

# University of the State of New York

77TH EXAMINATION

## CONIC SECTIONS

TUESDAY, JUNE 9, 1891—9 : 15 A. M. to 12 : 15 P. M., only

*40 credits, necessary to pass, 30*

*Credits allowed each answer depend on its completeness and accuracy*

NOTE.—Draw carefully and neatly each figure in construction or proof, using letters instead of numbers. Arrange work clearly and logically.

1. Given two points of a parabola and its directrix to find the focus. 3
2. Prove that the ordinate of any point of a parabola is a mean proportional between the latus rectum and the abscissa of the point. 6
3. Prove that the subtangent of a parabola is bisected at the vertex. 4
4. Describe a method of drawing an ellipse. 3
5. Prove that if  $d$  represents the abscissa of any point of an ellipse,  $r$  and  $r'$  its focal radii,  $2a$  its major axis and  $e$  its eccentricity :  

$$r = a + ed \text{ and } r' = a - ed. \quad 8$$
6. Draw a tangent and a normal at a given point of an ellipse. 6
7. Find any number of points in an hyperbola, the foci and  $2a$  the constant difference being given. 4
8. Prove that, if through a point  $P$  of an hyperbola, a line be drawn, bisecting the angle formed by the focal radii, every point of this line except  $P$  is on the convex side of the curve. 6