

ELEMENTARY ALGEBRA

Monday, June 15, 1908—9.15 a. m. to 12.15 p. m., only

Answer eight questions, selecting at least two from each group.

Group I 1 Reduce the following fraction to lowest terms:

$$\frac{4a^2 + 4}{8a^2 + 12a^2 + 12a + 6}$$

2 Answer either *a* or *b*:

a Give a rule for writing the square of any polynomial.

b Collect into parentheses the coefficients of *x*, *y* and *z* in the following:

$$2ax - 3by - 7cz - 2bx + 2cx + 8cz - 2cx - cy - cz$$

3 Factor four of the following: $x^4 + x^3 + x^2 + x$; $x^3 - 8$; $x^2 + 2x + 1 - y^2 - 2y - 1$; $49m^4 + 110m^2n^2 + 81n^4$; $x^2 + y^2$

4 A man having 10 hours at his disposal made an excursion, riding out at the rate of 10 miles an hour and returning on foot at the rate of 3 miles an hour; find the distance he rode.

Group II 5 Extract the square roots of the following polynomials:

$$4x^5 - 20x^4 - 4x^3 + 25x^2 + 10x + 1$$

$$1 + 10x + 25x^2 - 4x^3 - 20x^4 + 4x^5$$

Compare the roots and explain why the signs appear as they do. [3 credits for the explanation.]

6 Simplify $2\sqrt[3]{40} + 3\sqrt[3]{108} + \sqrt[3]{500} - \sqrt[3]{320} - 2\sqrt[3]{1372}$

7 Solve $\sqrt{x+4} + \sqrt{2x-1} = 6$

8 Prove that if four quantities are in proportion the product of the extremes is equal to the product of the means.

Group III 9 If the square root of $\frac{2}{3}$ of a number is subtracted from the number the remainder will be 140; find the number.

10 Solve $\begin{cases} x + y = 5 \\ x^2 + y^2 = 35 \end{cases}$

11 For building 108 rods of stone wall, 6 days fewer would have been required if 3 rods more a day had been built; find the number of rods built per day.

12 A man invests $\frac{2}{3}$ of his capital at 4% and the rest at 3 $\frac{1}{2}$ %; his annual income is \$76. Find his capital.