

ADVANCED ALGEBRA

Monday, June 12, 1911—9.15 a. m. to 12.15 p. m., only

Write at top of first page of answer paper (a) name of school where you have studied, (b) number of weeks and recitations a week in algebra.

The minimum time requirement is five recitations a week in algebra for two school years.

*Answer eight questions. No credit will be allowed unless all operations (except mental ones) necessary to find results are given; simply indicating the operations is not sufficient.*

1 Find the number of inscribed triangles that can be formed by joining 15 points on the circumference of a circle.

2 Derive the formula for finding  $P$  permutations of  $n$  things taken  $r$  at a time.

3 Find the roots of  $4x^2 + 8x + 5 = 0$  and represent them graphically.

4 Prove that the interchange of any two adjacent columns of a determinant changes the sign of the determinant.

5 Solve by determinants 
$$\begin{cases} x + 2y + 3z = 13 \\ 2x + y + z = 7 \\ 3x + 4y + 3z = 21 \end{cases}$$

6 Show that the equation  $x^3 + px + q = 0$  has but one real root if  $p$  and  $q$  are positive, and that such real root is negative.

7 In the equation  $x^3 - 3x - 4 = 0$ , find by Horner's method, to two decimal places, the root lying between 2 and 3.

8 Construct from  $x = -2$  to  $x = +3$  the graph of the equation  $x^3 - 2x^2 - 2x + 3 = y$  and from this graph locate the roots of the equation.

9 The roots of the equation  $4x^3 - 12x^2 + 11x - 3 = 0$  are in arithmetical progression; find these roots.

10 Transform the equation  $5x^3 - 6x^2 - 3x + 8 = 0$  into an equation with integral coefficients, the coefficient of the highest power being unity. How are the roots of the transformed equation related to those of the given equation?