be made using these rods as sides?

- [A] 3
- [B] 2
- [C] 1

[D] 4

# 21. 080121b, P.I. A2.A.67

If the sine of an angle is  $\frac{3}{5}$  and the angle is not in Quadrant I, what is the value of the cosine of the angle?

## 22. 080122b, P.I. A2.N.9

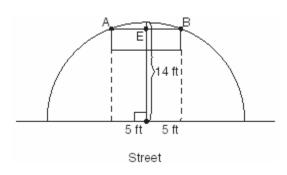
Show that the product of a + bi and its conjugate is a real number.

# 23. 080123b, P.I. A2.A.5

The price per person to rent a limousine for a prom varies inversely as the number of passengers. If five people rent the limousine, the cost is \$70 each. How many people are renting the limousine when the cost per *couple* is \$87.50?

### 24. 080124b P.I. G.G.48

The accompanying diagram shows a semicircular arch over a street that has a radius of 14 feet. A banner is attached to the arch at points A and B, such that AE = EB = 5feet. How many feet above the ground are these points of attachment for the banner?



# 25. 080125b, P.I. A2.A.23

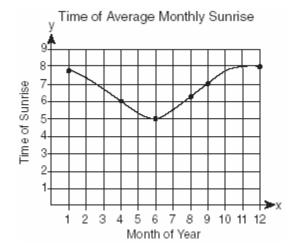
Working by herself, Mary requires 16 minutes more than Antoine to solve a mathematics problem. Working together, Mary and Antoine can solve the problem in 6 minutes. If this situation is represented by the equation  $\frac{6}{t} + \frac{6}{t+16} = 1$ , where t represents the number of minutes Antoine works alone to solve the problem, how many minutes will it take Antoine to solve the problem if he works by himself?

## **26.** 080126b, P.I. A2.A.76

If  $\sin x = \frac{4}{5}$ , where  $0^{\circ} < x < 90^{\circ}$ , find the value of  $\cos (x + 180^{\circ})$ .

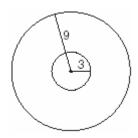
### 27. 080127b

The times of average monthly sunrise, as shown in the accompanying diagram, over the course of a 12-month interval can be modeled by the equation  $y = A\cos(Bx) + D$ . Determine the values of A, B, and D, and explain how you arrived at your values.



## 28. 080128b, P.I. A2.S.15

As shown in the accompanying diagram, a circular target with a radius of 9 inches has a bull's-eye that has a radius of 3 inches. If five arrows randomly hit the target, what is the probability that *at least* four hit the bull's-eye?



### 29. 080129b, P.I. A2.S.5

examination and received the following scores: 70, 60, 75, 68, 85, 86, 78, 72, 82, 88, 88, 73, 74, 79, 86, 82, 90, 92, 93, 73. Determine what percent of the students scored within one standard deviation of the mean. Do the results of the examination approximate a normal distribution? Justify your answer.

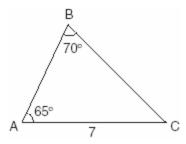
Twenty high school students took an

### 30. 080130b, P.I. A.G.1

A small, open-top packing box, similar to a shoebox without a lid, is three times as long as it is wide, and half as high as it is long. Each square inch of the bottom of the box costs \$0.008 to produce, while each square inch of any side costs \$0.003 to produce. Write a function for the cost of the box described above. Using this function, determine the dimensions of a box that would cost \$0.69 to produce.

## 31. 080131b, P.I. A2.A.73

In the accompanying diagram of  $\triangle ABC$ ,  $m \angle A = 65$ ,  $m \angle B = 70$ , and the side opposite vertex *B* is 7. Find the length of the side opposite vertex *A*, and find the area of  $\triangle ABC$ .



### **32.** 080132b, P.I. A2.A.27

The amount A, in milligrams, of a 10-milligram dose of a drug remaining in the body after t hours is given by the formula  $A = 10(0.8)^t$ . Find, to the *nearest tenth of an hour*, how long it takes for half of the drug dose to be left in the body.

## 33. 080133b, P.I. A2.S.7

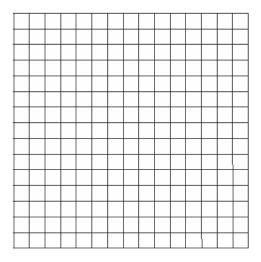
The availability of leaded gasoline in New York State is decreasing, as shown in the accompanying table.

Year	1984	1988	1992	1996	2000
Gallons Available (in thousands)	150	124	104	76	50

Determine a linear relationship for *x* (years) versus *y* (gallons available), based on the data given. The data should be entered using the year and gallons available (in thousands), such as (1984,150). If this relationship continues, determine the number of gallons of leaded gasoline available in New York State in the year 2005. If this relationship continues, during what year will leaded gasoline first become unavailable in New York State?

## **34.** 080134b, P.I. G.G.69

Given: A(1,6), B(7,9), C(13,6), and D(3,1)Prove: ABCD is a trapezoid. [The use of the accompanying grid is optional.]



- [1] C
- [2] D
- [3] <u>B</u>
- [4] C
- [5] D
- [6] C
- [7] A
- [8] D
- [9] B
- [10] D
- [11] C
- [12] B
- [13] <u>C</u>
- [14] <u>C</u>
- [15] D
- [16] C
- [17] <u>A</u>
- [18] <u>D</u>
- [19] D
- [20] A

- [2]  $-\frac{4}{5}$  or -0.8, and appropriate work is shown.
- [1]  $\frac{4}{5}$  or 0.8, and appropriate work is shown,

but the quadrant was not taken into consideration.

- or [1]  $-\frac{4}{5}$  or -0.8, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously
- [21] incorrect procedure.
  - [2] Appropriate work is shown, such as  $(a+bi)(a-bi) = a^2 + b^2$ .
  - [1] The conjugate is incorrect, but multiplication and substitution for  $i^2$  are appropriate.
  - or [1] The conjugate is correct, but one or more errors in multiplication and/or substitution for  $i^2$  are made.
  - [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously
- [22] incorrect procedure.
  - [2] 8, and appropriate work is shown, such as 5(70) = 43.75x.
  - [1] 4, and \$87.50 is used instead of \$43.75 per person.
  - or [1] Appropriate work is shown, but one computational error is made.
  - or [1] 8, but no work is shown.
  - [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously
- [23] incorrect procedure.

[2]  $\sqrt{171}$  or 13 or 13.1 or 13.08 or an equivalent answer, and appropriate work is shown, such as the use of the equation of a circle  $(x^2 + y^2 = r^2)$  or the Pythagorean theorem.

[1] Appropriate work is shown, but one computational error is made.

or [1] Incorrect analysis is shown, such as x = 5 and y = 14, but the work is concluded appropriately.

or [1] A correct answer is found, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

[2] 8 or an equivalent answer, and appropriate work is shown.

[1] The denominators are cleared correctly, such as 6(t+16)+6t=t(t+16), but the factoring is incorrect, or one error is made using the quadratic formula.

or [1] The denominators are not cleared correctly, but an equation of equal difficulty is solved.

or [1] 8 or an equivalent answer, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

[25] incorrect procedure.

[24]

[2]  $-\frac{3}{5}$ , and appropriate work is shown, such as  $\cos(x + 180) = \cos x \cos 180^\circ - \sin x \sin 180^\circ = \frac{3}{5}(-1) - \frac{4}{5}(0)$ .

or [2]  $-\frac{3}{5}$ , and appropriate work is shown,

such as cos(x + 180) = -cos x.

or [2]  $-\frac{3}{5}$ , and angle *x* is found, and correct substitution leads to cos(x + 180).

[1] Appropriate work is shown, but one computational error is made.

or [1]  $\cos x = \frac{4}{5}$  is found, but substitution

or  $[1] - \frac{3}{5}$ , but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously

[26] incorrect procedure.

errors are made.

[4] A = 1.5, B = 0.5, and D = 6.5 or an equivalent answer, and appropriate work is shown or an appropriate explanation is given for each number found.

[3] Correct answers are found, but appropriate work is shown or an appropriate explanation is given for only two of the numbers found.

[2] Only two correct answers are found, but appropriate work is shown or an appropriate explanation is given for the two answers.

[1] Only one correct answer is found, but appropriate work is shown or an appropriate explanation is given for that answer.

or [1] A = 1.5, B = 0.5, and D = 6.5 or an

or [1] A = 1.5, B = 0.5, and D = 6.5 or an equivalent answer, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously

[27] incorrect procedure.

[4] 
$$\frac{41}{59,049}$$
, and appropriate work is shown,

such as 
$${}_{5}C_{5}(\frac{1}{9})^{5} + {}_{5}C_{4}(\frac{1}{9})^{4}(\frac{8}{9})^{1}$$
.

- [3] Appropriate work is shown, but one computational error is made.
- or [3] The combination includes an incorrect setup for determining the probability of hitting the bull's-eye five times but a correct setup for determining the probability of hitting the bull's-eye four times, but an appropriate probability is found.
- [2] The probability of "exactly 4" is found. or [2] The probability of "at most 3" is found.
- [1] A probability of  $\frac{1}{9}$  is found, based on the area of the two circles.

or [1] 
$$\frac{41}{59,049}$$
, but no work is shown.

[28]

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- [4] 8.7 standard deviation, 70% within one standard deviation, and "Yes," and appropriate work is shown, and an appropriate justification is given. or [4] 8.7 standard deviation, 70% within one standard deviation, and "No," and appropriate work is shown, and an appropriate justification is given.
- [3] One error is made in determining the standard deviation or the percent, but all the other work is appropriate.
- [2] 8.7 and 70%, and appropriate work is shown, but no justification is given. or [2] The standard deviation is determined correctly, but more than one error is made when calculating the percent, but the justification is appropriate.
- [1] The standard deviation is determined correctly, but no further work is shown. or [1] The standard deviation is determined incorrectly, but the percent is appropriate, based on the incorrect standard deviation. [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect precedure.

[29] incorrect procedure.

[4]  $c(x) = 0.06x^2$  or an equivalent equation; width =  $\sqrt{11.5}$  inches or an equivalent, length =  $3\sqrt{11.5}$  inches or an equivalent, and height  $=\frac{3}{2}\sqrt{11.5}$  inches or an equivalent, and

appropriate work is shown.

- [3] Appropriate work is shown, but one computational error is made.
- or [3] One or more dimensions are represented incorrectly, but all further work is appropriate.
- or [3] The correct function is found and solved for x, but no further work is shown.
- [2] The dimensions are represented correctly, but the equation is incorrect, but all further work is appropriate.
- or [2] The dimensions are represented correctly, and the correct function is written, but further work is incomplete or is incorrect. [1] The dimensions are represented correctly, but the function is written and solved incorrectly.

or [1] 
$$\sqrt{11.5}$$
,  $3\sqrt{11.5}$ , and  $\frac{3}{2}\sqrt{11.5}$ , but no

work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously

[30] incorrect procedure.

- [4] BC = 6.75 and the area of  $\triangle ABC =$ 16.7055 or 16.71 or an equivalent answer, and appropriate work is shown, such as using the Law of Sines and the formula for the area of a triangle.
- [3] Appropriate work is shown, but one computational error is made.
- [2] Only the correct length of BC is found, and appropriate work is shown.
- or [2] The length of BC is found incorrectly, but an appropriate area of the triangle is found, based on the incorrect value of  $\overline{BC}$ .
- [1] The Law of Sines is used, and appropriate substitution is made, but no further work is shown.
- or [1] BC = 6.75 and the area of  $\triangle ABC =$ 16.7055 or 16.71 or an equivalent answer, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously
- [31] incorrect procedure.
  - [4] 3.1, and appropriate work is shown, such as  $5 = 10(0.8)^t$ .
  - [3] Appropriate work is shown, but one computational or rounding error is made. or [3] An incorrect value for A is used, but the equation is solved appropriately.
  - [2] An incorrect value for A is used, but the equation is solved appropriately, but one computational or rounding error is made.
  - [1] 3.1, but no work is shown.
  - [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously
- [32] incorrect procedure.

- [6] y = -6.2x + 12,451.2; 20.2 thousand; and 2008; and appropriate work is shown.
- [5] The correct equation is shown, but only the number of gallons or the year is correct.
- [4] The slope and *y*-intercept are incorrect, but the slope is negative and the number of gallons and the year are appropriate, based on the incorrect equation.
- [3] The slope and *y*-intercept are incorrect, but the slope is negative, but only the number of gallons or the year is appropriate, based on the incorrect equation.
- [2] The correct equation is shown, but the number of gallons and the year are not determined or are determined incorrectly. or [2] The incorrect equation y = 6.2x + 12,451.2 is shown, but appropriate work is shown for the number of gallons and the year.
- [1] An incorrect equation is shown with a negative slope, and the number of gallons and the year are not determined.
- or [1] 20.2 thousand and 2008, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

[33]

[6] The correct slopes of  $AB = \frac{1}{2}$  and

 $CD = \frac{1}{2}$  are found,  $\overline{AB} \| \overline{CD}$  is stated, and an explanation of why they are parallel is given.

The correct slopes of  $AD = -\frac{5}{2}$  and

 $BC = -\frac{1}{2}$  are found,  $\overline{AD}$  is not parallel to

 $\overline{BC}$  is stated, and an explanation of why they are not parallel is given. An explanation that ABCD is a trapezoid is given.

[5] The correct slopes of  $\overline{AB}$ ,  $\overline{CD}$ ,  $\overline{AD}$ , and  $\overline{BC}$  are found, and  $\overline{AB} \parallel \overline{CD}$  and

 $\overline{AD}$  not  $\|\overline{BC}\|$  are stated, but an explanation that ABCD is a trapezoid is not given.

or [5] One computational error is made in finding the slopes, but all further work is appropriate, based on the calculated slopes.

[4] The correct slope of  $\overline{AB}$  and  $\overline{CD}$  are found, and  $\overline{AB} \parallel \overline{CD}$  is stated, but incorrect

slopes of  $\overline{AD}$  and  $\overline{BC}$  are found, but an explanation of why they are not parallel is given, but an explanation that ABCD is a trapezoid is not given.

or [4] More than one computational error is made in finding the slopes, but  $\overline{AB}$  and  $\overline{CD}$  are found to have equal slopes and  $\overline{AD}$  and  $\overline{BC}$  to have different slopes, but an

explanation that ABCD is a trapezoid is given. [3] Incorrect slopes of  $\overline{AB}$ ,  $\overline{CD}$ ,  $\overline{AD}$ , and  $\overline{BC}$ 

are found, such as by using an incorrect formula,  $\overline{AB}$  and  $\overline{CD}$  are found to have equal slopes and  $\overline{AD}$  and  $\overline{BC}$  to have different

slopes and AD and BC to have different slopes, but an explanation that ABCD is a trapezoid is given.

- [2] Only the correct slopes of AB, CD, AD, and  $\overline{BC}$  are found, and appropriate work is shown.
- [1] Only two correct slopes are found, and [34] appropriate work is shown.

or [1] 
$$AB = \frac{1}{2}$$
,  $CD = \frac{1}{2}$ ,  $AD = -\frac{5}{2}$ , and

$$BC = -\frac{1}{2}$$
, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.