

University of the State of New York

Examinations Department

78th examination

ALGEBRA

Wednesday, Nov. 25, 1891—9 : 15 a. m. to 12 : 15 p. m., only

48 credits, necessary to pass, 36

Give each step of solution. Express final result in its simplest form and mark it *Ans.*

1. Distinguish between (a) independent equations and simultaneous equations; (b) a radical and a surd. Give examples illustrating each answer. 4
2. Let $-a$ and $+b$ each represent a quantity. Find (a) their sum; (b) their difference; (c) their product; (d) their quotient. State why you consider each result obtained correct. 4
3. Reduce to lowest terms (a) $\frac{x^4 + x^2}{x^4 - 1}$; (b) $\frac{a - 3}{9 - a^2}$. 4
4. Reduce to a fractional form $\frac{x^4 - x^2 - 1}{x^2 + x + 1} - (x - x^2 - 1)$. 3
5. Simplify $\frac{a + x}{a - x} - \frac{a - x}{a + x}$. 2
6. Solve the equations,
 - (a) $(x - a)(x - b) + (a + b)^2 = (x + a)(x + b)$. 3
 - (b) $\frac{9}{x} - \frac{5}{y} = 2$, and $\frac{5}{x} + \frac{3}{y} = 30$. 4
7. Expand by the binomial theorem $(2a^3 - 3b^3)^5$. State the method of finding the coefficients of the terms and the exponents of their literal factors. 5
8. A rows m miles down stream in b hours and returns in c hours. Find A's rate of rowing in still water and the rate of the current. 4
9. Solve the equations,
 - (a) $\frac{2x^2 - 8}{7} - 3x + 7 = \frac{x - 3}{3}$. 3
 - (b) $x + \sqrt{xy} + y = 7$ and $x^2 + xy + y^2 = 21$. 4
10. Reduce to simplest form,
 - (a) $3\sqrt{5} - 4\sqrt{2}$ multiplied by $2\sqrt{5} + 3\sqrt{2}$. 3
 - (b) $21\sqrt{384}$ divided by $8\sqrt{98}$. 2
11. Find two numbers which are to each other as 4 to 3 and whose product increased by their sum equals 62. 3