ALGEBRA II

The University of the State of New York
REGENTS HIGH SCHOOL EXAMINATION

ALGEBRA II

Friday, June 21, 2019 — 1:15 to 4:15 p.m., only

Student Name: _________________________________________________________

School Name: ______________________________________________________________

The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

Print your name and the name of your school on the lines above.

A separate answer sheet for Part I has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 37 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. All work should be written in pen, except graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale.

The formulas that you may need to answer some questions in this examination are found at the end of the examination. This sheet is perforated so you may remove it from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will not be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice...
A graphing calculator and a straightedge (ruler) must be available for you to use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.
Part I

Answer all 24 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For each statement or question, choose the word or expression that, of those given, best completes the statement or answers the question. Record your answers on your separate answer sheet. [48]

1 A sociologist reviews randomly selected surveillance videos from a public park over a period of several years and records the amount of time people spent on a smartphone. The statistical procedure the sociologist used is called
(1) a census (3) an observational study
(2) an experiment (4) a sample survey

2 Which statement(s) are true for all real numbers?

I \((x - y)^2 = x^2 + y^2\)
II \((x + y)^3 = x^3 + 3xy + y^3\)

(1) I, only (3) I and II
(2) II, only (4) neither I nor II

3 What is the solution set of the following system of equations?

\[
\begin{align*}
y &= 3x + 6 \\
y &= (x + 4)^2 - 10
\end{align*}
\]

(1) \(\{(−5,−9)\}\) (3) \(\{(0,6),(−5,−9)\}\)
(2) \(\{(5,21)\}\) (4) \(\{(0,6),(5,21)\}\)

Use this space for computations.
4 Irma initially ran one mile in over ten minutes. She then began a training program to reduce her one-mile time. She recorded her one-mile time once a week for twelve consecutive weeks, as modeled in the graph below.

Which statement regarding Irma's one-mile training program is correct?

(1) Her one-mile speed increased as the number of weeks increased.
(2) Her one-mile speed decreased as the number of weeks increased.
(3) If the trend continues, she will run under a six-minute mile by week thirteen.
(4) She reduced her one-mile time the most between weeks ten and twelve.

5 A 7-year lease for office space states that the annual rent is $85,000 for the first year and will increase by 6% each additional year of the lease. What will the total rent expense be for the entire 7-year lease?

(1) $42,809.63 (2) $90,425.53
(3) $595,000.00 (4) $713,476.20
6 The graph of \( y = f(x) \) is shown below.

Which expression defines \( f(x) \)?

(1) \( 2x \) 
(2) \( 5(2^x) \) 
(3) \( 5\left(2^{\frac{x}{2}}\right) \) 
(4) \( 5(2^{2x}) \)

7 Given \( P(x) = x^3 - 3x^2 - 2x + 4 \), which statement is true?

(1) \( (x - 1) \) is a factor because \( P(1) = 2 \).
(2) \( (x + 1) \) is a factor because \( P(-1) = 2 \).
(3) \( (x + 1) \) is a factor because \( P(1) = 0 \).
(4) \( (x - 1) \) is a factor because \( P(1) = 0 \).

8 For \( x \geq 0 \), which equation is false?

(1) \( \left(\frac{3}{2}\right)^2 = \sqrt[4]{x^3} \) 
(2) \( \left(\frac{3}{2}\right)^{\frac{1}{2}} = \sqrt[4]{x^3} \) 
(3) \( \left(\frac{3}{2}\right)^{\frac{1}{2}} = \sqrt[4]{x^3} \) 
(4) \( \left(\frac{2}{3}\right)^2 = \sqrt[3]{x^4} \)
9 What is the inverse of the function \( y = 4x + 5 \)?

(1) \( x = \frac{1}{4}y - \frac{5}{4} \)  \hspace{1cm} (3) \( y = 4x - 5 \)

(2) \( y = \frac{1}{4}x - \frac{5}{4} \)  \hspace{1cm} (4) \( y = \frac{1}{4x + 5} \)

10 Which situation could be modeled using a geometric sequence?

(1) A cell phone company charges $30.00 per month for 2 gigabytes of data and $12.50 for each additional gigabyte of data.

(2) The temperature in your car is 79°. You lower the temperature of your air conditioning by 2° every 3 minutes in order to find a comfortable temperature.

(3) David’s parents have set a limit of 50 minutes per week that he may play online games during the school year. However, they will increase his time by 5% per week for the next ten weeks.

(4) Sarah has $100.00 in her piggy bank and saves an additional $15.00 each week.

11 The completely factored form of \( n^4 - 9n^2 + 4n^3 - 36n - 12n^2 + 108 \) is

(1) \( (n^2 - 9)(n + 6)(n - 2) \)

(2) \( (n + 3)(n - 3)(n + 6)(n - 2) \)

(3) \( (n - 3)(n + 3)(n + 6)(n - 2) \)

(4) \( (n + 3)(n - 3)(n - 6)(n + 2) \)
What is the solution when the equation $wx^2 + w = 0$ is solved for $x$, where $w$ is a positive integer?

(1) $-1$  (3) 6
(2) 0  (4) $\pm i$

A group of students was trying to determine the proportion of candies in a bag that are blue. The company claims that 24% of candies in bags are blue. A simulation was run 100 times with a sample size of 50, based on the premise that 24% of the candies are blue. The approximately normal results of the simulation are shown in the dot plot below.

The simulation results in a mean of 0.254 and a standard deviation of 0.060. Based on this simulation, what is a plausible interval containing the middle 95% of the data?

(1) (0.194, 0.314)  (3) $(-0.448, 0.568)$
(2) (0.134, 0.374)  (4) (0.254, 0.374)
14 Selected values for the functions $f$ and $g$ are shown in the tables below.

<table>
<thead>
<tr>
<th>$x$</th>
<th>$f(x)$</th>
<th>$x$</th>
<th>$g(x)$</th>
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<tr>
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<td>-1.01</td>
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<td>-6</td>
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<td>2.53</td>
<td>13.11</td>
<td>3.01</td>
</tr>
<tr>
<td>9.01</td>
<td>3.01</td>
<td>16.52</td>
<td>3.29</td>
</tr>
</tbody>
</table>

A solution to the equation $f(x) = g(x)$ is

(1) 0  \hspace{1cm} (3) 3.01
(2) 2.53 \hspace{1cm} (4) 8.52

15 The expression $6 - (3x - 2i)^2$ is equivalent to

(1) $-9x^2 + 12xi + 10$ \hspace{1cm} (3) $-9x^2 + 10$
(2) $9x^2 - 12xi + 2$ \hspace{1cm} (4) $-9x^2 + 12xi - 4i + 6$

16 A number, minus twenty times its reciprocal, equals eight.
   The number is

(1) 10 or $-2$ \hspace{1cm} (3) $-10$ or $-2$
(2) 10 or 2 \hspace{1cm} (4) $-10$ or 2
17 A savings account, $S$, has an initial value of $50. The account grows at a 2% interest rate compounded $n$ times per year, $t$, according to the function below.

$$S(t) = 50\left(1 + \frac{0.02}{n}\right)^{nt}$$

Which statement about the account is correct?

1. As the value of $n$ increases, the amount of interest per year decreases.
2. As the value of $n$ increases, the value of the account approaches the function $S(t) = 50e^{0.02t}$.
3. As the value of $n$ decreases to one, the amount of interest per year increases.
4. As the value of $n$ decreases to one, the value of the account approaches the function $S(t) = 50(1 - 0.02)^t$.

18 There are 400 students in the senior class at Oak Creek High School. All of these students took the SAT. The distribution of their SAT scores is approximately normal. The number of students who scored within 2 standard deviations of the mean is approximately

1. 75  (3) 300
2. 95  (4) 380

19 The solution set for the equation $b = \sqrt{2b^2 - 64}$ is

1. $\{-8\}$  (3) $\{\pm 8\}$
2. $\{8\}$  (4) $\{\}$
20 Which table best represents an exponential relationship?

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<td>2</td>
</tr>
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<td>4</td>
<td>1</td>
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<td>(\frac{1}{2})</td>
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(1) 

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(2) 

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(3) 

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<td>3</td>
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<td>4</td>
<td>64</td>
</tr>
<tr>
<td>5</td>
<td>125</td>
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</tbody>
</table>

(4) 

21 A sketch of \(r(x)\) is shown below.

An equation for \(r(x)\) could be

1. \(r(x) = (x - a)(x + b)(x + c)\)
2. \(r(x) = (x + a)(x - b)(x - c)^2\)
3. \(r(x) = (x + a)(x - b)(x - c)\)
4. \(r(x) = (x - a)(x + b)(x + c)^2\)
22 The temperature, in degrees Fahrenheit, in Times Square during a day in August can be predicted by the function \( T(x) = 8\sin(0.3x - 3) + 74 \), where \( x \) is the number of hours after midnight. According to this model, the predicted temperature, to the nearest degree Fahrenheit, at 7 P.M. is

(1) 68  
(2) 74  
(3) 77  
(4) 81

23 Consider the system of equations below:

\[
\begin{align*}
x + y - z &= 6 \\
2x - 3y + 2z &= -19 \\
-x + 4y - z &= 17
\end{align*}
\]

Which number is not the value of any variable in the solution of the system?

(1) -1  
(2) 2  
(3) 3  
(4) -4

24 Camryn puts $400 into a savings account that earns 6% annually. The amount in her account can be modeled by \( C(t) = 400(1.06)^t \) where \( t \) is the time in years. Which expression best approximates the amount of money in her account using a weekly growth rate?

(1) \( 400(1.001153846)^t \)  
(2) \( 400(1.001121184)^t \)  
(3) \( 400(1.001153846)^{52t} \)  
(4) \( 400(1.001121184)^{52t} \)
### Part II

Answer all 8 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [16]

The table below shows the number of hours of daylight on the first day of each month in Rochester, NY.

<table>
<thead>
<tr>
<th>Month</th>
<th>Hours of Daylight</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jan.</td>
<td>9.4</td>
</tr>
<tr>
<td>Feb.</td>
<td>10.6</td>
</tr>
<tr>
<td>March</td>
<td>11.9</td>
</tr>
<tr>
<td>April</td>
<td>13.9</td>
</tr>
<tr>
<td>May</td>
<td>14.7</td>
</tr>
<tr>
<td>June</td>
<td>15.4</td>
</tr>
<tr>
<td>July</td>
<td>15.1</td>
</tr>
<tr>
<td>Aug.</td>
<td>13.9</td>
</tr>
<tr>
<td>Sept.</td>
<td>12.5</td>
</tr>
<tr>
<td>Oct.</td>
<td>11.1</td>
</tr>
<tr>
<td>Nov.</td>
<td>9.7</td>
</tr>
<tr>
<td>Dec.</td>
<td>9.0</td>
</tr>
</tbody>
</table>

Given the data, what is the average rate of change in hours of daylight per month from January 1st to April 1st?

Interpret what this means in the context of the problem.
26 Algebraically solve for $x$:

\[
\frac{7}{2x} - \frac{2}{x + 1} = \frac{1}{4}
\]
27 Graph \( f(x) = \log_2(x + 6) \) on the set of axes below.
28 Given $\tan \theta = \frac{7}{24}$, and $\theta$ terminates in Quadrant III, determine the value of $\cos \theta$.

29 Kenzie believes that for $x \geq 0$, the expression $(\sqrt[7]{x^3})(\sqrt[5]{x^3})$ is equivalent to $\sqrt[35]{x^6}$. Is she correct? Justify your response algebraically.
When the function \( p(x) \) is divided by \( x - 1 \) the quotient is \( x^2 + 7 + \frac{5}{x - 1} \). State \( p(x) \) in standard form.
31 Write a recursive formula for the sequence 6, 9, 13.5, 20.25, . . .
Robin flips a coin 100 times. It lands heads up 43 times, and she wonders if the coin is unfair. She runs a computer simulation of 750 samples of 100 fair coin flips. The output of the proportion of heads is shown below.

Do the results of the simulation provide strong evidence that Robin’s coin is unfair? Explain your answer.
Factor completely over the set of integers: $16x^4 - 81$

Sara graphed the polynomial $y = 16x^4 - 81$ and stated “All the roots of $y = 16x^4 - 81$ are real.” Is Sara correct? Explain your reasoning.
The half-life of a radioactive substance is 15 years.

Write an equation that can be used to determine the amount, \( s(t) \), of 200 grams of this substance that remains after \( t \) years.

Determine algebraically, to the nearest year, how long it will take for \( \frac{1}{10} \) of this substance to remain.
35 Determine an equation for the parabola with focus $(4, -1)$ and directrix $y = -5$.
(Use of the grid below is optional.)
Juan and Filipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

<table>
<thead>
<tr>
<th></th>
<th>Juan Wins</th>
<th>Filipe Wins</th>
</tr>
</thead>
<tbody>
<tr>
<td>Short Practice</td>
<td>8</td>
<td>10</td>
</tr>
<tr>
<td>Time</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Long Practice</td>
<td>15</td>
<td>12</td>
</tr>
<tr>
<td>Time</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Given that the practice time was long, determine the exact probability that Filipe wins the next match.

Determine whether or not the two events “Filipe wins” and “long practice time” are independent. Justify your answer.
Part IV

Answer the question in this part. A correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided to determine your answer. Note that diagrams are not necessarily drawn to scale. A correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [6]

37 Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function \( f(t) = -13\cos(0.8\pi t) + 13 \), where \( t \) represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of \( f(t) \).

Interpret what the period represents in this context.

Question 37 is continued on the next page.
Question 37 continued

On the grid below, graph \emph{at least one} cycle of \( f(t) \) that includes the \( y \)-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.
Scrap Graph Paper — This sheet will *not* be scored.
Scrap Graph Paper — This sheet will *not* be scored.
### High School Math Reference Sheet

- 1 inch = 2.54 centimeters
- 1 meter = 39.37 inches
- 1 mile = 5280 feet
- 1 mile = 1760 yards
- 1 mile = 1.609 kilometers

- 1 kilometer = 0.62 mile
- 1 pound = 16 ounces
- 1 pound = 0.454 kilogram
- 1 kilogram = 2.2 pounds
- 1 ton = 2000 pounds

- 1 cup = 8 fluid ounces
- 1 pint = 2 cups
- 1 quart = 2 pints
- 1 gallon = 4 quarts
- 1 gallon = 3.785 liters
- 1 liter = 0.264 gallon
- 1 liter = 1000 cubic centimeters

<table>
<thead>
<tr>
<th>Shape</th>
<th>Formula</th>
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<tbody>
<tr>
<td>Triangle</td>
<td>[ A = \frac{1}{2}bh ]</td>
</tr>
<tr>
<td>Parallelogram</td>
<td>[ A = bh ]</td>
</tr>
<tr>
<td>Circle</td>
<td>[ A = \pi r^2 ]</td>
</tr>
<tr>
<td>Circle</td>
<td>[ C = \pi d \text{ or } C = 2\pi r ]</td>
</tr>
<tr>
<td>General Prisms</td>
<td>[ V = Bh ]</td>
</tr>
<tr>
<td>Cylinder</td>
<td>[ V = \pi r^2 h ]</td>
</tr>
<tr>
<td>Sphere</td>
<td>[ V = \frac{4}{3} \pi r^3 ]</td>
</tr>
<tr>
<td>Cone</td>
<td>[ V = \frac{1}{3} \pi r^2 h ]</td>
</tr>
<tr>
<td>Pyramid</td>
<td>[ V = \frac{1}{3} Bh ]</td>
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<table>
<thead>
<tr>
<th>Theorem/Formula</th>
<th>Equation</th>
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<tbody>
<tr>
<td><strong>Pythagorean Theorem</strong></td>
<td>[ a^2 + b^2 = c^2 ]</td>
</tr>
<tr>
<td><strong>Quadratic Formula</strong></td>
<td>[ x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} ]</td>
</tr>
<tr>
<td><strong>Arithmetic Sequence</strong></td>
<td>[ a_n = a_1 + (n - 1)d ]</td>
</tr>
<tr>
<td><strong>Geometric Sequence</strong></td>
<td>[ a_n = a_1 r^n - 1 ]</td>
</tr>
<tr>
<td><strong>Geometric Series</strong></td>
<td>[ S_n = \frac{a_1 - a_1 r^n}{1 - r} ]</td>
</tr>
<tr>
<td><strong>Radians</strong></td>
<td>1 radian = [\frac{180}{\pi}] degrees</td>
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<tr>
<td><strong>Degrees</strong></td>
<td>1 degree = [\frac{\pi}{180}] radians</td>
</tr>
<tr>
<td><strong>Exponential Growth/Decay</strong></td>
<td>[ A = A_0 e^{k(t - t_0)} + B_0 ]</td>
</tr>
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### Regents Examination in Algebra II – June 2019

**Scoring Key: Part I (Multiple-Choice Questions)**

<table>
<thead>
<tr>
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<th>Date</th>
<th>Question Number</th>
<th>Scoring Key</th>
<th>Question Type</th>
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**Regents Examination in Algebra II – June 2019
Scoring Key: Parts II, III, and IV ( Constructed-Response Questions)**

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**Key**

- **MC** = Multiple-choice question
- **CR** = Constructed-response question

The chart for determining students' final examination scores for the June 2019 Regents Examination in Algebra II will be posted on the Department's web site at: [http://www.p12.nysed.gov/assessment/](http://www.p12.nysed.gov/assessment/) on the day of the examination. Conversion charts provided for the previous administrations of the Regents Examination in Algebra II must NOT be used to determine students' final scores for this administration.
FOR TEACHERS ONLY

The University of the State of New York
REGENTS HIGH SCHOOL EXAMINATION

ALGEBRA II

Friday, June 21, 2019 — 1:15 p.m. to 4:15 p.m., only

RATING GUIDE

Updated information regarding the rating of this examination may be posted on the New York State Education Department’s web site during the rating period. Check this web site at: http://www.p12.nysed.gov/assessment/ and select the link “Scoring Information” for any recently posted information regarding this examination. This site should be checked before the rating process for this examination begins and several times throughout the Regents Examination period.

The Department is providing supplemental scoring guidance, the “Model Response Set,” for the Regents Examination in Algebra II. This guidance is intended to be part of the scorer training. Schools are encouraged to incorporate the Model Response Sets into the scorer training or to use them as additional information during scoring. While not reflective of all scenarios, the model responses selected for the Model Response Set illustrate how less common student responses to constructed-response questions may be scored. The Model Response Set will be available on the Department’s web site at http://www.nysedregents.org/algebratwo/.
Mechanics of Rating

The following procedures are to be followed for scoring student answer papers for the Regents Examination in Algebra II. More detailed information about scoring is provided in the publication Information Booklet for Scoring the Regents Examination in Algebra II.

Do not attempt to correct the student’s work by making insertions or changes of any kind. In scoring the constructed-response questions, use check marks to indicate student errors. Unless otherwise specified, mathematically correct variations in the answers will be allowed. Units need not be given when the wording of the questions allows such omissions.

Each student’s answer paper is to be scored by a minimum of three mathematics teachers. No one teacher is to score more than approximately one-third of the constructed-response questions on a student’s paper. Teachers may not score their own students’ answer papers. On the student’s separate answer sheet, for each question, record the number of credits earned and the teacher’s assigned rater/scorer letter.

Schools are not permitted to rescore any of the constructed-response questions on this exam after each question has been rated once, regardless of the final exam score. Schools are required to ensure that the raw scores have been added correctly and that the resulting scale score has been determined accurately.

Raters should record the student’s scores for all questions and the total raw score on the student’s separate answer sheet. Then the student’s total raw score should be converted to a scale score by using the conversion chart that will be posted on the Department’s web site at: http://www.p12.nysed.gov/assessment/ by Friday, June 21, 2019. Because scale scores corresponding to raw scores in the conversion chart may change from one administration to another, it is crucial that, for each administration, the conversion chart provided for that administration be used to determine the student’s final score. The student’s scale score should be entered in the box provided on the student’s separate answer sheet. The scale score is the student’s final examination score.
I. General Principles for Rating

The rubrics for the constructed-response questions on the Regents Examination in Algebra II are designed to provide a systematic, consistent method for awarding credit. The rubrics are not to be considered all-inclusive; it is impossible to anticipate all the different methods that students might use to solve a given problem. Each response must be rated carefully using the teacher’s professional judgment and knowledge of mathematics; all calculations must be checked. The specific rubrics for each question must be applied consistently to all responses. In cases that are not specifically addressed in the rubrics, raters must follow the general rating guidelines in the publication Information Booklet for Scoring the Regents Examination in Algebra II, use their own professional judgment, confer with other mathematics teachers, and/or contact the State Education Department for guidance. During each Regents Examination administration period, rating questions may be referred directly to the Education Department. The contact numbers are sent to all schools before each administration period.

II. Full-Credit Responses

A full-credit response provides a complete and correct answer to all parts of the question. Sufficient work is shown to enable the rater to determine how the student arrived at the correct answer.

When the rubric for the full-credit response includes one or more examples of an acceptable method for solving the question (usually introduced by the phrase “such as”), it does not mean that there are no additional acceptable methods of arriving at the correct answer. Unless otherwise specified, mathematically correct alternative solutions should be awarded credit. The only exceptions are those questions that specify the type of solution that must be used; e.g., an algebraic solution or a graphic solution. A correct solution using a method other than the one specified is awarded half the credit of a correct solution using the specified method.

III. Appropriate Work

Full-Credit Responses: The directions in the examination booklet for all the constructed-response questions state: “Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc.” The student has the responsibility of providing the correct answer and showing how that answer was obtained. The student must “construct” the response; the teacher should not have to search through a group of seemingly random calculations scribbled on the student paper to ascertain what method the student may have used.

Responses With Errors: Rubrics that state “Appropriate work is shown, but…” are intended to be used with solutions that show an essentially complete response to the question but contain certain types of errors, whether computational, rounding, graphing, or conceptual. If the response is incomplete; i.e., an equation is written but not solved or an equation is solved but not all of the parts of the question are answered, appropriate work has not been shown. Other rubrics address incomplete responses.

IV. Multiple Errors

Computational Errors, Graphing Errors, and Rounding Errors: Each of these types of errors results in a 1-credit deduction. Any combination of two of these types of errors results in a 2-credit deduction. No more than 2 credits should be deducted for such mechanical errors in a 4-credit question and no more than 3 credits should be deducted in a 6-credit question. The teacher must carefully review the student’s work to determine what errors were made and what type of errors they were.

Conceptual Errors: A conceptual error involves a more serious lack of knowledge or procedure. Examples of conceptual errors include using the incorrect formula for the area of a figure, choosing the incorrect trigonometric function, or multiplying the exponents instead of adding them when multiplying terms with exponents.

If a response shows repeated occurrences of the same conceptual error, the student should not be penalized twice. If the same conceptual error is repeated in responses to other questions, credit should be deducted in each response.

For 4- and 6-credit questions, if a response shows one conceptual error and one computational, graphing, or rounding error, the teacher must award credit that takes into account both errors. Refer to the rubric for specific scoring guidelines.
Part II

For each question, use the specific criteria to award a maximum of 2 credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

(25)  
[2] 1.5, and a correct interpretation is written.

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] 1.5, but the interpretation is incomplete, incorrect, or missing.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(26)  
[2] \{-2,7\}, and correct algebraic work is shown.

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] A correct quadratic equation in standard form is written, but no further correct work is shown.

or

[1] \{-2,7\}, but a method other than algebraic is used.

or

[1] \{-2,7\}, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(27)  

[1] One graphing error is made.

or

[1] One conceptual error is made.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
(28) [2] $-\frac{24}{25}$ or equivalent, and correct work is shown.

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] $-\frac{24}{25}$, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(29) [2] A correct justification indicating a negative response is given.

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or


[0] No, but no justification is given.

or

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(30) [2] $x^3 - x^2 + 7x - 2$ is stated and correct work is shown.

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] $x^3 - x^2 + 7x - 2$, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
(31) \[ a_1 = 6 \]
\[ a_n = \frac{3}{2} a_{n-1} \text{ or equivalent is written.} \]

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] \[ a_1 = 6 \text{ or } a_n = \frac{3}{2} a_{n-1} \] is written, but no further correct work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(32) \[ 2 \] No or not unfair, and a correct explanation is written.

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] No or not unfair, but the explanation is incomplete.

[0] No or not unfair, but the explanation is missing or incorrect.

or

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
Part III

For each question, use the specific criteria to award a maximum of 4 credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

\[(33) \quad [4] \quad (4x^2 + 9)(2x + 3)(2x - 3) \text{ and correct work is shown, and a correct explanation indicating a negative response is written.} \]

[3] Appropriate work is shown, but one computational, factoring, or simplification error is made.

or

[3] Appropriate work is shown, but the explanation is incomplete.

[2] Appropriate work is shown, but two or more computational, factoring, or simplification errors are made.

or

[2] Appropriate work is shown, but one conceptual error is made.

or

[2] Appropriate work is shown to find \((4x^2 + 9)(2x + 3)(2x - 3)\), but no further correct work is shown.

or

[2] A correct explanation indicating a negative response is written, but no further correct work is shown.

[1] Appropriate work is shown, but one conceptual error and one computational, factoring, or simplification error are made.

or

[1] \((4x^2 + 9)(4x^2 - 9)\), but no further correct work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
(34) \[ s(t) = 200 \left( \frac{1}{2} \right)^{\frac{t}{\sqrt{15}}} \text{ or equivalent, 50 and correct algebraic work is shown.} \]

[3] Appropriate work is shown, but one computational, notation, or rounding error is made.

or

[3] \[ s(t) = 200 \left( \frac{1}{2} \right)^{\frac{t}{\sqrt{15}}} \text{ and 50, but a method other than algebraic is used.} \]

[2] Appropriate work is shown, but two or more computational, notation, or rounding errors are made.

or

[2] Appropriate work is shown, but one conceptual error is made.

or

[2] \[ s(t) = 200 \left( \frac{1}{2} \right)^{\frac{t}{\sqrt{15}}} \text{ is written, but no further correct work is shown.} \]

or

[2] Appropriate work is shown to find 50, but no further correct work is shown.

[1] Appropriate work is shown, but one conceptual error and one computational, notation, or rounding error are made.

or

[1] 50, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
(35) \[ y + 3 = \frac{1}{8}(x - 4)^2, \] or an equivalent equation, and correct work is shown.

[3] Appropriate work is shown, but one computational or graphing error is made.

[2] Appropriate work is shown, but two or more computational or graphing errors are made.

or

[2] Appropriate work is shown, but one conceptual error is made.

[1] Appropriate work is shown, but one conceptual error and one computational or graphing error are made.

or

[1] \[ y + 3 = \frac{1}{8}(x - 4)^2, \] but no work is shown.

or

[1] The vertex, \((4, -3)\), was correctly determined, but no further correct work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
(36)  [4] $\frac{12}{27}$ or equivalent and correct work is shown, not independent and a correct justification is given.

[3] Appropriate work is shown, but one computational or simplification error is made.

[2] Appropriate work is shown, but two or more computational or simplification errors are made.

or

[2] Appropriate work is shown, but one conceptual error is made.

or

[2] Appropriate work is shown to find $\frac{12}{27}$, but no further correct work is shown.

or

[2] Not independent and a correct justification is given, but no further correct work is shown.

[1] Appropriate work is shown, but one conceptual error and one computational or simplification error are made.

or

[1] $\frac{12}{27}$, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
Part IV

For each question, use the specific criteria to award a maximum of 6 credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

(37) [6] 2.5, a correct interpretation is written, a correct graph is drawn, and a correct justification indicating a negative response is given.

[5] Appropriate work is shown, but one computational, graphing, or rounding error is made.

or

[5] 2.5, a correct interpretation is written, and a correct graph is drawn, but an incomplete justification is written.

[4] Appropriate work is shown, but two computational, graphing, or rounding errors are made.

or

[4] Appropriate work is shown, but one conceptual error is made.

[3] Appropriate work is shown, but three or more computational or graphing errors are made.

or

[3] Appropriate work is shown, but one conceptual error and one computational or graphing error are made.

[2] Appropriate work is shown, but two conceptual errors are made.

or

[2] Appropriate work is shown, but one conceptual error and two or more computational or graphing errors are made.

or

[2] 2.5 and a correct interpretation is written, but no further correct work is shown.

or

[2] A correct graph is drawn, but no further correct work is shown.

or

[2] A correct justification indicating a negative response is given, but no further correct work is shown.
[1] 2.5 or a correct interpretation is written, but no further correct work is shown.  
   
   or  
   
[1] Appropriate work is shown, but two conceptual errors and one computational  
   or graphing error are made.  
   
[0] No, but no further correct work is shown.  
   
   or  
   
[0] A zero response is completely incorrect, irrelevant, or incoherent or is a  
   correct response that was obtained by an obviously incorrect procedure.
# Map to the Learning Standards

## Algebra II

### June 2019

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<td>Constructed Response</td>
<td>2</td>
<td>A-APR.D</td>
</tr>
<tr>
<td>31</td>
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<td>2</td>
<td>F-BF.A</td>
</tr>
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<td>S-IC.A</td>
</tr>
<tr>
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<td>4</td>
<td>A-SSE.A</td>
</tr>
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<td>G-GPE.A</td>
</tr>
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<td>4</td>
<td>S-CP.A</td>
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<tr>
<td>37</td>
<td>Constructed Response</td>
<td>6</td>
<td>F-IF.B</td>
</tr>
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The Chart for Determining the Final Examination Score for the June 2019 Regents Examination in Algebra II will be posted on the Department’s web site at: http://www.p12.nysed.gov/assessment/ by Friday, June 21, 2019. Conversion charts provided for previous administrations of the Regents Examination in Algebra II must NOT be used to determine students’ final scores for this administration.

Online Submission of Teacher Evaluations of the Test to the Department

Suggestions and feedback from teachers provide an important contribution to the test development process. The Department provides an online evaluation form for State assessments. It contains spaces for teachers to respond to several specific questions and to make suggestions. Instructions for completing the evaluation form are as follows:


2. Select the test title.

3. Complete the required demographic fields.

4. Complete each evaluation question and provide comments in the space provided.

5. Click the SUBMIT button at the bottom of the page to submit the completed form.
25 The table below shows the number of hours of daylight on the first day of each month in Rochester, NY.

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Given the data, what is the average rate of change in hours of daylight per month from January 1st to April 1st?

Interpret what this means in the context of the problem.

It means that over the course from January to April, the average rate of change of the number of hours of daylight is 1.5.

Score 2: The student gave a complete and correct response.
25 The table below shows the number of hours of daylight on the first day of each month in Rochester, NY.

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Given the data, what is the average rate of change in hours of daylight per month from January 1st to April 1st?

\[
\frac{\Delta y}{\Delta x} = \frac{13.9 - 9.4}{4 - 1} = 1.5
\]

Interpret what this means in the context of the problem.

On average, the number of hours of daylight increased 1.5 hours per month from January - April.

Score 2: The student gave a complete and correct response.
The table below shows the number of hours of daylight on the first day of each month in Rochester, NY.

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Given the data, what is the average rate of change in hours of daylight per month from January 1st to April 1st?

\[
\frac{13.9 - 9.4}{4 - 1} = \frac{4.5}{3} = 1.5
\]

Interpret what this means in the context of the problem.

On average, the temperature increased by 1.5 degrees every month.

Score 1: The student gave an incorrect interpretation.
25 The table below shows the number of hours of daylight on the first day of each month in Rochester, NY.

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Given the data, what is the average rate of change in hours of daylight per month from January 1st to April 1st?

\[
\frac{\Delta y}{\Delta x} = \frac{4.5}{3} = 1.5 \text{ hrs/month}
\]

Interpret what this means in the context of the problem.

Every month from January to April, there are 1.5 more hours of daylight.

Score 1: The student gave an incomplete interpretation.
25 The table below shows the number of hours of daylight on the first day of each month in Rochester, NY.

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Given the data, what is the average rate of change in hours of daylight per month from January 1st to April 1st?

\[
\text{Jan} \to \text{Apr.} \quad \frac{9.4 - 13.9}{4.5}
\]

Interpret what this means in the context of the problem.

\[
\text{A means from January to April, the number of daylight hours increases by 4.5.}
\]

**Score 0:** The student found an incorrect average rate of change and wrote an incomplete interpretation.
Algebraically solve for \( x \):

\[
\frac{7}{2x} - \frac{2}{x+1} = \frac{1}{4}
\]

\[
\frac{[7][x+1]}{(2x)[x+1]} - \frac{4x}{(2x)(x+1)} = \frac{1}{4}
\]

\[
\frac{3x + 7 - 4x}{(2x)(x+1)} = \frac{1}{4}
\]

\[
\frac{3x + 7 - 4x}{(2x)(x+1)} = \frac{1}{4}
\]

\[
(2x)(x+1) = (4)(3x+7)
\]

\[
2x^2 + 2x = 12x + 28
\]

\[
-12x - 12x
\]

\[
2x^2 - 10x = 28
\]

\[
-28
\]

\[
2x^2 - 10x - 28 = 0
\]

\[
2(x^2 - 5x - 14) = 0
\]

\[
2(x + 2)(x - 7) = 0
\]

\[
\text{Score 2: The student gave a complete and correct response.}
\]
26 Algebraically solve for $x$:

\[
\frac{28(x+1)}{x+4} - \frac{2}{x+4} = \frac{2x(x+1)}{x+4}
\]

\[
\text{LCD: } 2x(x+1) + 4
\]

\[
28x + 28 - 10x = 2x^2 + 2x
\]

\[
12x + 28 = 2x^2 + 2x
\]

\[
0 = 2x^2 - 12x + 2x - 28
\]

\[
0 = 2x^2 - 10x - 28
\]

\[
(2x+4)(x-7) = 0
\]

\[
2x + 4 = 0 \quad \mid \quad x - 7 = 0
\]

\[
x = -2
\]

\[
x = 7
\]

Score 2: The student gave a complete and correct response.
26 Algebraically solve for $x$:

\[
\frac{7}{2x} - \frac{2}{x + 1} = \frac{1}{4}
\]

\[
\frac{7}{-y} = \frac{2}{-1} = \frac{1}{4}
\]

\[
\frac{7 - \frac{2}{x + 1}}{2x + 1} = \frac{1}{4}
\]

\[
\frac{7x + 7}{2x^2 + 2x} - \frac{4x}{2x^2 + 2x} = \frac{1}{4}
\]

\[
\frac{3x + 7}{2x^2 + 2x} \times \frac{1}{4} = \frac{-56}{-14 + 14}
\]

\[
x = \frac{1}{7}
\]

\[
-2 \text{ is extraneous root}
\]

**Score 1:** The student incorrectly identified $-2$ as an extraneous root.
26 Algebraically solve for $x$:

\[
\frac{7}{2x} \cdot \frac{2}{x+1} = \frac{1}{4}
\]

\[
\frac{7x+7-4x}{2x(x+1)} = \frac{1}{4}
\]

\[
2x(x+1) = 28x + 28 - 16x
\]

\[
2x^2 + 2x = 12x + 28
\]

\[
-10x - 28 = 0
\]

\[
2(x^2 - 5x - 14) = 0
\]

\[
2(x+2)(x-7) = 0
\]

\[
x = 7
\]

\[
x = -2
\]

\[
\text{undefined}
\]

**Score 1:** The student made a computational error by not distributing the 2 correctly.
26 Algebraically solve for $x$:

\[
\frac{7}{2x} - \frac{2}{x + 1} = \frac{1}{4}
\]

\[
\begin{align*}
7x + 7 &= 4x \\
3x &= 7 \\
\therefore x &= \frac{7}{3} = \frac{9}{4}
\end{align*}
\]

Score 0: The student made a conceptual error and a computational error.
27 Graph $f(x) = \log_2(x + 6)$ on the set of axes below.

Score 2: The student gave a complete and correct response.
27 Graph $f(x) = \log_2(x + 6)$ on the set of axes below.

Score 2: The student gave a complete and correct response.
27 Graph $f(x) = \log_2(x + 6)$ on the set of axes below.

Score 1: The student made an error graphing the end behavior as $x \to -6$. 
Question 27

27 Graph $f(x) = \log_2(x + 6)$ on the set of axes below.

Score 0: The student made multiple graphing errors.
28 Given \( \tan \theta = \frac{7}{24} \), and \( \theta \) terminates in Quadrant III, determine the value of \( \cos \theta \).

Score 2: The student gave a complete and correct response.
28 Given \( \tan \theta = \frac{7}{24} \), and \( \theta \) terminates in Quadrant III, determine the value of \( \cos \theta \).

\[ \begin{align*}
7^2 + 24^2 &= x^2 \\
49 + 576 &= x^2 \\
\sqrt{625} &= x
\end{align*} \]

\( x = 25 \)

Score 2: The student gave a complete and correct response.
Question 28

28 Given $\tan \theta = \frac{7}{24}$, and $\theta$ terminates in Quadrant III, determine the value of $\cos \theta$.

\[ \cos Q = \frac{A}{H} = \frac{24}{25} \]

\[ a^2 + b^2 = c^2 \]
\[ 7^2 + 24^2 = x^2 \]
\[ 49 + 576 = x^2 \]
\[ \sqrt{625} = 25 \]
\[ x = 25 \]

Score 1: The student did not consider the quadrant.
Question 28

28 Given $\tan \theta = \frac{7}{24}$, and $\theta$ terminates in Quadrant III, determine the value of $\cos \theta$.

\[
\tan \theta = \frac{7}{24} \quad \cos \theta = \frac{\sqrt{a^2 + b^2}}{a}
\]

\[
7^2 + b^2 = a^2
\]

\[
a^2 = 144
\]

\[
-49 = -49
\]

\[
b^2 = 527
\]

\[
b = 23
\]

Score 0: The student did not show enough correct work to receive any credit.
29 Kenzie believes that for $x \geq 0$, the expression $\left( \sqrt[2]{x^2} \right) \left( \sqrt[3]{x^3} \right)$ is equivalent to $\sqrt[6]{x^6}$. Is she correct? Justify your response algebraically.

\[
\left( x^{\frac{2}{7}} \right) \left( x^{\frac{3}{5}} \right) = x^{\frac{31}{35}} = \sqrt[35]{x^{31}}
\]

She is not correct because when you convert the expression into radical form and multiply, add the exponents, the answer should be $\sqrt[35]{x^{31}}$.

Score 2: The student gave a complete and correct response.
29 Kenzie believes that for $x \geq 0$, the expression $\left(\sqrt[2]{x^2}\right)\left(\sqrt[3]{x^3}\right)$ is equivalent to $x^{35/35}$. Is she correct? Justify your response algebraically.

Score 2: The student gave a complete and correct response. It is indicated that Kenzie is incorrect.
Question 29

29 Kenzie believes that for $x \geq 0$, the expression $\left( \sqrt[2]{x^2} \right) \left( \sqrt[3]{x^3} \right)$ is equivalent to $\sqrt[6]{x^6}$. Is she correct? Justify your response algebraically.

$$\left( \sqrt[2]{x^2} \right) \left( \sqrt[3]{x^3} \right) = \left( x \right)^{\frac{6}{35}}$$

Score 1: The student applied exponent properties incorrectly.
29 Kenzie believes that for $x \geq 0$, the expression $\left( \sqrt[2]{x} \right) \left( \sqrt[3]{x} \right)$ is equivalent to $\sqrt[6]{x^5}$. Is she correct? Justify your response algebraically.

\[
\left( \sqrt[2]{x} \right) \left( \sqrt[3]{x} \right) = 1.84767919
\]

\[
\sqrt[6]{x^5} = 1.126178081
\]

No, when plugging in a tester they are not the same

Score 1: The student used a method other than algebraic by showing a contradiction.
29 Kenzie believes that for \( x \geq 0 \), the expression \( \left( \sqrt[7]{x^2} \right) \left( \sqrt[5]{x^3} \right) \) is equivalent to \( \sqrt[35]{x^6} \). Is she correct? Justify your response algebraically.

\[
\sqrt[7]{x^2} = (x^2)^{\frac{2}{7}} \\
\sqrt[5]{x^3} = (x^3)^{\frac{2}{5}} \\
(x^2)^{\frac{2}{7}} \cdot (x^3)^{\frac{2}{5}} = x^{\frac{2}{7} \cdot 2} \cdot x^{\frac{2}{5} \cdot 3} = x^{\frac{4}{7}} \cdot x^{\frac{6}{5}} = x^{\frac{4}{7} + \frac{6}{5}} = x^{\frac{20 + 42}{35}} = x^{\frac{62}{35}}
\]

\[
= \left( \sqrt[35]{x^6} \right)^{\frac{35}{62}}
\]

\textbf{Score 0:} The student made multiple errors.
30 When the function \( p(x) \) is divided by \( x - 1 \) the quotient is \( x^2 + 7 + \frac{5}{x - 1} \). State \( p(x) \) in standard form.

\[
\frac{p(x)}{x-1} = x^2 + 7 + \frac{5}{x - 1}
\]

\[
x^2(x-1) + 7(x-1) + \left(\frac{5}{x-1}\right)(x-1)
\]

\[
x^3 - x^2 + 7x - 7 + 5
\]

\[
= x^3 - x^2 + 7x - 2
\]

**Score 2:** The student gave a complete and correct response.
30 When the function $p(x)$ is divided by $x - 1$ the quotient is $x^2 + 7 + \frac{5}{x - 1}$. State $p(x)$ in standard form.

**Score 2:** The student gave a complete and correct response.
Question 30

30 When the function \( p(x) \) is divided by \( x - 1 \) the quotient is \( x^2 + 7 + \frac{5}{x - 1} \). State \( p(x) \) in standard form.

\[
\frac{p(x)}{x - 1} = x^2 + 7 + \frac{5}{x - 1}
\]

\[
(x - 1) \left( x^2 + 7 \right) + \frac{5}{x - 1}
\]

\[
x^3 - x^2 + 7x - 7 + 5
\]

\[
\frac{x^3 - x^2 + 7x - 2}{x - 1}
\]

\[
p(x) = x^3 - x^2 + 7x - 2
\]

Score 2: The student gave a complete and correct response.
Question 30

30 When the function \( p(x) \) is divided by \( x - 1 \) the quotient is \( x^2 + 7 + \frac{5}{x - 1} \). State \( p(x) \) in standard form.

\[ \begin{align*}
&x^3 - x^2 + 7x - 7 + 5x - 5 \\
&x^3 - x^2 + 12x - 12
\end{align*} \]

Score 1:  The student incorrectly distributed the \( x - 1 \) to the rational term.
30 When the function \( p(x) \) is divided by \( x - 1 \) the quotient is \( x^2 + 7 + \frac{5}{x - 1} \). State \( p(x) \) in standard form.

\[
\begin{align*}
x - 1 (x^2) &= \boxed{x^3 - x^2} \quad \frac{x^2}{7} \\
x - 1 (7) &= \boxed{7x - 7}
\end{align*}
\]

\[
\begin{align*}
x - 1 \sqrt{x^3 - x^2 + 7x - 7} &= \boxed{x^2 + 7} \\
- x^3 + x^2 &= \boxed{-x - 7}
\end{align*}
\]

**Score 1:** The student excluded the remainder.
30 When the function $p(x)$ is divided by $x - 1$ the quotient is $x^2 + 7 + \frac{5}{x - 1}$. State $p(x)$ in standard form.

Score 0: The student made an error distributing the $x^2$ and did not state $p(x)$ in standard form.
31 Write a recursive formula for the sequence 6, 9, 13.5, 20.25, . . .

\[ a_1 = 6 \]

\[ a_n = a_{n-1} \cdot 1.5 \]

Check:
\[ a_2 = a_1 \cdot 1.5 \]
\[ a_2 = a_1 \cdot 1.5 \]
\[ a_2 = 6 \cdot 1.5 \]
\[ a_2 = 9 \]

\[ \sqrt{\quad} \]

Score 2: The student gave a complete and correct response.
31 Write a recursive formula for the sequence 6, 9, 13.5, 20.25, . . .

\[
\begin{align*}
A_1 &= 6 \\
A_n &= A_{n-1} \cdot r \\
A_n &= A_{n-1} \cdot \frac{3}{2} \\
A_1 &= 6
\end{align*}
\]

Score 2: The student gave a complete and correct response.
31 Write a recursive formula for the sequence 6, 9, 13.5, 20.25, . . .

\[
\begin{align*}
a_1 &= 6 \\
\,a_n &= a_1 \left(\frac{3}{2}\right)^{n-1}
\end{align*}
\]

**Score 1:** The student received credit for writing \(a_1 = 6\).
31 Write a recursive formula for the sequence 6, 9, 13.5, 20.25, \ldots

\[ a_n = 1.5(a_{n-1}) \]

**Score 1:** The student did not write the initial term.
31 Write a recursive formula for the sequence $6, 9, 13.5, 20.25, \ldots$.

\[
\begin{align*}
\alpha_n & = 60 \\
\alpha_{n-1} & = 9, 1.5
\end{align*}
\]

\[
6, 9, 13.5, 20.25
\]

\[
\begin{array}{cccc}
1.5 & 1.5 & 1.5 & \ldots
\end{array}
\]

**Score 0:** The student did not show enough correct work to receive any credit.
Robin flips a coin 100 times. It lands heads up 43 times, and she wonders if the coin is unfair. She runs a computer simulation of 750 samples of 100 fair coin flips. The output of the proportion of heads is shown below.

Do the results of the simulation provide strong evidence that Robin’s coin is unfair? Explain your answer.

\[
\text{Robin's coin} = \frac{43}{100} = 0.43
\]

\[
0.499 \pm 2(0.049) \rightarrow (0.401, 0.597)
\]

Since 0.43 is within the interval of (0.401, 0.597) her coin is likely not unfair.

**Score 2:** The student gave a complete and correct response.
32 Robin flips a coin 100 times. It lands heads up 43 times, and she wonders if the coin is unfair. She runs a computer simulation of 750 samples of 100 fair coin flips. The output of the proportion of heads is shown below.

Do the results of the simulation provide strong evidence that Robin’s coin is unfair? Explain your answer.

\[ \frac{43}{100} = 0.43 \]

No because 0.43 falls inside the 95% 2 standard deviation.
Robin flips a coin 100 times. It lands heads up 43 times, and she wonders if the coin is unfair. She runs a computer simulation of 750 samples of 100 fair coin flips. The output of the proportion of heads is shown below.

Do the results of the simulation provide strong evidence that Robin’s coin is unfair? Explain your answer.

Score 1: The student gave a correct explanation based on an inappropriate interval.
32 Robin flips a coin 100 times. It lands heads up 43 times, and she wonders if the coin is unfair. She runs a computer simulation of 750 samples of 100 fair coin flips. The output of the proportion of heads is shown below.

Do the results of the simulation provide strong evidence that Robin’s coin is unfair? Explain your answer.

Score 1: The student gave an explanation, but provided no statistical evidence.
32 Robin flips a coin 100 times. It lands heads up 43 times, and she wonders if the coin is unfair. She runs a computer simulation of 750 samples of 100 fair coin flips. The output of the proportion of heads is shown below.

Do the results of the simulation provide strong evidence that Robin’s coin is unfair? Explain your answer.

Yes, her coin is more than 1 standard deviation away. Although it isn’t more than 1.5 deviations, it is still much less than the mean.

Score 0: The student did not show enough correct statistical evidence to receive any credit.
Question 33

33 Factor completely over the set of integers: $16x^4 - 81$

$$16x^4 - 81 = (4x^2 + 9)(4x^2 - 9) = (4x^2 + 9)(2x + 3)(2x - 3)$$

Sara graphed the polynomial $y = 16x^4 - 81$ and stated “All the roots of $y = 16x^4 - 81$ are real.” Is Sara correct? Explain your reasoning.

$$a = 16, b = 0, c = -81$$

$$4x^2 + 9 = 0, 2x + 3 = 0, 2x - 3 = 0$$

NO, when you make mini equations, $4x^2 + 9 = 0$ can be solved for $x$, but your answer is an imaginary number, meaning not all roots of $y = 16x^4 - 81 = 0$ are real.

Score 4: The student gave a complete and correct response.
Sara graphed the polynomial $y = 16x^4 - 81$ and stated “All the roots of $y = 16x^4 - 81$ are real.” Is Sara correct? Explain your reasoning.

<table>
<thead>
<tr>
<th>$2x - 3 = 0$</th>
<th>$2x + 3 = 0$</th>
<th>$4x^2 + 9 = 0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$2x = 3$</td>
<td>$2x = -3$</td>
<td>$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$</td>
</tr>
<tr>
<td>$x = \frac{3}{2}$</td>
<td>$x = -\frac{3}{2}$</td>
<td>$b^2 - 4ac = 0^2 - 4(1)(9) = -36$</td>
</tr>
</tbody>
</table>

Sara is incorrect. Although 2 of the roots are real, we know at least one root is nonreal because, when using the quadratic formula to determine the roots for the factor $4x^2 + 9$, the discriminant is negative.

**Score 4:** The student gave a complete and correct response.
Question 33

33 Factor completely over the set of integers: $16x^4 - 81$

$$
(4x^2 - 9)(4x^2 + 9) \\
(2x-3)(2x+3)(4x^2 + 9)
$$

Sara graphed the polynomial $y = 16x^4 - 81$ and stated “All the roots of $y = 16x^4 - 81$ are real.” Is Sara correct? Explain your reasoning.

No because the graph only crosses the x-axis two times meaning only 2 real roots not 4.

Score 4: The student gave a complete and correct response.
33 Factor completely over the set of integers: $16x^4 - 81$

$$
\begin{align*}
16x^4 - 81 &= (4x^2 - 9)(4x^2 + 9) \\
&= (2x + 3)(2x - 3)(2x + 3)(2x - 3) \\
&= (2x + 3)^2(2x - 3)
\end{align*}
$$

Sara graphed the polynomial $y = 16x^4 - 81$ and stated “All the roots of $y = 16x^4 - 81$ are real.” Is Sara correct? Explain your reasoning.

No. Because it has 4 possible zeros, but only crosses the x-axis twice. (Graphing calculator)
Question 33

33 Factor completely over the set of integers: $16x^4 - 81$

\[
(4x^2 - 9)(4x^2 + 9)
\]

\[
4x^2 - 9 = 0
\]

\[
4x^2 = 9
\]

\[
x^2 = \frac{9}{4}
\]

\[
x = \pm \frac{3}{2}
\]

\[
4x^2 + 9 = 0
\]

\[
x^2 = -\frac{9}{4}
\]

\[
x = \pm \frac{3}{2}i
\]

Sara graphed the polynomial $y = 16x^4 - 81$ and stated “All the roots of $y = 16x^4 - 81$ are real.”

Is Sara correct? Explain your reasoning.

**Not all of the roots of $16x^4 - 81$ are real, because if it would be real it wouldn’t have an imaginary number.**

**Score 3:** The student did not factor completely.
Question 33

33 Factor completely over the set of integers: $16x^4 - 81$

\[
\frac{(4x^2 - 9)(4x^2 + 9)}{(2x + 3)(2x - 3)} (2x + 3i)(2x - 3i)
\]

Sara graphed the polynomial $y = 16x^4 - 81$ and stated “All the roots of $y = 16x^4 - 81$ are real.” Is Sara correct? Explain your reasoning.

Roots: $\frac{-3}{2}, \frac{3}{2}, \frac{3i}{2}, -\frac{3i}{2}$

No, b/c $\frac{3i}{2}$ and $-\frac{3i}{2}$ are imaginary #s

Score 3: The student did not factor over the set of integers.
33 Factor completely over the set of integers: $16x^4 - 81$

\[
\frac{(4x^2+9)(2x+3)(2x-3)}{(4x^2+9)(4x^2-9)}
\]

\[
\frac{16x^4 - 81}{2x+3} \quad 2x-3
\]

Sara graphed the polynomial $y = 16x^4 - 81$ and stated “All the roots of $y = 16x^4 - 81$ are real.” Is Sara correct? Explain your reasoning.

Sara is incorrect because if you plug into $y = \ldots$ and go to 2nd graph to the table and scroll up you can see there are some unreal roots.

<table>
<thead>
<tr>
<th>Value</th>
<th>$y$ Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>-17</td>
<td>1.34 e 6</td>
</tr>
<tr>
<td>-16</td>
<td>1.05 e 6</td>
</tr>
<tr>
<td>-15</td>
<td>809919</td>
</tr>
<tr>
<td>-14</td>
<td>614575</td>
</tr>
</tbody>
</table>
33 Factor completely over the set of integers: $16x^4 - 81$

$$16x^4 - 81 = (4x^2 - 9)(4x^2 + 9) = (2x - 3)(2x + 3)(4x^2 + 9)$$

Sara graphed the polynomial $y = 16x^4 - 81$ and stated “All the roots of $y = 16x^4 - 81$ are real.” Is Sara correct? Explain your reasoning.

$$\begin{align*}
(2x - 3)(2x + 3) &= 0 \\
2x - 3 &= 0 \quad 2x + 3 &= 0 \\
2x &= 3 \quad 2x &= -3 \\
x &= \frac{3}{2} \quad x &= \frac{-3}{2}
\end{align*}$$

No, because $1.5$ is a real number but $-1.5$ is not a real number because it is negative.

Score 1: The student made one factoring error and gave an incorrect explanation.
33 Factor completely over the set of integers: \(16x^4 - 81\)

\[
16x^4 - 81
\]

Sara graphed the polynomial \(y = 16x^4 - 81\) and stated “All the roots of \(y = 16x^4 - 81\) are real.” Is Sara correct? Explain your reasoning.

Sarah is incorrect because some of the roots are imaginary.

**Score 0:** The student’s explanation was not sufficient to receive any credit.
Question 34

34 The half-life of a radioactive substance is 15 years.

Write an equation that can be used to determine the amount, \( s(t) \), of 200 grams of this substance that remains after \( t \) years.

\[
s(t) = 200 \left( \frac{1}{2} \right)^{\frac{t}{15}}
\]

Determine algebraically, to the nearest year, how long it will take for \( \frac{1}{10} \) of this substance to remain.

\[
\frac{20}{200} = 200 \left( \frac{1}{2} \right)^{\frac{t}{15}}
\]

\[
\frac{1}{10} = \left( \frac{1}{2} \right)^{\frac{t}{15}}
\]

\[
\log \left( \frac{1}{10} \right) = \frac{t}{15} \log \left( \frac{1}{2} \right)
\]

\[
3.32193 = \frac{t}{15}
\]

\[
49.8289 = t
\]

50 years

Score 4: The student gave a complete and correct response.
34 The half-life of a radioactive substance is 15 years.

Write an equation that can be used to determine the amount, \( s(t) \), of 200 grams of this substance that remains after \( t \) years.

\[
s(t) = 200 \left( \frac{1}{2} \right)^{t/15}
\]

Determine algebraically, to the nearest year, how long it will take for \( \frac{1}{10} \) of this substance to remain.

\[
\frac{1}{10} = 200 \left( \frac{1}{2} \right)^{t/15}
\]

\[
\frac{1}{200} = \left( \frac{1}{2} \right)^{t/15}
\]

\[
\log(\frac{1}{200}) = \frac{t}{15} \log(\frac{1}{2})
\]

\[
t = 164 \text{ years}
\]

Score 3: The student made an error assuming that \( \frac{1}{10} \) of a gram of the substance remained.
The half-life of a radioactive substance is 15 years.

Write an equation that can be used to determine the amount, $s(t)$, of 200 grams of this substance that remains after $t$ years.

$$s(t) = 200 (0.5)^t$$

Determine algebraically, to the nearest year, how long it will take for $\frac{1}{10}$ of this substance to remain.

\[
\frac{20}{200} = \frac{200 (0.5)^t}{200} \\
0.1 = (0.5)^t \\
\log 0.1 = t \log 0.5 \\
\frac{1}{\log 0.5} \cdot \frac{1}{\log 0.5} \\
\frac{-1}{-1} = t \\
3.32 \cdot 15 = 49.82 \\
49.82 \rightarrow 50 \\
50 \text{ years}
\]

Score 3: The student made an error writing the equation for $s(t)$, assuming $t$ was the number of half-lives.
The half-life of a radioactive substance is 15 years.

Write an equation that can be used to determine the amount, \( s(t) \), of 200 grams of this substance that remains after \( t \) years.

\[
s(t) = 200 \left( \frac{1}{2} \right)^t
\]

Determine algebraically, to the nearest year, how long it will take for \( \frac{1}{10} \) of this substance to remain.

\[
\begin{align*}
\frac{1}{10} &= \frac{200 \left( \frac{1}{2} \right)^t}{200} \\
\log_{200} \frac{1}{200} &= \log_{200} \left( \frac{1}{2} \right)^t \\
\log_{200} \frac{1}{200} &= \frac{t \log_{200} \frac{1}{2}}{\log_{200} \frac{1}{2}} \\
t &= 10.96578428 \\
\therefore 11 \text{ years}
\end{align*}
\]

Score 2: The student wrote an incorrect equation and made an error assuming \( \frac{1}{10} \) of a gram of the substance remained.
34 The half-life of a radioactive substance is 15 years.

Write an equation that can be used to determine the amount, \( s(t) \), of 200 grams of this substance that remains after \( t \) years.

\[
\frac{200}{100} = 200(1-r)^{15} = 200(1-0.45) + 100(1-0.045) +
\]

Determine algebraically, to the nearest year, how long it will take for \( \frac{1}{10} \) of this substance to remain.

\[
15 = (1-0.45) \quad \frac{200}{200} = 200(1-0.045)^x, \\
1 = (1.955)^x \\
x = 50
\]

It will take 50 years to only have \( \frac{1}{10} \) of the substance to remain.

**Score 1:** The student received no credit for the first part and showed incomplete algebraic work on the second part.
Question 34

34 The half-life of a radioactive substance is 15 years.

Write an equation that can be used to determine the amount, \( s(t) \), of 200 grams of this substance that remains after \( t \) years.

\[
s(t) = 200 \left( \frac{1}{2} \right)^{15t}
\]

Determine algebraically, to the nearest year, how long it will take for \( \frac{1}{10} \) of this substance to remain.

\[
s(t) = 200 \left( \frac{1}{2} \right)^{15 \left( \frac{1}{10} \right)} \rightarrow 71 \text{ years}
\]

Score 1: The student received 1 credit for the equation.
34 The half-life of a radioactive substance is 15 years.

Write an equation that can be used to determine the amount, \( s(t) \), of 200 grams of this substance that remains after \( t \) years.

\[
S(t) = 200(1-0.15)^t
\]

Determine algebraically, to the nearest year, how long it will take for \( \frac{1}{10} \) of this substance to remain.

\[
\frac{20g}{200} = \frac{200(0.85)^t}{200}
\]

\[
0.1 = 0.85^t
\]

\[
\log_{0.85}0.1 = \log_{0.85}0.85
\]

\[
\therefore 13 \text{ years}
\]

**Score 0:** The student did not show enough correct work to receive any credit.
Determine an equation for the parabola with focus \((4, -1)\) and directrix \(y = -5\).

(Use of the grid below is optional.)

\[ y = \frac{1}{8} x^2 - x - 1 \]

**Score 4:** The student gave a complete and correct response.
35 Determine an equation for the parabola with focus $(4, -1)$ and directrix $y = -5$.
(Use of the grid below is optional.)

\[
y = \frac{1}{2(-1-(-5))} (x-4)^2 + \frac{-1+(-5)}{2} \\
= \frac{1}{8} (x-4)^2 - 3
\]

**Score 4:** The student gave a complete and correct response.
35 Determine an equation for the parabola with focus \((4, -1)\) and directrix \(y = -5\).
(Use of the grid below is optional.)

\[
\begin{align*}
\frac{1}{4p}x &= -5 + 1 = \frac{-6}{2} = 3 \\
y &= \frac{1}{4p} (x-4)^2 - 3 \\
y &= -\frac{1}{8} (x-4)^2 - 3
\end{align*}
\]

**Score 3:** The student used an incorrect value for \(p\).
35 Determine an equation for the parabola with focus \((4, -1)\) and directrix \(y = -5\).

(Use of the grid below is optional.)

\[ y = (x - 4)^2 - 3 \]

Score 2: The student correctly found the vertex and received 1 credit for the equation.
35 Determine an equation for the parabola with focus \((4, -1)\) and directrix \(y = -5\).
(Use of the grid below is optional.)

\[
\frac{1}{4}(x-h)+k = \frac{1}{8}(x-4) - 3
\]

\[
\text{vertex: } (4, -3)
\]

Score 2: The student correctly found the vertex and received 1 credit for the equation.
Question 35

35 Determine an equation for the parabola with focus $(4, -1)$ and directrix $y = -5$.
(Use of the grid below is optional.)

\[ f(x) = (x^2 - 4) - 3 \]

Score 1: The student correctly found the vertex, but made multiple errors writing the equation.
Question 35

Determine an equation for the parabola with focus \((4, -1)\) and directrix \(y = -5\).

(Use of the grid below is optional.)

\[
y = \frac{1}{8} (x - 4) - 5
\]

\[
\frac{1}{4p} = \frac{1}{8}, \quad p = 2
\]

Score 0: The student did not show enough correct work to receive any credit.
Juan and Filipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

<table>
<thead>
<tr>
<th></th>
<th>Juan Wins</th>
<th>Filipe Wins</th>
</tr>
</thead>
<tbody>
<tr>
<td>Short Practice Time</td>
<td>8</td>
<td>10</td>
</tr>
<tr>
<td>Long Practice Time</td>
<td>15</td>
<td>12</td>
</tr>
</tbody>
</table>

Given that the practice time was long, determine the exact probability that Filipe wins the next match.

\[
P(F|L) = \frac{12}{27}
\]

Determine whether or not the two events “Filipe wins” and “long practice time” are independent. Justify your answer.

\[
P(F|L) \neq P(F)
\]

\[
\frac{12}{27} \neq \frac{22}{45}
\]

\[.44 \neq .488
\]

Score 4: The student gave a complete and correct response.
Juan and Filipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

<table>
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<tr>
<th>Short Practice Time</th>
<th>Juan Wins</th>
<th>Filipe Wins</th>
</tr>
</thead>
<tbody>
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<td>10</td>
</tr>
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<td>Long Practice Time</td>
<td>15</td>
<td>12</td>
</tr>
<tr>
<td></td>
<td>23</td>
<td>22</td>
</tr>
<tr>
<td></td>
<td>45</td>
<td></td>
</tr>
</tbody>
</table>

Given that the practice time was long, determine the exact probability that Filipe wins the next match.

\[ P(F \mid L) = \frac{12}{27} \]

Determine whether or not the two events “Filipe wins” and “long practice time” are independent. Justify your answer.

\[ P(F \text{ and } L) = P(F) \cdot P(L) \]

\[ \frac{12}{45} = \frac{22}{45} \cdot \frac{22}{45} \]

\[ \neq 0.2667 \neq 0.2933 \]

No, the two events are not independent.

**Score 4:** The student gave a complete and correct response.
36 Juan and Filipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

<table>
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<th>Juan Wins</th>
<th>Filipe Wins</th>
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</tr>
<tr>
<td>Long Practice Time</td>
<td>15</td>
</tr>
<tr>
<td>23</td>
<td>22</td>
</tr>
<tr>
<td>45</td>
<td></td>
</tr>
</tbody>
</table>

Given that the practice time was long, determine the exact probability that Filipe wins the next match.

\[
P(F | S^c) = \frac{P(F \cap S^c)}{P(S^c)} = \frac{12/45}{27/45} = 0.160 \quad \text{(or 16%)}
\]

Determine whether or not the two events “Filipe wins” and “long practice time” are independent. Justify your answer.

\[
P(F \cap S^c) = P(F) \cdot P(S^c)
\]

\[
\frac{12}{45} = \left(\frac{22}{45}\right) \times \left(\frac{27}{45}\right)
\]

0.267 \neq 0.293

not independent

Score 3: The student made a computational error finding \( p(f | s^c) \).
36 Juan and Filipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

<table>
<thead>
<tr>
<th>Practice Time</th>
<th>Juan Wins</th>
<th>Filipe Wins</th>
</tr>
</thead>
<tbody>
<tr>
<td>Short</td>
<td>8</td>
<td>10</td>
</tr>
<tr>
<td>Long</td>
<td>15</td>
<td>12</td>
</tr>
</tbody>
</table>

Given that the practice time was long, determine the exact probability that Filipe wins the next match.

\[ P(F|L) = \frac{\frac{12}{27}}{\frac{22}{45}} = \frac{0.44}{0.48} = 0.44 \]

Determine whether or not the two events “Filipe wins” and “long practice time” are independent. Justify your answer.

\[ P(A) = P(A|B) \]
\[ P(F) \neq P(F|B) \]
\[ \frac{22}{45} = 0.44 \]
\[ 0.48 \neq 0.44 \]

not independent

Score 3: The student made an error rounding to 0.48.
Juan and Filipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

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<th>Juan Wins</th>
<th>Filipe Wins</th>
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<tbody>
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<td>10</td>
</tr>
<tr>
<td>Long Practice Time</td>
<td>15</td>
<td>12</td>
</tr>
</tbody>
</table>

Given that the practice time was long, determine the exact probability that Filipe wins the next match.

\[
\frac{12}{15+12} = \frac{12}{27}
\]

Determine whether or not the two events “Filipe wins” and “long practice time” are independent. Justify your answer.

The events of “Filipe wins” and “long practice” are dependent on one another because as “long practices” are done, the less times the event of “Filipe wins”.

Score 2: The student only received credit for the first part.
36 Juan and Filipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

<table>
<thead>
<tr>
<th>Practice Time</th>
<th>Juan Wins</th>
<th>Filipe Wins</th>
</tr>
</thead>
<tbody>
<tr>
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<td>10</td>
</tr>
<tr>
<td>Long</td>
<td>15</td>
<td>12</td>
</tr>
</tbody>
</table>

Given that the practice time was long, determine the exact probability that Filipe wins the next match.

\[
\frac{12}{27}
\]

Determine whether or not the two events “Filipe wins” and “long practice time” are independent. Justify your answer.

\[
\frac{2\cdot 8}{45} = \frac{16}{27}
\]

No because they are different %

**Score 1:** The student received one credit for \(\frac{12}{27}\).
Juan and Filipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

<table>
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<tr>
<th></th>
<th>Juan Wins</th>
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<tr>
<td>Long Practice Time</td>
<td>15</td>
<td>12</td>
</tr>
</tbody>
</table>

Given that the practice time was long, determine the exact probability that Filipe wins the next match.

\[
\text{Probability that Filipe wins the next match is } \frac{13}{28}
\]

Determine whether or not the two events “Filipe wins” and “long practice time” are independent. Justify your answer.

\[
\frac{12}{28} \approx 0.428571 \approx 44\%
\]

They're independent to each other because they don't have the same proportion, it's only a 44% between them.

Score 0: The student did not show enough correct work to receive any credit.
37 Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function $f(t) = -13\cos(0.8\pi t) + 13$, where $t$ represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of $f(t)$.

\[ \text{BP: } 2\pi \quad \theta = 0.8\pi \]
\[ (P) \cdot 8\pi = 2\pi \]
\[ \theta = 2.5 \]

Interpret what the period represents in this context.

The period of $f(t)$ represents the amount of time it would take the tire to spin one full rotation.

Score 6: The student gave a complete and correct response.
On the grid below, graph \textit{at least one} cycle of \( f(t) \) that includes the \( y \)-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

\[ \text{No because at its max height, the tire can only reach 26 feet, as proven through adding the absolute value of } a \quad (13) \quad \text{to } d \quad (\text{the midline}, 13). \]
Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function \( f(t) = -13\cos(0.8\pi t) + 13 \), where \( t \) represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of \( f(t) \).

\[
\text{period} = \frac{2\pi}{0.8\pi} = 2.5 \text{ seconds}
\]

Interpret what the period represents in this context.

\[\text{period is the time it takes for the nail to make one rotation}\]

Question 37 is continued on the next page.

Score 6: The student gave a complete and correct response.
On the grid below, graph at least one cycle of $f(t)$ that includes the $y$-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

No, the maximum of the sinusoidal curve is 26.
37 Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function \( f(t) = -13\cos(0.8\pi t) + 13 \), where \( t \) represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of \( f(t) \).

It takes 2.5 seconds for the nail to do a full rotation on the tire.

Interpret what the period represents in this context.

Score 5: The student made one graphing error.
On the grid below, graph at least one cycle of $f(t)$ that includes the $y$-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

No, it peaks at 28 inches.
37 Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function \( f(t) = -13\cos(0.8\pi t) + 13 \), where \( t \) represents the time (in seconds) since the nail first became caught in the tire. Determine the period of \( f(t) \).

\[
\begin{align*}
\text{Period} & = \frac{2\pi}{0.8} \\
\text{Period} & = 2.5 \\
\end{align*}
\]

Interpret what the period represents in this context.

Score 4: The student did not interpret the period and gave an incomplete justification in the last part.
On the grid below, graph at least one cycle of $f(t)$ that includes the $y$-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

No, it does not because the cosine graph's amplitude is 13 and the midline is 13.
37 Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function \( f(t) = -13\cos(0.8\pi t) + 13 \), where \( t \) represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of \( f(t) \).

\[
\frac{2\pi}{0.8\pi} = 2.5 \text{ seconds},
\]

Interpret what the period represents in this context.

It takes 2.5 seconds for the nail to go from high point back to high point.

Question 37 is continued on the next page.

Score 3: The student made a labeling error on the graph and did not answer the last part.
On the grid below, graph \textit{at least one} cycle of \( f(t) \) that includes the \( y \)-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.
37 Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function $f(t) = -13\cos(0.8\pi t) + 13$, where $t$ represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of $f(t)$.

The period is $0.8$ second, this represents how many times it takes for the nail to reach the original height it became stuck at.

Interpret what the period represents in this context.

Score 3: The student gave a correct interpretation based on an incorrect period and received full credit for the graph.
On the grid below, graph at least one cycle of \( f(t) \) that includes the \( y \)-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.
Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function \( f(t) = -13\cos(0.8\pi t) + 13 \), where \( t \) represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of \( f(t) \).

\[
\begin{align*}
\text{Period} (P) &= \frac{2\pi}{0.8\pi} \\
P &= \frac{2}{0.8} = 2.5
\end{align*}
\]

Interpret what the period represents in this context.

*It takes 2.5 seconds for the nail to complete 1 full rotation.*

Question 37 is continued on the next page.

**Score 2:** The student received credit for the period and the interpretation.
On the grid below, graph \( at \text{ least one } \) cycle of \( f(t) \) that includes the \( y \)-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.
Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function $f(t) = -13\cos(0.8\pi t) + 13$, where $t$ represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of $f(t)$.

Interpret what the period represents in this context.

**Score 2:** The student drew a correct graph.
On the grid below, graph *at least one* cycle of \( f(t) \) that includes the \( y \)-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

*No, the nail would not be short enough to go in the fire. It would just tip over.*
37 Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function $f(t) = -13\cos(0.8\pi t) + 13$, where $t$ represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of $f(t)$.

\[
\text{Period} = \frac{2\pi}{\text{frequency}} \quad \text{Period} = \frac{2}{0.8} = 2.5
\]

Interpret what the period represents in this context.

Question 37 is continued on the next page.

Score 1: The student received credit for correctly finding the period.
Question 37 continued.

On the grid below, graph *at least one* cycle of $f(t)$ that includes the $y$-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

**NO**
Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function \( f(t) = -13\cos(0.8\pi t) + 13 \), where \( t \) represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of \( f(t) \).

Interpret what the period represents in this context.

\( f(t) \) represents the cycle of the wheel at how high the nail is from the ground.

**Score 1:** The student received one credit for the graph.
On the grid below, graph at least one cycle of $f(t)$ that includes the $y$-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.
Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function $f(t) = -13\cos(0.8\pi t) + 13$, where $t$ represents the time (in seconds) since the nail first became caught in the tire.

Determine the period of $f(t)$.

Interpret what the period represents in this context.

$f(t)$ represents one cycle of the wheel, and how high the nail is from the ground.
On the grid below, graph at least one cycle of $f(t)$ that includes the $y$-intercept of the function.

Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

No, the maximum height is 23.5 inches.
The State Education Department / The University of the State of New York

Regents Examination in Algebra II – June 2019
Chart for Converting Total Test Raw Scores to Final Exam Scores (Scale Scores)
(Use for the June 2019 exam only.)

To determine the student’s final examination score (scale score), find the student’s total test raw score in the column labeled “Raw Score” and then locate the scale score that corresponds to that raw score. The scale score is the student’s final examination score. Enter this score in the space labeled “Scale Score” on the student’s answer sheet.

Schools are not permitted to rescore any of the open-ended questions on this exam after each question has been rated once, regardless of the final exam score. Schools are required to ensure that the raw scores have been added correctly and that the resulting scale score has been determined accurately.

Because scale scores corresponding to raw scores in the conversion chart change from one administration to another, it is crucial that for each administration the conversion chart provided for that administration be used to determine the student’s final score. The chart above is usable only for this administration of the Regents Examination in Algebra II.