

Monday, January 25, 1909—9.15 a. m. to 12.15 p. m., only

Answer eight questions, selecting at least two from each group.

Group I 1 Solve as a quadratic $x^2 + 2x + 10 - \sqrt{x^2 + 2x + 10} = 20$
Verify two values of x obtained.

2 A laborer received \$15 for a certain number of days work; if he had received 25 cents less a day, it would have taken him 2 days longer to earn the same amount. How long did he work?

3 Solve $\begin{cases} x + y + \sqrt{x + y} = 12 \\ x - y + \sqrt{x - y} = 2 \end{cases}$

4 Factor three of the following:

$$x^4 + 4; \quad m^2 - 2mn + n^2 + 5m - 5n; \quad a^2 - n^2 - m^2 - 2ab + 2mn + b^2;$$

$$x^3 + 7x^2 - 7x - 49x^2 + 6x + 42$$

Group II 5 Find the value of $\frac{\sqrt{a} - \sqrt{x}}{\sqrt{a-x}}$ when $x = a$. Interpret your result.

6 Extract the square root of each of two of the following:
 $7 + 4\sqrt{3}$; $3 + \sqrt{5}$; $2a + 2\sqrt{a^2 - b^2}$

7 Simplify two of the following: $(3\sqrt[4]{\frac{1}{b}})^2$; $\sqrt[3]{\frac{a}{bc}} \cdot \sqrt{\frac{a}{bd}}$;
 $\frac{3\sqrt{11}}{2\sqrt{98}} \cdot \frac{7\sqrt{22}}{5}$; $\sqrt{24} + \sqrt{54} - \sqrt{6}$

8 Multiply $a^{\frac{1}{2}} + a^{\frac{1}{3}} - 3a^{\frac{1}{4}} + 1 - a^{-\frac{1}{4}} + a^{-\frac{1}{2}}$ by $a^{\frac{1}{4}} - 2 + a^{-\frac{1}{4}}$

Group III 9 Derive the formula for the last term and for the sum of an arithmetical progression.

10 In a geometrical progression $a = 2$, $r = \frac{1}{2}$, $l = \frac{1}{16}$; find s and n .

11 What two numbers whose difference is d are to each other as $a:b$?

12 Reduce each of the following to its simplest form with positive exponent: $a^8 \cdot a^{-2}$; $(3a)^{-5} \cdot (3a)^5$; $a^{m-3} \cdot a^{3-2m}$;

$$\frac{8a^{-x}b^{-y}z^2}{a^{3x}b^{5y}z^2}$$