1 On the set of axes below, $\overline{AB}$ is dilated by a scale factor of $\frac{5}{2}$ centered at point $P$.

Which statement is always true?
1) $\overline{PA} \cong \overline{A'A''}$
2) $\overline{AB} \parallel \overline{A'B''}$
3) $\overline{AB} = \overline{A'B''}$
4) $\frac{5}{2}(\overline{A'B''}) = \overline{AB}$

2 The coordinates of the vertices of parallelogram $CDEH$ are $C(-5,5)$, $D(2,5)$, $E(-1,-1)$, and $H(-8,-1)$. What are the coordinates of $P$, the point of intersection of diagonals $CE$ and $DH$?
1) $(-2,3)$
2) $(-2,2)$
3) $(-3,2)$
4) $(-3,-2)$

3 The coordinates of the endpoints of $\overline{QS}$ are $Q(-9,8)$ and $S(9,-4)$. Point $R$ is on $\overline{QS}$ such that $QR:RS$ is in the ratio of 1:2. What are the coordinates of point $R$?
1) $(0,2)$
2) $(3,0)$
3) $(-3,4)$
4) $(-6,6)$

4 If the altitudes of a triangle meet at one of the triangle’s vertices, then the triangle is
1) a right triangle
2) an acute triangle
3) an obtuse triangle
4) an equilateral triangle

5 In the diagram below of $\triangle ACD$, $\overline{DB}$ is a median to $\overline{AC}$, and $\overline{AB} \cong \overline{DB}$.

If $m\angle DAB = 32^\circ$, what is $m\angle BDC$?
1) $32^\circ$
2) $52^\circ$
3) $58^\circ$
4) $64^\circ$
6. What are the coordinates of the center and the length of the radius of the circle whose equation is $x^2 + y^2 = 8x - 6y + 39$?
   1) center (−4,3) and radius 64
   2) center (4,−3) and radius 64
   3) center (−4,3) and radius 8
   4) center (4,−3) and radius 8

7. In the diagram below of parallelogram $ABCD$, $AFGB$, $CF$ bisects $∠DCB$, $DG$ bisects $∠ADC$, and $CF$ and $DG$ intersect at $E$.

If $m∠B = 75°$, then the measure of $∠EFA$ is
   1) 142.5°
   2) 127.5°
   3) 52.5°
   4) 37.5°

8. What is an equation of a line that is perpendicular to the line whose equation is $2y + 3x = 1$?
   1) $y = \frac{2}{3}x + \frac{5}{2}$
   2) $y = \frac{3}{2}x + 2$
   3) $y = -\frac{2}{3}x + 1$
   4) $y = -\frac{3}{2}x + \frac{1}{2}$

9. Triangles $ABC$ and $RST$ are graphed on the set of axes below.

Which sequence of rigid motions will prove $△ABC ≅ △RST$?
   1) a line reflection over $y = x$
   2) a rotation of 180° centered at (1,0)
   3) a line reflection over the $x$-axis followed by a translation of 6 units right
   4) a line reflection over the $x$-axis followed by a line reflection over $y = 1$

10. If the line represented by $y = -\frac{1}{4}x - 2$ is dilated by a scale factor of 4 centered at the origin, which statement about the image is true?
    1) The slope is $-\frac{1}{4}$ and the $y$-intercept is $-8$.
    2) The slope is $-\frac{1}{4}$ and the $y$-intercept is $-2$.
    3) The slope is $-1$ and the $y$-intercept is $-8$.
    4) The slope is $-1$ and the $y$-intercept is $-2$. 

2
11. Square $MATH$ has a side length of 7 inches. Which three-dimensional object will be formed by continuously rotating square $MATH$ around side $AT$?
   1) a right cone with a base diameter of 7 inches
   2) a right cylinder with a diameter of 7 inches
   3) a right cone with a base radius of 7 inches
   4) a right cylinder with a radius of 7 inches

12. Circle $O$ with a radius of 9 is drawn below. The measure of central angle $AOC$ is 120°.

What is the area of the shaded sector of circle $O$?
   1) $6\pi$
   2) $12\pi$
   3) $27\pi$
   4) $54\pi$

13. In quadrilateral $QRST$, diagonals $QS$ and $RT$ intersect at $M$. Which statement would always prove quadrilateral $QRST$ is a parallelogram?
   1) $\angle TQR$ and $\angle QRS$ are supplementary.
   2) $QM \cong SM$ and $QT \cong RS$
   3) $QR \cong TS$ and $QT \cong RS$
   4) $QR \cong TS$ and $QT \parallel RS$

14. A standard-size golf ball has a diameter of 1.680 inches. The material used to make the golf ball weighs 0.6523 ounce per cubic inch. What is the weight, to the nearest hundredth of an ounce, of one golf ball?
   1) 1.10
   2) 1.62
   3) 2.48
   4) 3.81

15. Chelsea is sitting 8 feet from the foot of a tree. From where she is sitting, the angle of elevation of her line of sight to the top of the tree is 36°. If her line of sight starts 1.5 feet above ground, how tall is the tree, to the nearest foot?
   1) 8
   2) 7
   3) 6
   4) 4

16. In the diagram below of right triangle $ABC$, altitude $CD$ intersects hypotenuse $AB$ at $D$.

Which equation is always true?
   1) $\frac{AD}{AC} = \frac{CD}{BC}$
   2) $\frac{AD}{CD} = \frac{BD}{CD}$
   3) $\frac{AC}{CD} = \frac{BC}{CD}$
   4) $\frac{AD}{AC} = \frac{AC}{BD}$
17. A countertop for a kitchen is modeled with the dimensions shown below. An 18-inch by 21-inch rectangle will be removed for the installation of the sink.

What is the area of the top of the installed countertop, to the nearest square foot?
1) 26
2) 23
3) 22
4) 19

18. In the diagram below, $BC$ connects points $B$ and $C$ on the congruent sides of isosceles triangle $ADE$, such that $\triangle ABC$ is isosceles with vertex angle $A$.

If $AB = 10$, $BD = 5$, and $DE = 12$, what is the length of $BC$?
1) 6
2) 7
3) 8
4) 9

19. In $\triangle ABC$ below, angle $C$ is a right angle.

Which statement must be true?
1) $\sin A = \cos B$
2) $\sin A = \tan B$
3) $\sin B = \tan A$
4) $\sin B = \cos B$
20 In right triangle $RST$, altitude $TV$ is drawn to hypotenuse $RS$. If $RV = 12$ and $RT = 18$, what is the length of $SV$?
1) $6\sqrt{5}$
2) 15
3) $6\sqrt{6}$
4) 27

21 What is the volume, in cubic centimeters, of a right square pyramid with base edges that are 64 cm long and a slant height of 40 cm?
1) 8192.0
2) 13,653.3
3) 32,768.0
4) 54,613.3

22 In the diagram below, chords $PQ$ and $RS$ of circle $O$ intersect at $T$.

Which relationship must always be true?
1) $RT = TQ$
2) $RT = TS$
3) $RT + TS = PT + TQ$
4) $RT \times TS = PT \times TQ$

23 A rhombus is graphed on the set of axes below.

Which transformation would carry the rhombus onto itself?
1) $180^\circ$ rotation counterclockwise about the origin
2) reflection over the line $y = \frac{1}{2}x + 1$
3) reflection over the line $y = 0$
4) reflection over the line $x = 0$

24 A 15-foot ladder leans against a wall and makes an angle of $65^\circ$ with the ground. What is the horizontal distance from the wall to the base of the ladder, to the nearest tenth of a foot?
1) 6.3
2) 7.0
3) 12.9
4) 13.6
25 In parallelogram $ABCD$ shown below, $m\angle DAC = 98^\circ$ and $m\angle ACD = 36^\circ$.

What is the measure of angle $B$? Explain why.

26 An airplane took off at a constant angle of elevation. After the plane traveled for 25 miles, it reached an altitude of 5 miles, as modeled below.

To the nearest tenth of a degree, what was the angle of elevation?

27 On the set of axes below, $\triangle ABC \cong \triangle DEF$.

Describe a sequence of rigid motions that maps $\triangle ABC$ onto $\triangle DEF$.

28 The vertices of $\triangle ABC$ have coordinates $A(-2,-1)$, $B(10,-1)$, and $C(4,4)$. Determine and state the area of $\triangle ABC$. [The use of the set of axes below is optional.]
29. Using the construction below, state the degree measure of \(\angle CAD\). Explain why.

[Diagram of construction]

30. In the diagram below of circle \(K\), secant \(PLKE\) and tangent \(PZ\) are drawn from external point \(P\).

If \(m\angle Z = 56^\circ\), determine and state the degree measure of angle \(P\).

[Diagram of circle with secant and tangent]

31. A large water basin is in the shape of a right cylinder. The inside of the basin has a diameter of \(8 \frac{1}{4}\) feet and a height of 3 feet. Determine and state, to the nearest cubic foot, the number of cubic feet of water that it will take to fill the basin to a level of \(1 \frac{1}{2}\) foot from the top.

32. Triangle \(ABC\) is shown below. Using a compass and straightedge, construct the dilation of \(\triangle ABC\) centered at \(B\) with a scale factor of 2. [Leave all construction marks.]

[Diagram of triangle with dilation]

Is the image of \(\triangle ABC\) similar to the original triangle? Explain why.

33. In the diagram below, \(\triangle ABE \cong \triangle CBD\).

[Diagram of triangles]

Prove: \(\triangle AFD \cong \triangle CFE\)
34  A cargo trailer, pictured below, can be modeled by a rectangular prism and a triangular prism. Inside the trailer, the rectangular prism measures 6 feet wide and 10 feet long. The walls that form the triangular prism each measure 4 feet wide inside the trailer. The diagram below is of the floor, showing the inside measurements of the trailer.

If the inside height of the trailer is 6.5 feet, what is the total volume of the inside of the trailer, to the nearest cubic foot?

35  The coordinates of the vertices of $\triangle ABC$ are $A(1,2)$, $B(-5,3)$, and $C(-6,-3)$. Prove that $\triangle ABC$ is isosceles. State the coordinates of point $D$ such that quadrilateral $ABCD$ is a square. Prove that your quadrilateral $ABCD$ is a square. [The use of the set of axes below is optional.]
0819geo
Answer Section

1 ANS: 2 PTS: 2 REF: 081901geo NAT: G.SRT.A.1 TOP: Line Dilations

2 ANS: 3
\[ M_x = \frac{-5 + 1}{2} = \frac{6}{2} = 3 \quad M_y = \frac{5 + 1}{2} = \frac{4}{2} = 2 \]

PTS: 2 REF: 081902geo NAT: G.GPE.B.4 TOP: Quadrilaterals in the Coordinate Plane KEY: general

3 ANS: 3
\[-9 + \frac{1}{3}(9 - 9) = -9 + \frac{1}{3}(18) = -9 + 6 = -3 \quad 8 + \frac{1}{3}(-4 - 8) = 8 + \frac{1}{3}(-12) = 8 - 4 = 4 \]

PTS: 2 REF: 081903geo NAT: G.GPE.B.6 TOP: Directed Line Segments

4 ANS: 1 PTS: 2 REF: 081904geo NAT: G.CO.C.10 TOP: Centroid, Orthocenter, Incenter and Circumcenter

5 ANS: 3

PTS: 2 REF: 081905geo NAT: G.CO.C.10 TOP: Exterior Angle Theorem

6 ANS: 4
\[ x^2 - 8x + y^2 + 6y = 39 \]
\[ x^2 - 8x + 16 + y^2 + 6y + 9 = 39 + 16 + 9 \]
\[ (x - 4)^2 + (y + 3)^2 = 64 \]

PTS: 2 REF: 081906geo NAT: G.GPE.A.1 TOP: Equations of Circles KEY: completing the square

7 ANS: 2

8 ANS: 1
\[ m = \frac{-A}{B} = \frac{-3}{2} \quad m_\perp = \frac{2}{3} \]

PTS: 2 REF: 081908geo NAT: G.GPE.B.5 TOP: Parallel and Perpendicular Lines
KEY: identify perpendicular lines

9 ANS: 2 PTS: 2 REF: 081909geo NAT: G.CO.A.5
TOP: Compositions of Transformations KEY: identify

10 ANS: 1
A dilation by a scale factor of 4 centered at the origin preserves parallelism and \((0, -2) \rightarrow (0, -8)\).

PTS: 2 REF: 081910geo NAT: G.SRT.A.1 TOP: Line Dilations

11 ANS: 4 PTS: 2 REF: 081911geo NAT: G.GMD.B.4
TOP: Rotations of Two-Dimensional Objects

12 ANS: 4
\[ \left( \frac{360 - 120}{360} \right) (\pi)(9^2) = 54\pi \]

PTS: 2 REF: 081912geo NAT: G.C.B.5 TOP: Sectors

13 ANS: 3 PTS: 2 REF: 081913geo NAT: G.CO.C.11
TOP: Special Quadrilaterals

14 ANS: 2
\[ \frac{4}{3} \pi \times \left( \frac{1.68}{2} \right)^3 \times 0.6523 \approx 1.62 \]

PTS: 2 REF: 081914geo NAT: G.MG.A.2 TOP: Density

15 ANS: 2
\[ \tan 36^\circ = \frac{x}{8} \quad 5.8 + 1.5 \approx 7 \]
\[ x \approx 5.8 \]

PTS: 2 REF: 081915geo NAT: G.SRT.C.8 TOP: Using Trigonometry to Find a Side

16 ANS: 1 PTS: 2 REF: 081916geo NAT: G.SRT.B.5
TOP: Similarity KEY: leg

17 ANS: 4
\[ (8 \times 2) + (3 \times 2) - \left( \frac{18}{12} \times \frac{21}{12} \right) \approx 19 \]

PTS: 2 REF: 081917geo NAT: G.MG.A.3 TOP: Compositions of Polygons and Circles
18  \[ \frac{10}{x} = \frac{15}{12} \]
   \[ x = 8 \]
   PTS: 2  REF: 081918geo  NAT: G.SRT.B.5  TOP: Similarity
   KEY: basic
19  ANS: 1  PTS: 2  REF: 081919geo  NAT: G.SRT.C.7
   TOP: Cofunctions
20  ANS: 2
   \[ 18^2 = 12(x + 12) \]
   \[ 324 = 12(x + 12) \]
   \[ 27 = x + 12 \]
   \[ x = 15 \]
   PTS: 2  REF: 081920geo  NAT: G.SRT.B.5  TOP: Similarity
   KEY: leg
21  ANS: 3
   \[ \sqrt{40^2 - \left( \frac{64}{2} \right)^2} = 24 \]
   \[ V = \frac{1}{3} (64)^2 \cdot 24 = 32768 \]
   PTS: 2  REF: 081921geo  NAT: G.GMD.A.3  TOP: Volume
   KEY: pyramids
22  ANS: 4  PTS: 2  REF: 081922geo  NAT: G.C.A.2
   TOP: Chords, Secants and Tangents
   KEY: intersecting chords, length
23  ANS: 4  PTS: 2  REF: 081923geo  NAT: G.CO.A.3
   TOP: Mapping a Polygon onto Itself
24  ANS: 1
   \[ \cos 65 = \frac{x}{15} \]
   \[ x \approx 6.3 \]
   PTS: 2  REF: 081924geo  NAT: G.SRT.C.8  TOP: Using Trigonometry to Find a Side
25  ANS:
   \[ \angle D = 46^\circ \] because the angles of a triangle equal 180°. \[ \angle B = 46^\circ \] because opposite angles of a parallelogram are congruent.
26  ANS:
   \[ \sin^{-1} \left( \frac{5}{25} \right) = 11.5 \]
   PTS: 2  REF: 081926geo  NAT: G.SRT.C.8  TOP: Using Trigonometry to Find an Angle
27 ANS:
\[ r_y = 2 \quad r_{-y-axis} \]

PTS: 2  REF: 081927geo  NAT: G.CO.A.5  TOP: Compositions of Transformations
KEY: identify

28 ANS:
\[ \frac{1}{2} \times 5 \times 12 = 30 \]

PTS: 2  REF: 081928geo  NAT: G.GPE.B.7  TOP: Polygons in the Coordinate Plane

29 ANS:
30° \( \angle CAD \) is an equilateral triangle, so \( \angle CAB = 60° \). Since \( AD \) is an angle bisector, \( \angle CAD = 30° \).

PTS: 2  REF: 081929geo  NAT: G.CO.D.12  TOP: Constructions
KEY: equilateral triangles

30 ANS:
\[ \frac{124}{2} - \frac{56}{2} = 34 \]

PTS: 2  REF: 081930geo  NAT: G.C.A.2  TOP: Chords, Secants and Tangents
KEY: secant and tangent drawn from common point, angle

31 ANS:
\[ \left( \frac{2.5}{3} \right) \left( \pi \right) \left( \frac{8.25}{2} \right)^2 \approx 134 \]

PTS: 2  REF: 081931geo  NAT: G.GMD.A.3  TOP: Volume
KEY: cylinders

32 ANS:
Yes, because a dilation preserves angle measure.

PTS: 4  REF: 081932geo  NAT: G.CO.D.12  TOP: Constructions
KEY: congruent and similar figures

33 ANS:
\( \triangle ABE \cong \triangle CBD \) (given); \( \angle A \cong \angle C \) (CPCTC); \( \angle AFD \cong \angle CFE \) (vertical angles are congruent); \( AB \cong CB \), \( DB \cong EB \) (CPCTC); \( AD \cong CE \) (segment subtraction); \( \triangle AFD \cong \triangle CFE \) (AAS)

PTS: 4  REF: 081933geo  NAT: G.SRT.B.5  TOP: Triangle Proofs
KEY: proof
34 ANS:
\[ \left( (10 \times 6) + \sqrt{7(7-6)(7-4)(7-4)} \right)(6.5) \approx 442 \]

PTS: 4       REF: 081934geo   NAT: G.GMD.A.3   TOP: Volume
KEY: compositions

35 ANS:
\[ AB = \sqrt{(-5-1)^2 + (3-2)^2} = \sqrt{37}, \quad BC = \sqrt{(-5-6)^2 + (3-(-3))^2} = \sqrt{37} \quad \text{(because } AB = BC, \triangle ABC \text{ is isosceles).} \]
\[ AD = \sqrt{(1-0)^2 + (2-(-4))^2} = \sqrt{37}, \quad CD = \sqrt{(-6-0)^2 + (-3-(-4))^2} = \sqrt{37}, \]
\[ m_{AB} = \frac{3-2}{-5-1} = \frac{1}{6}, \quad m_{CD} = \frac{3-(-3)}{-5-(-6)} = 6 \quad \text{(} ABCD \text{ is a square because all four sides are congruent, consecutive sides are perpendicular since slopes are opposite reciprocals and so } \angle B \text{ is a right angle).} \]

PTS: 6       REF: 081935geo   NAT: G.GPE.B.4   TOP: Quadrilaterals in the Coordinate Plane
KEY: grids