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REGENTS BY TYPE

The NY Algebra I CCSS Regents Exams Questions from Spring 2013 to January 2016 Sorted by Type

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Algebra I Common Core State Standards Multiple Choice Regents Exam Questions

1. The function \( h(t) = -16t^2 + 144 \) represents the height, \( h(t) \), in feet, of an object from the ground at \( t \) seconds after it is dropped. A realistic domain for this function is
   1) \(-3 \leq t \leq 3\)
   2) \(0 \leq t \leq 3\)
   3) \(0 \leq h(t) \leq 144\)
   4) all real numbers

2. For which function defined by a polynomial are the zeros of the polynomial \(-4\) and \(-6\)?
   1) \(y = x^2 - 10x - 24\)
   2) \(y = x^2 + 10x + 24\)
   3) \(y = x^2 + 10x - 24\)
   4) \(y = x^2 - 10x + 24\)

3. A polynomial function contains the factors \(x\), \(x - 2\), and \(x + 5\). Which graph(s) below could represent the graph of this function?

4. Which trinomial is equivalent to \(3(x - 2)^2 - 2(x - 1)\)?
   1) \(3x^2 - 2x - 10\)
   2) \(3x^2 - 2x - 14\)
   3) \(3x^2 - 14x + 10\)
   4) \(3x^2 - 14x + 14\)

5. If \(f(x) = x^2 - 2x - 8\) and \(g(x) = \frac{1}{4}x - 1\), for which value of \(x\) is \(f(x) = g(x)\)?
   1) \(-1.75\) and \(-1.438\)
   2) \(-1.75\) and \(4\)
   3) \(-1.438\) and \(0\)
   4) \(4\) and \(0\)

6. A pattern of blocks is shown below.

   ![Pattern of blocks](image)

   If the pattern of blocks continues, which formula(s) could be used to determine the number of blocks in the \(n\)th term?

<table>
<thead>
<tr>
<th>I</th>
<th>II</th>
<th>III</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a_n = n + 4)</td>
<td>(a_1 = 2)</td>
<td>(a_n = a_{n-1} + 4)</td>
</tr>
<tr>
<td></td>
<td>(a_n = a_{n-1} + 4)</td>
<td>(a_n = 4n - 2)</td>
</tr>
</tbody>
</table>

   1) I and II
   2) I and III
   3) II and III
   4) III, only
7 A population that initially has 20 birds approximately doubles every 10 years. Which graph represents this population growth?

1)  

2)  

3)  

4)  

8 The function \( V(t) = 1350(1.017)^t \) represents the value \( V(t) \), in dollars, of a comic book \( t \) years after its purchase. The yearly rate of appreciation of the comic book is

1) 17%
2) 1.7%
3) 1.017%
4) 0.017%

9 Which system of equations has the same solution as the system below?

\[
\begin{align*}
2x + 2y &= 16 \\
3x - y &= 4
\end{align*}
\]

1) \( 2x + 2y = 16 \\
6x - 2y = 4 \)
2) \( 2x + 2y = 16 \\
6x - 2y = 8 \)
3) \( x + y = 16 \\
3x - y = 4 \)
4) \( 6x + 6y = 48 \\
6x + 2y = 8 \)

10 The formula for the volume of a cone is \( V = \frac{1}{3} \pi r^2 h \). The radius, \( r \), of the cone may be expressed as

1) \( \sqrt{\frac{3V}{\pi h}} \)
2) \( \sqrt[3]{\frac{V}{3\pi h}} \)
3) \( 3\sqrt[3]{\frac{V}{\pi h}} \)
4) \( \frac{1}{3} \sqrt[3]{\frac{V}{\pi h}} \)
11 Which graph represents \( f(x) = \begin{cases} x & \text{if } x < 1 \\ \sqrt{x} & \text{if } x \geq 1 \end{cases} \)?

1)  
2)  
3)  
4)  

12 Mo's farm stand sold a total of 165 pounds of apples and peaches. She sold apples for $1.75 per pound and peaches for $2.50 per pound. If she made $337.50, how many pounds of peaches did she sell?

1) 11  
2) 18  
3) 65  
4) 100

13 If a sequence is defined recursively by \( f(0) = 2 \) and \( f(n + 1) = -2f(n) + 3 \) for \( n \geq 0 \), then \( f(2) \) is equal to

1) 1  
2) -11  
3) 5  
4) 17

14 The graph below represents a jogger's speed during her 20-minute jog around her neighborhood.

Which statement best describes what the jogger was doing during the 9 – 12 minute interval of her jog?

1) She was standing still.  
2) She was increasing her speed.  
3) She was decreasing her speed.  
4) She was jogging at a constant rate.
15 Which equation has the same solutions as
\[ x^2 + 6x - 7 = 0? \]
1) \((x + 3)^2 = 2\)
2) \((x - 3)^2 = 2\)
3) \((x - 3)^2 = 16\)
4) \((x + 3)^2 = 16\)

16 Which equation(s) represent the graph below?

I \[ y = (x + 2)(x^2 - 4x - 12) \]
II \[ y = (x - 3)(x^2 + x - 2) \]
III \[ y = (x - 1)(x^2 - 5x - 6) \]

1) I, only
2) II, only
3) I and II
4) II and III

18 If \( A = 3x^2 + 5x - 6 \) and \( B = -2x^2 - 6x + 7 \), then \( A - B \) equals
1) \(-5x^2 - 11x + 13\)
2) \(5x^2 + 11x - 13\)
3) \(-5x^2 - x + 1\)
4) \(5x^2 - x + 1\)

19 For a recently released movie, the function
\[ y = 119.67(0.61)^x \] models the revenue earned, \( y \), in millions of dollars each week, \( x \), for several weeks after its release. Based on the equation, how much more money, in millions of dollars, was earned in revenue for week 3 than for week 5?
1) 37.27
2) 27.16
3) 17.06
4) 10.11

20 The value of the \( x \)-intercept for the graph of
\[ 4x - 5y = 40 \] is
1) 10
2) \(\frac{4}{5}\)
3) \(-\frac{4}{5}\)
4) -8

21 When factored completely, the expression \( p^4 - 81 \) is equivalent to
1) \((p^2 + 9)(p^2 - 9)\)
2) \((p^2 - 9)(p^2 - 9)\)
3) \((p^2 + 9)(p + 3)(p - 3)\)
4) \((p + 3)(p - 3)(p + 3)(p - 3)\)
22 Given: \( y + x > 2 \)
\[ y \leq 3x - 2 \]
Which graph shows the solution of the given set of inequalities?

23 Given: \( L = \sqrt{2} \)
\[ M = 3\sqrt{3} \]
\[ N = \sqrt{16} \]
\[ P = \sqrt{9} \]
Which expression results in a rational number?
1) \( L + M \)
2) \( M + N \)
3) \( N + P \)
4) \( P + L \)

24 If \( 4x^2 - 100 = 0 \), the roots of the equation are
1) \(-25\) and \(25\)
2) \(-25\), only
3) \(-5\) and \(5\)
4) \(-5\), only

25 Which statement is not always true?
1) The product of two irrational numbers is irrational.
2) The product of two rational numbers is rational.
3) The sum of two rational numbers is rational.
4) The sum of a rational number and an irrational number is irrational.

26 Four expressions are shown below.

I \[ 2(2x^2 - 2x - 60) \]
II \[ 4(x^2 - x - 30) \]
III \[ 4(x + 6)(x - 5) \]
IV \[ 4x(x - 1) - 120 \]

The expression \( 4x^2 - 4x - 120 \) is equivalent to
1) \( I \) and \( II \), only
2) \( II \) and \( IV \), only
3) \( I, II, \) and \( IV \)
4) \( II, III, \) and \( IV \)

27 Which domain would be the most appropriate set to use for a function that predicts the number of household online-devices in terms of the number of people in the household?
1) integers
2) whole numbers
3) irrational numbers
4) rational numbers
28 A ball is thrown into the air from the edge of a 48-foot-high cliff so that it eventually lands on the ground. The graph below shows the height, $y$, of the ball from the ground after $x$ seconds.

For which interval is the ball's height always decreasing?
1) $0 \leq x \leq 2.5$
2) $0 < x < 5.5$
3) $2.5 < x < 5.5$
4) $x \geq 2$

29 How does the graph of $f(x) = 3(x - 2)^2 + 1$ compare to the graph of $g(x) = x^2$?
1) The graph of $f(x)$ is wider than the graph of $g(x)$, and its vertex is moved to the left 2 units and up 1 unit.
2) The graph of $f(x)$ is narrower than the graph of $g(x)$, and its vertex is moved to the right 2 units and up 1 unit.
3) The graph of $f(x)$ is narrower than the graph of $g(x)$, and its vertex is moved to the left 2 units and up 1 unit.
4) The graph of $f(x)$ is wider than the graph of $g(x)$, and its vertex is moved to the right 2 units and up 1 unit.

30 Morgan can start wrestling at age 5 in Division 1. He remains in that division until his next odd birthday when he is required to move up to the next division level. Which graph correctly represents this information?

31 A company that manufactures radios first pays a start-up cost, and then spends a certain amount of money to manufacture each radio. If the cost of manufacturing $r$ radios is given by the function $c(r) = 5.25r + 125$, then the value 5.25 best represents
1) the start-up cost
2) the profit earned from the sale of one radio
3) the amount spent to manufacture each radio
4) the average number of radios manufactured
32. The two sets of data below represent the number of runs scored by two different youth baseball teams over the course of a season.

Team A: 4, 8, 5, 12, 3, 9, 5, 2
Team B: 5, 9, 11, 4, 6, 11, 2, 7
Which set of statements about the mean and standard deviation is true?
1) mean A < mean B, standard deviation A > standard deviation B
2) mean A > mean B, standard deviation A < standard deviation B
3) mean A < mean B, standard deviation A < standard deviation B
4) mean A > mean B, standard deviation A > standard deviation B

33. The diagrams below represent the first three terms of a sequence.

Assuming the pattern continues, which formula determines \( a_n \), the number of shaded squares in the \( n \)th term?
1) \( a_n = 4n + 12 \)
2) \( a_n = 4n + 8 \)
3) \( a_n = 4n + 4 \)
4) \( a_n = 4n + 2 \)

34. What are the roots of the equation \( x^2 + 4x - 16 = 0 \)?
1) \( 2 \pm 2\sqrt{5} \)
2) \( -2 \pm 2\sqrt{5} \)
3) \( 2 \pm 4\sqrt{5} \)
4) \( -2 \pm 4\sqrt{5} \)

35. A student is asked to solve the equation \( 4(3x - 1)^2 - 17 = 83 \). The student's solution to the problem starts as \( 4(3x - 1)^2 = 100 \)
\( (3x - 1)^2 = 25 \)
A correct next step in the solution of the problem is
1) \( 3x - 1 = \pm 5 \)
2) \( 3x - 1 = \pm 25 \)
3) \( 9x^2 - 1 = 25 \)
4) \( 9x^2 - 6x + 1 = 5 \)

36. Given the following expressions:

I. \( \frac{5}{8} + \frac{3}{5} \)
II. \( \frac{1}{2} + \sqrt{2} \)
III. \( \sqrt{5} \cdot \left( \sqrt{5} \right) \)
IV. \( 3 \cdot \left( \sqrt{49} \right) \)
Which expression(s) result in an irrational number?
1) II, only
2) III, only
3) I, III, IV
4) II, III, IV

37. If \( f(x) = \frac{\sqrt{2x + 3}}{6x - 5} \), then \( f\left( \frac{1}{2} \right) = \)
1) 1
2) -2
3) -1
4) \( \frac{13}{3} \)
38. The zeros of the function \( f(x) = (x + 2)^2 - 25 \) are
   1) \(-2\) and 5
   2) \(-3\) and 7
   3) \(-5\) and 2
   4) \(-7\) and 3

39. Given the graph of the line represented by the equation \( f(x) = -2x + b \), if \( b \) is increased by 4 units, the graph of the new line would be shifted 4 units
   1) right
   2) up
   3) left
   4) down

40. After performing analyses on a set of data, Jackie examined the scatter plot of the residual values for each analysis. Which scatter plot indicates the best linear fit for the data?
41 Which function has the same \( y \)-intercept as the graph below?

\[ y = \frac{12 - 6x}{4} \]

1) \( y = \frac{12 - 6x}{4} \)
2) \( 27 + 3y = 6x \)
3) \( 6y + x = 18 \)
4) \( y + 3 = 6x \)

42 The graph of the equation \( y = ax^2 \) is shown below.

If \( a \) is multiplied by \( \frac{1}{2} \), the graph of the new equation is

1) wider and opens downward
2) wider and opens upward
3) narrower and opens downward
4) narrower and opens upward

43 Which recursively defined function represents the sequence 3, 7, 15, 31, …?

1) \( f(1) = 3, \quad f(n + 1) = 2f(n) + 3 \)
2) \( f(1) = 3, \quad f(n + 1) = 2f(n) - 1 \)
3) \( f(1) = 3, \quad f(n + 1) = 2f(n) + 1 \)
4) \( f(1) = 3, \quad f(n + 1) = 3f(n) - 2 \)

44 Krystal was given $3000 when she turned 2 years old. Her parents invested it at a 2% interest rate compounded annually. No deposits or withdrawals were made. Which expression can be used to determine how much money Krystal had in the account when she turned 18?

1) \( 3000(1 + 0.02)^{16} \)
2) \( 3000(1 - 0.02)^{16} \)
3) \( 3000(1 + 0.02)^{18} \)
4) \( 3000(1 - 0.02)^{18} \)

45 Which inequality is represented by the graph below?

1) \( y \leq 2x - 3 \)
2) \( y \geq 2x - 3 \)
3) \( y \leq -3x + 2 \)
4) \( y \geq -3x + 2 \)
46 A typical cell phone plan has a fixed base fee that includes a certain amount of data and an overage charge for data use beyond the plan. A cell phone plan charges a base fee of $62 and an overage charge of $30 per gigabyte of data that exceed 2 gigabytes. If $C$ represents the cost and $g$ represents the total number of gigabytes of data, which equation could represent this plan when more than 2 gigabytes are used?

1) $C = 30 + 62(2 - g)$
2) $C = 30 + 62(g - 2)$
3) $C = 62 + 30(2 - g)$
4) $C = 62 + 30(g - 2)$

47 Which recursively defined function has a first term equal to 10 and a common difference of 4?

1) $f(1) = 10$
2) $f(1) = 4$
3) $f(1) = f(x - 1) + 4$
4) $f(1) = 4f(x - 1)$

48 Miriam and Jessica are growing bacteria in a laboratory. Miriam uses the growth function $f(t) = n^{2t}$ while Jessica uses the function $g(t) = n^{4t}$, where $n$ represents the initial number of bacteria and $t$ is the time, in hours. If Miriam starts with 16 bacteria, how many bacteria should Jessica start with to achieve the same growth over time?

1) 32
2) 16
3) 8
4) 4

49 If the quadratic formula is used to find the roots of the equation $x^2 - 6x - 19 = 0$, the correct roots are

1) $3 \pm 2\sqrt{7}$
2) $-3 \pm 2\sqrt{7}$
3) $3 \pm 4\sqrt{14}$
4) $-3 \pm 4\sqrt{14}$

50 The table below shows the annual salaries for the 24 members of a professional sports team in terms of millions of dollars.

<table>
<thead>
<tr>
<th>0.5</th>
<th>0.5</th>
<th>0.6</th>
<th>0.7</th>
<th>0.75</th>
<th>0.8</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.0</td>
<td>1.0</td>
<td>1.1</td>
<td>1.25</td>
<td>1.3</td>
<td>1.4</td>
</tr>
<tr>
<td>1.4</td>
<td>1.8</td>
<td>2.5</td>
<td>3.7</td>
<td>3.8</td>
<td>4.0</td>
</tr>
<tr>
<td>4.2</td>
<td>4.6</td>
<td>5.1</td>
<td>6.0</td>
<td>6.3</td>
<td>7.2</td>
</tr>
</tbody>
</table>

The team signs an additional player to a contract worth 10 million dollars per year. Which statement about the median and mean is true?

1) Both will increase.
2) Only the median will increase.
3) Only the mean will increase.
4) Neither will change.

51 A company produces $x$ units of a product per month, where $C(x)$ represents the total cost and $R(x)$ represents the total revenue for the month. The functions are modeled by $C(x) = 300x + 250$ and $R(x) = -0.5x^2 + 800x - 100$. The profit is the difference between revenue and cost where $P(x) = R(x) - C(x)$. What is the total profit, $P(x)$, for the month?

1) $P(x) = -0.5x^2 + 500x - 150$
2) $P(x) = -0.5x^2 + 500x - 350$
3) $P(x) = -0.5x^2 - 500x + 350$
4) $P(x) = -0.5x^2 + 500x + 350$
52. The graph of the function \( f(x) = \sqrt{x + 4} \) is shown below.

The domain of the function is
1) \( \{x \mid x > 0\} \)
2) \( \{x \mid x \geq 0\} \)
3) \( \{x \mid x > -4\} \)
4) \( \{x \mid x \geq -4\} \)

53. The graph of \( f(x) \) is shown below.

Which function could represent the graph of \( f(x) \)?
1) \( f(x) = (x + 2)(x^2 + 3x - 4) \)
2) \( f(x) = (x - 2)(x^2 + 3x - 4) \)
3) \( f(x) = (x + 2)(x^2 + 3x + 4) \)
4) \( f(x) = (x - 2)(x^2 + 3x + 4) \)

54. If the area of a rectangle is expressed as \( x^4 - 9y^2 \), then the product of the length and the width of the rectangle could be expressed as
1) \( (x - 3y)(x + 3y) \)
2) \( (x^2 - 3y)(x^2 + 3y) \)
3) \( (x^2 - 3y)(x^2 - 3y) \)
4) \( (x^4 + y)(x - 9y) \)

55. Which quadratic function has the largest maximum?
1) \( h(x) = (3 - x)(2 + x) \)
2) \( k(x) = -5x^2 - 12x + 4 \)
3) \( h(x) = (3 - x)(2 + x) \)
4) \( k(x) = -5x^2 - 12x + 4 \)

56. If \( f(1) = 3 \) and \( f(n) = -2f(n - 1) + 1 \), then \( f(5) = \)
1) \(-5\)
2) \(11\)
3) \(21\)
4) \(43\)
57 Christopher looked at his quiz scores shown below for the first and second semester of his Algebra class.
Semester 1: 78, 91, 88, 83, 94
Semester 2: 91, 96, 80, 77, 88, 85, 92
Which statement about Christopher's performance is correct?
1) The interquartile range for semester 1 is greater than the interquartile range for semester 2.
2) The median score for semester 1 is greater than the median score for semester 2.
3) The mean score for semester 2 is greater than the mean score for semester 1.
4) The third quartile for semester 2 is greater than the third quartile for semester 1.

58 John has four more nickels than dimes in his pocket, for a total of $1.25. Which equation could be used to determine the number of dimes, x, in his pocket?
1) 0.10(x + 4) + 0.05(x) = $1.25
2) 0.05(x + 4) + 0.10(x) = $1.25
3) 0.10(4x) + 0.05(x) = $1.25
4) 0.05(4x) + 0.10(x) = $1.25

59 The solution of the equation \((x + 3)^2 = 7\) is
1) \(3 \pm \sqrt{7}\)
2) \(7 \pm \sqrt{3}\)
3) \(-3 \pm \sqrt{7}\)
4) \(-7 \pm \sqrt{3}\)

60 The cost of airing a commercial on television is modeled by the function \(C(n) = 110n + 900\), where \(n\) is the number of times the commercial is aired. Based on this model, which statement is true?
1) The commercial costs $0 to produce and $110 per airing up to $900.
2) The commercial costs $110 to produce and $900 each time it is aired.
3) The commercial costs $900 to produce and $110 each time it is aired.
4) The commercial costs $1010 to produce and can air an unlimited number of times.

61 A cell phone company charges $60.00 a month for up to 1 gigabyte of data. The cost of additional data is $0.05 per megabyte. If \(d\) represents the number of additional megabytes used and \(c\) represents the total charges at the end of the month, which linear equation can be used to determine a user's monthly bill?
1) \(c = 60 - 0.05d\)
2) \(c = 60.05d\)
3) \(c = 60d - 0.05\)
4) \(c = 60 + 0.05d\)

62 An astronaut drops a rock off the edge of a cliff on the Moon. The distance, \(d(t)\), in meters, the rock travels after \(t\) seconds can be modeled by the function \(d(t) = 0.8t^2\). What is the average speed, in meters per second, of the rock between 5 and 10 seconds after it was dropped?
1) 12
2) 20
3) 60
4) 80
63 Which ordered pair is not in the solution set of 
\[ y > \frac{-1}{2}x + 5 \] and \[ y \leq 3x - 2 \]?
1) (5,3)  
2) (4,3)  
3) (3,4)  
4) (4,4)

64 If \( f(x) = \frac{1}{3}x + 9 \), which statement is always true?
1) \( f(x) < 0 \)  
2) \( f(x) > 0 \)  
3) If \( x < 0 \), then \( f(x) < 0 \).  
4) If \( x > 0 \), then \( f(x) > 0 \).

65 Keith determines the zeros of the function \( f(x) \) to be \(-6\) and \(5\). What could be Keith's function?
1) \( f(x) = (x + 5)(x + 6) \)  
2) \( f(x) = (x + 5)(x - 6) \)  
3) \( f(x) = (x - 5)(x + 6) \)  
4) \( f(x) = (x - 5)(x - 6) \)

66 Grisham is considering the three situations below.
I. For the first 28 days, a sunflower grows at a rate of 3.5 cm per day.  
II. The value of a car depreciates at a rate of 15% per year after it is purchased.  
III. The amount of bacteria in a culture triples every two days during an experiment.  
Which of the statements describes a situation with an equal difference over an equal interval?
1) I, only  
2) II, only  
3) I and III  
4) II and III

67 Given the following quadratic functions:
\[ g(x) = -x^2 - x + 6 \]

<table>
<thead>
<tr>
<th>( x )</th>
<th>-3</th>
<th>-2</th>
<th>-1</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>( n(x) )</td>
<td>-7</td>
<td>0</td>
<td>5</td>
<td>8</td>
<td>9</td>
<td>8</td>
<td>5</td>
<td>0</td>
<td>-7</td>
</tr>
</tbody>
</table>

Which statement about these functions is true?
1) Over the interval \(-1 \leq x \leq 1\), the average rate of change for \( n(x) \) is less than that for \( g(x) \).  
2) The \( y \)-intercept of \( g(x) \) is greater than the \( y \)-intercept for \( n(x) \).  
3) The function \( g(x) \) has a greater maximum value than \( n(x) \).  
4) The sum of the roots of \( n(x) = 0 \) is greater than the sum of the roots of \( g(x) = 0 \).

68 Two functions, \( y = |x - 3| \) and \( 3x + 3y = 27 \), are graphed on the same set of axes. Which statement is true about the solution to the system of equations?
1) \((3,0)\) is the solution to the system because it satisfies the equation \( y = |x - 3| \).  
2) \((9,0)\) is the solution to the system because it satisfies the equation \( 3x + 3y = 27 \).  
3) \((6,3)\) is the solution to the system because it satisfies both equations.  
4) \((3,0)\), \((9,0)\), and \((6,3)\) are the solutions to the system of equations because they all satisfy at least one of the equations.

69 If Lylah completes the square for \( f(x) = x^2 - 12x + 7 \) in order to find the minimum, she must write \( f(x) \) in the general form \( f(x) = (x - a)^2 + b \). What is the value of \( a \) for \( f(x) \)?
1) \( 6 \)  
2) \(-6\)  
3) \( 12 \)  
4) \(-12\)
70 Beverly did a study this past spring using data she collected from a cafeteria. She recorded data weekly for ice cream sales and soda sales. Beverly found the line of best fit and the correlation coefficient, as shown in the diagram below.

Given this information, which statement(s) can correctly be concluded?
I. Eating more ice cream causes a person to become thirsty.
II. Drinking more soda causes a person to become hungry.
III. There is a strong correlation between ice cream sales and soda sales.
1) I, only
2) III, only
3) I and III
4) II and III

71 Which expression is equivalent to \(x^4 - 12x^2 + 36\)?
1) \((x^2 - 6)(x^2 - 6)\)
2) \((x^2 + 6)(x^2 + 6)\)
3) \((6 - x^2)(6 + x^2)\)
4) \((x^2 + 6)(x^2 - 6)\)

72 Which statistic would indicate that a linear function would not be a good fit to model a data set?
1) \(r = -0.93\)
2) \(r = 1\)
3) \(r = 0\)
4) All of the above

73 What is the value of \(x\) in the equation \(\frac{x - 2}{3} + \frac{1}{6} = \frac{5}{6}\)?
1) 4
2) 6
3) 8
4) 11
74 Natasha is planning a school celebration and wants to have live music and food for everyone who attends. She has found a band that will charge her $750 and a caterer who will provide snacks and drinks for $2.25 per person. If her goal is to keep the average cost per person between $2.75 and $3.25, how many people, \( p \), must attend?

1) \( 225 < p < 325 \)  
2) \( 325 < p < 750 \)  
3) \( 500 < p < 1000 \)  
4) \( 750 < p < 1500 \)

75 Firing a piece of pottery in a kiln takes place at different temperatures for different amounts of time. The graph below shows the temperatures in a kiln while firing a piece of pottery after the kiln is preheated to 200ºF.

During which time interval did the temperature in the kiln show the greatest average rate of change?

1) 0 to 1 hour  
2) 1 hour to 1.5 hours  
3) 2.5 hours to 5 hours  
4) 5 hours to 8 hours

76 The equation for the volume of a cylinder is \( V = \pi r^2 h \). The positive value of \( r \), in terms of \( h \) and \( V \), is

1) \( r = \sqrt{\frac{V}{\pi h}} \)  
2) \( r = \sqrt{V \pi h} \)  
3) \( r = 2V \pi h \)  
4) \( r = \frac{V}{2\pi} \)

77 In the function \( f(x) = (x - 2)^2 + 4 \), the minimum value occurs when \( x \) is

1) \(-2\)  
2) \(2\)  
3) \(-4\)  
4) \(4\)

78 A satellite television company charges a one-time installation fee and a monthly service charge. The total cost is modeled by the function \( y = 40 + 90x \). Which statement represents the meaning of each part of the function?

1) \( y \) is the total cost, \( x \) is the number of months of service, $90 is the installation fee, and $40 is the service charge per month.  
2) \( y \) is the total cost, \( x \) is the number of months of service, $40 is the installation fee, and $90 is the service charge per month.  
3) \( x \) is the total cost, \( y \) is the number of months of service, $40 is the installation fee, and $90 is the service charge per month.  
4) \( x \) is the total cost, \( y \) is the number of months of service, $90 is the installation fee, and $40 is the service charge per month.
79 The distance a free falling object has traveled can be modeled by the equation \( d = \frac{1}{2} at^2 \), where \( a \) is acceleration due to gravity and \( t \) is the amount of time the object has fallen. What is \( t \) in terms of \( a \) and \( d \)?

1) \( t = \sqrt{\frac{2d}{a}} \)
2) \( t = \frac{2d}{a} \)
3) \( t = \left( \frac{da}{d} \right)^\frac{1}{2} \)
4) \( t = \left( \frac{2d}{a} \right)^\frac{1}{2} \)

80 The table below shows the cost of mailing a postcard in different years. During which time interval did the cost increase at the greatest average rate?

<table>
<thead>
<tr>
<th>Year</th>
<th>1898</th>
<th>1971</th>
<th>1985</th>
<th>2006</th>
<th>2012</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cost (¢)</td>
<td>1</td>
<td>6</td>
<td>14</td>
<td>24</td>
<td>35</td>
</tr>
</tbody>
</table>

1) 1898-1971
2) 1971-1985
3) 1985-2006
4) 2006-2012

81 The Jamison family kept a log of the distance they traveled during a trip, as represented by the graph below.

During which interval was their average speed the greatest?

1) the first hour to the second hour
2) the second hour to the fourth hour
3) the sixth hour to the eighth hour
4) the eighth hour to the tenth hour

82 Let \( f \) be a function such that \( f(x) = 2x - 4 \) is defined on the domain \( 2 \leq x \leq 6 \). The range of this function is

1) \( 0 \leq y \leq 8 \)
2) \( 0 \leq y < \infty \)
3) \( 2 \leq y \leq 6 \)
4) \( -\infty < y < \infty \)
83 Joey enlarged a 3-inch by 5-inch photograph on a copy machine. He enlarged it four times. The table below shows the area of the photograph after each enlargement.

<table>
<thead>
<tr>
<th>Enlargement</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Area (square inches)</td>
<td>15</td>
<td>18.8</td>
<td>23.4</td>
<td>29.3</td>
<td>36.6</td>
</tr>
</tbody>
</table>

What is the average rate of change of the area from the original photograph to the fourth enlargement, to the nearest tenth?
1) 4.3  
2) 4.5  
3) 5.4  
4) 6.0

84 For which value of $P$ and $W$ is $P + W$ a rational number?
1) $P = \frac{1}{\sqrt{3}}$ and $W = \frac{1}{\sqrt{6}}$  
2) $P = \frac{1}{\sqrt{4}}$ and $W = \frac{1}{\sqrt{9}}$  
3) $P = \frac{1}{\sqrt{6}}$ and $W = \frac{1}{\sqrt{10}}$  
4) $P = \frac{1}{\sqrt{25}}$ and $W = \frac{1}{\sqrt{2}}$

85 If $f(x) = 3^x$ and $g(x) = 2x + 5$, at which value of $x$ is $f(x) < g(x)$?
1) $-1$  
2) 2  
3) $-3$  
4) 4

86 When $(2x - 3)^2$ is subtracted from $5x^2$, the result is
1) $x^2 - 12x - 9$  
2) $x^2 - 12x + 9$  
3) $x^2 + 12x - 9$  
4) $x^2 + 12x + 9$

87 During the 2010 season, football player McGee’s earnings, $m$, were 0.005 million dollars more than those of his teammate Fitzpatrick’s earnings, $f$. The two players earned a total of 3.95 million dollars. Which system of equations could be used to determine the amount each player earned, in millions of dollars?
1) $m + f = 3.95$  
2) $m - 3.95 = f$  
3) $f - 3.95 = m$  
4) $m + f = 3.95$  

88 A laboratory technician studied the population growth of a colony of bacteria. He recorded the number of bacteria every other day, as shown in the partial table below.

<table>
<thead>
<tr>
<th>$t$ (time, in days)</th>
<th>0</th>
<th>2</th>
<th>4</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f(t)$ (bacteria)</td>
<td>25</td>
<td>15,625</td>
<td>9,765,625</td>
<td>65,700,062</td>
</tr>
</tbody>
</table>

Which function would accurately model the technician's data?
1) $f(t) = 25^t$  
2) $f(t) = 25^{t+1}$  
3) $f(t) = 25t$  
4) $f(t) = 25(t + 1)$
89 The graph of \( y = f(x) \) is shown below.

Which point could be used to find \( f(2) \)?
1) \( A \)
2) \( B \)
3) \( C \)
4) \( D \)

91 Which representations are functions?

1) I and II
2) II and IV
3) III, only
4) IV, only

92 Which value of \( x \) satisfies the equation \( \frac{7}{3} \left( x + \frac{9}{28} \right) = 20 \)?
1) 8.25
2) 8.89
3) 19.25
4) 44.92

93 The cost of a pack of chewing gum in a vending machine is $0.75. The cost of a bottle of juice in the same machine is $1.25. Julia has $22.00 to spend on chewing gum and bottles of juice for her team and she must buy seven packs of chewing gum. If \( b \) represents the number of bottles of juice, which inequality represents the maximum number of bottles she can buy?
1) \( 0.75b + 1.25(7) \geq 22 \)
2) \( 0.75b + 1.25(7) \leq 22 \)
3) \( 0.75(7) + 1.25b \geq 22 \)
4) \( 0.75(7) + 1.25b \leq 22 \)
94 The graph of a linear equation contains the points (3,11) and (−2,1). Which point also lies on the graph?
1) (2,1)  
2) (2,4)  
3) (2,6)  
4) (2,9)

95 Peyton is a sprinter who can run the 40-yard dash in 4.5 seconds. He converts his speed into miles per hour, as shown below.
\[
\frac{40 \text{yd}}{4.5 \text{sec}} \cdot \frac{3 \text{ft}}{1 \text{yd}} \cdot \frac{5280 \text{ft}}{1 \text{mi}} \cdot \frac{60 \text{sec}}{1 \text{min}} \cdot \frac{60 \text{min}}{1 \text{hr}}
\]
Which ratio is incorrectly written to convert his speed?
1) \(\frac{3 \text{ ft}}{1 \text{yd}}\)  
2) \(\frac{5280 \text{ ft}}{1 \text{mi}}\)  
3) \(\frac{60 \text{ sec}}{1 \text{min}}\)  
4) \(\frac{60 \text{ min}}{1 \text{hr}}\)

96 Officials in a town use a function, \(C\), to analyze traffic patterns. \(C(n)\) represents the rate of traffic through an intersection where \(n\) is the number of observed vehicles in a specified time interval. What would be the most appropriate domain for the function?
1) \(\{\ldots -2, -1, 0, 1, 2, 3, \ldots \}\)  
2) \(\{-2, -1, 0, 1, 2, 3\}\)  
3) \(\{0, \frac{1}{2}, 1, \frac{1}{2}, 2, \frac{1}{2}\}\)  
4) \(\{0, 1, 2, 3, \ldots \}\)

97 In 2013, the United States Postal Service charged $0.46 to mail a letter weighing up to 1 oz. and $0.20 per ounce for each additional ounce. Which function would determine the cost, in dollars, \(c(z)\), of mailing a letter weighing \(z\) ounces where \(z\) is an integer greater than 1?
1) \(c(z) = 0.46z + 0.20\)  
2) \(c(z) = 0.20z + 0.46\)  
3) \(c(z) = 0.46(z - 1) + 0.20\)  
4) \(c(z) = 0.20(z - 1) + 0.46\)

98 Which situation could be modeled by using a linear function?
1) a bank account balance that grows at a rate of 5% per year, compounded annually  
2) a population of bacteria that doubles every 4.5 hours  
3) the cost of cell phone service that charges a base amount plus 20 cents per minute  
4) the concentration of medicine in a person’s body that decays by a factor of one-third every hour
99 A function is graphed on the set of axes below.

Which function is related to the graph?

1) \( f(x) = \begin{cases} x^2, & x < 1 \\ x - 2, & x > 1 \end{cases} \)

2) \( f(x) = \begin{cases} x^2, & x < 1 \\ \frac{1}{2}x + \frac{1}{2}, & x > 1 \end{cases} \)

3) \( f(x) = \begin{cases} x^2, & x < 1 \\ 2x - 7, & x > 1 \end{cases} \)

4) \( f(x) = \begin{cases} x^2, & x < 1 \\ \frac{3}{2}x - \frac{9}{2}, & x > 1 \end{cases} \)

100 When solving the equation \( x^2 - 8x - 7 = 0 \) by completing the square, which equation is a step in the process?

1) \( (x - 4)^2 = 9 \)

2) \( (x - 4)^2 = 23 \)

3) \( (x - 8)^2 = 9 \)

4) \( (x - 8)^2 = 23 \)

101 Given the functions \( h(x) = \frac{1}{2}x + 3 \) and \( j(x) = |x| \), which value of \( x \) makes \( h(x) = j(x) \)?

1) \(-2\)

2) \(2\)

3) \(3\)

4) \(-6\)

102 The table below shows the number of grams of carbohydrates, \( x \), and the number of Calories, \( y \), of six different foods.

<table>
<thead>
<tr>
<th>Carbohydrates (x)</th>
<th>Calories (y)</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>120</td>
</tr>
<tr>
<td>9.5</td>
<td>138</td>
</tr>
<tr>
<td>10</td>
<td>147</td>
</tr>
<tr>
<td>6</td>
<td>88</td>
</tr>
<tr>
<td>7</td>
<td>108</td>
</tr>
<tr>
<td>4</td>
<td>62</td>
</tr>
</tbody>
</table>

Which equation best represents the line of best fit for this set of data?

1) \( y = 15x \)

2) \( y = 0.07x \)

3) \( y = 0.1x - 0.4 \)

4) \( y = 14.1x + 5.8 \)

103 A sunflower is 3 inches tall at week 0 and grows 2 inches each week. Which function(s) shown below can be used to determine the height, \( f(n) \), of the sunflower in \( n \) weeks?

I. \( f(n) = 2n + 3 \)

II. \( f(n) = 2n + 3(n - 1) \)

III. \( f(n) = f(n - 1) + 2 \) where \( f(0) = 3 \)

1) I and II

2) II, only

3) III, only

4) I and III
104 Which equation is equivalent to \( y - 34 = x(x - 12) \)?

1) \( y = (x - 17)(x + 2) \)
2) \( y = (x - 17)(x - 2) \)
3) \( y = (x - 6)^2 + 2 \)
4) \( y = (x - 6)^2 - 2 \)

105 The graph representing a function is shown below.

Which function has a minimum that is less than the one shown in the graph?

1) \( y = x^2 - 6x + 7 \)
2) \( y = |x + 3| - 6 \)
3) \( y = x^2 - 2x - 10 \)
4) \( y = |x - 8| + 2 \)

106 What are the solutions to the equation \( x^2 - 8x = 24 \)?

1) \( x = 4 \pm 2\sqrt{10} \)
2) \( x = -4 \pm 2\sqrt{10} \)
3) \( x = 4 \pm 2\sqrt{2} \)
4) \( x = -4 \pm 2\sqrt{2} \)

107 What are the zeros of the function \( f(x) = x^2 - 13x - 30 \)?

1) \(-10 \text{ and } 3\)
2) \(10 \text{ and } -3\)
3) \(-15 \text{ and } 2\)
4) \(15 \text{ and } -2\)

108 The third term in an arithmetic sequence is 10 and the fifth term is 26. If the first term is \( a_1 \), which is an equation for the \( n \)th term of this sequence?

1) \( a_n = 8n + 10 \)
2) \( a_n = 8n - 14 \)
3) \( a_n = 16n + 10 \)
4) \( a_n = 16n - 38 \)

109 Which point is not on the graph represented by \( y = x^2 + 3x - 6 \)?

1) \((-6, 12)\)
2) \((-4, -2)\)
3) \((2, 4)\)
4) \((3, -6)\)

110 A construction company uses the function \( f(p) \), where \( p \) is the number of people working on a project, to model the amount of money it spends to complete a project. A reasonable domain for this function would be

1) positive integers
2) positive real numbers
3) both positive and negative integers
4) both positive and negative real numbers
111 The graph of $y = f(x)$ is shown below.

What is the graph of $y = f(x + 1) - 2$?

112 The range of the function defined as $y = 5^x$ is

1) $y < 0$
2) $y > 0$
3) $y \leq 0$
4) $y \geq 0$

113 Last week, a candle store received $355.60 for
selling 20 candles. Small candles sell for $10.98 and large candles sell for $27.98. How many large
 candles did the store sell?

1) 6
2) 8
3) 10
4) 12

114 What is the correlation coefficient of the linear fit of the data shown below, to the nearest hundredth?

1) 1.00
2) 0.93
3) −0.93
4) −1.00
115 Which graph shows a line where each value of $y$ is three more than half of $x$?

![Graph 1](image1)

116 The zeros of the function $f(x) = 3x^2 - 3x - 6$ are

1) $-1$ and $-2$
2) $1$ and $-2$
3) $1$ and $2$
4) $-1$ and $2$

117 The length of the shortest side of a right triangle is 8 inches. The lengths of the other two sides are represented by consecutive odd integers. Which equation could be used to find the lengths of the other sides of the triangle?

1) $8^2 + (x + 1) = x^2$
2) $x^2 + 8^2 = (x + 1)^2$
3) $8^2 + (x + 2) = x^2$
4) $x^2 + 8^2 = (x + 2)^2$

118 The owner of a small computer repair business has one employee, who is paid an hourly rate of $22$. The owner estimates his weekly profit using the function $P(x) = 8600 - 22x$. In this function, $x$ represents the number of

1) computers repaired per week
2) hours worked per week
3) customers served per week
4) days worked per week

119 Rowan has $50 in a savings jar and is putting in $5 every week. Jonah has $10 in his own jar and is putting in $15 every week. Each of them plots his progress on a graph with time on the horizontal axis and amount in the jar on the vertical axis. Which statement about their graphs is true?

1) Rowan’s graph has a steeper slope than Jonah’s.
2) Rowan’s graph always lies above Jonah’s.
3) Jonah’s graph has a steeper slope than Rowan’s.
4) Jonah’s graph always lies above Rowan’s.
120 The graph below was created by an employee at a gas station.

Which statement can be justified by using the graph?
1) If 10 gallons of gas was purchased, $35 was paid.
2) For every gallon of gas purchased, $3.75 was paid.
3) For every 2 gallons of gas purchased, $5.00 was paid.
4) If zero gallons of gas were purchased, zero miles were driven.

121 The value in dollars, \( v(x) \), of a certain car after \( x \) years is represented by the equation \( v(x) = 25,000(0.86)^x \). To the nearest dollar, how much more is the car worth after 2 years than after 3 years?
1) 2589
2) 6510
3) 15,901
4) 18,490

122 Connor wants to attend the town carnival. The price of admission to the carnival is $4.50, and each ride costs an additional 79 cents. If he can spend at most $16.00 at the carnival, which inequality can be used to solve for \( r \), the number of rides Connor can go on, and what is the maximum number of rides he can go on?
1) \( 0.79 + 4.50r \leq 16.00; 3 \) rides
2) \( 0.79 + 4.50r \leq 16.00; 4 \) rides
3) \( 4.50 + 0.79r \leq 16.00; 14 \) rides
4) \( 4.50 + 0.79r \leq 16.00; 15 \) rides

123 Which equation has the same solutions as \( 2x^2 + x - 3 = 0 \)?
1) \( (x + 3)^2 = 21 \)
2) \( (x - 3)^2 = 21 \)
3) \( (x + 3)(x - 1) = 0 \)
4) \( (x - 3)(x + 1) = 0 \)

124 Fred is given a rectangular piece of paper. If the length of Fred's piece of paper is represented by \( 2x - 6 \) and the width is represented by \( 3x - 5 \), then the paper has a total area represented by
1) \( 5x - 11 \)
2) \( 6x^2 - 28x + 30 \)
3) \( 10x - 22 \)
4) \( 6x^2 - 6x - 11 \)

125 Which equation has the same solution as \( x^2 - 6x - 12 = 0 \)?
1) \( (x + 3)^2 = 21 \)
2) \( (x - 3)^2 = 21 \)
3) \( (x + 3)^2 = 3 \)
4) \( (x - 3)^2 = 3 \)
126 Which table of values represents a linear relationship?

<table>
<thead>
<tr>
<th>x</th>
<th>f(x)</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1</td>
<td>-3</td>
</tr>
<tr>
<td>0</td>
<td>-2</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>6</td>
</tr>
<tr>
<td>3</td>
<td>13</td>
</tr>
</tbody>
</table>

1)  

<table>
<thead>
<tr>
<th>x</th>
<th>f(x)</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1</td>
<td>1/2</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>2</td>
<td>4</td>
</tr>
<tr>
<td>3</td>
<td>8</td>
</tr>
</tbody>
</table>

2)  

<table>
<thead>
<tr>
<th>x</th>
<th>f(x)</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1</td>
<td>-3</td>
</tr>
<tr>
<td>0</td>
<td>-1</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>3</td>
<td>5</td>
</tr>
</tbody>
</table>

3)  

<table>
<thead>
<tr>
<th>x</th>
<th>f(x)</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1</td>
<td>-1</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>8</td>
</tr>
<tr>
<td>3</td>
<td>27</td>
</tr>
</tbody>
</table>

4)  

127 Sam and Jeremy have ages that are consecutive odd integers. The product of their ages is 783. Which equation could be used to find Jeremy’s age, \( j \), if he is the younger man?

1) \( j^2 + 2 = 783 \)
2) \( j^2 - 2 = 783 \)
3) \( j^2 + 2j = 783 \)
4) \( j^2 - 2j = 783 \)

128 The graphs below represent functions defined by polynomials. For which function are the zeros of the polynomials 2 and \(-3\)?

1) 

2) 

3) 

4)
129  The inequality $7 - \frac{2}{3}x < x - 8$ is equivalent to
   1) $x > 9$
   2) $x > -\frac{3}{5}$
   3) $x < 9$
   4) $x < -\frac{3}{5}$

130  The equation $A = 1300(1.02)^7$ is being used to calculate the amount of money in a savings account. What does 1.02 represent in this equation?
   1) 0.02% decay
   2) 0.02% growth
   3) 2% decay
   4) 2% growth

131  Michael borrows money from his uncle, who is charging him simple interest using the formula $I = Prt$. To figure out what the interest rate, $r$, is, Michael rearranges the formula to find $r$. His new formula is $r$ equals
   1) $\frac{I-P}{t}$
   2) $\frac{P-I}{t}$
   3) $\frac{I}{Pt}$
   4) $\frac{Pt}{I}$

132  What is one point that lies in the solution set of the system of inequalities graphed below?

133  Which function is shown in the table below?

<table>
<thead>
<tr>
<th>x</th>
<th>f(x)</th>
</tr>
</thead>
<tbody>
<tr>
<td>-2</td>
<td>1/9</td>
</tr>
<tr>
<td>-1</td>
<td>1/3</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>3</td>
</tr>
<tr>
<td>2</td>
<td>9</td>
</tr>
<tr>
<td>3</td>
<td>27</td>
</tr>
</tbody>
</table>
134 Which graph represents the solution of \( y \leq x + 3 \) and \( y \geq -2x - 2 \)?

1) 

2) 

3) 

4) 

135 To watch a varsity basketball game, spectators must buy a ticket at the door. The cost of an adult ticket is $3.00 and the cost of a student ticket is $1.50. If the number of adult tickets sold is represented by \( a \) and student tickets sold by \( s \), which expression represents the amount of money collected at the door from the ticket sales?

1) \( 4.50as \)
2) \( 4.50(a + s) \)
3) \( (3.00a)(1.50s) \)
4) \( 3.00a + 1.50s \)

136 Corinne is planning a beach vacation in July and is analyzing the daily high temperatures for her potential destination. She would like to choose a destination with a high median temperature and a small interquartile range. She constructed box plots shown in the diagram below.

Which destination has a median temperature above 80 degrees and the smallest interquartile range?

1) Ocean Beach
2) Whispering Palms
3) Serene Shores
4) Pelican Beach

137 Alicia has invented a new app for smart phones that two companies are interested in purchasing for a 2-year contract. Company \( A \) is offering her $10,000 for the first month and will increase the amount each month by $5000. Company \( B \) is offering $500 for the first month and will double their payment each month from the previous month. Monthly payments are made at the end of each month. For which monthly payment will company \( B \)'s payment first exceed company \( A \)'s payment?

1) 6
2) 7
3) 8
4) 9
Isaiah collects data from two different companies, each with four employees. The results of the study, based on each worker’s age and salary, are listed in the tables below.

Which statement is true about these data?
1) The median salaries in both companies are greater than $37,000.
2) The mean salary in company 1 is greater than the mean salary in company 2.
3) The salary range in company 2 is greater than the salary range in company 1.
4) The mean age of workers at company 1 is greater than the mean age of workers at company 2.

The table below shows the average yearly balance in a savings account where interest is compounded annually. No money is deposited or withdrawn after the initial amount is deposited.

Which type of function best models the given data?
1) linear function with a negative rate of change
2) linear function with a positive rate of change
3) exponential decay function
4) exponential growth function

Which pair of equations could _not_ be used to solve the following equations for $x$ and $y$?

$4x + 2y = 22$
$-2x + 2y = -8$

1) $4x + 2y = 22$
2) $4x + 2y = 22$
3) $12x + 6y = 66$
4) $8x + 4y = 44$

$2x - 2y = 8$
$-4x + 4y = -16$
$6x - 6y = 24$
$-8x + 8y = -8$
141 The table below shows the average diameter of a pupil in a person’s eye as he or she grows older.

<table>
<thead>
<tr>
<th>Age (years)</th>
<th>Average Pupil Diameter (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>4.7</td>
</tr>
<tr>
<td>30</td>
<td>4.3</td>
</tr>
<tr>
<td>40</td>
<td>3.9</td>
</tr>
<tr>
<td>50</td>
<td>3.5</td>
</tr>
<tr>
<td>60</td>
<td>3.1</td>
</tr>
<tr>
<td>70</td>
<td>2.7</td>
</tr>
<tr>
<td>80</td>
<td>2.3</td>
</tr>
</tbody>
</table>

What is the average rate of change, in millimeters per year, of a person’s pupil diameter from age 20 to age 80?
1) 2.4
2) 0.04
3) −2.4
4) −0.04

142 The table below represents the function $F$.

<table>
<thead>
<tr>
<th>$x$</th>
<th>3</th>
<th>4</th>
<th>6</th>
<th>7</th>
<th>8</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F(x)$</td>
<td>9</td>
<td>17</td>
<td>65</td>
<td>129</td>
<td>257</td>
</tr>
</tbody>
</table>

The equation that represents this function is
1) $F(x) = 3^x$
2) $F(x) = 3x$
3) $F(x) = 2^x + 1$
4) $F(x) = 2x + 3$

143 When factored completely, $x^3 - 13x^2 - 30x$ is
1) $(x+3)(x-10)$
2) $(x-3)(x-10)$
3) $(x+2)(x-15)$
4) $(x-2)(x+15)$

144 Given the functions $g(x)$, $f(x)$, and $h(x)$ shown below:

$$g(x) = x^2 - 2x$$

The correct list of functions ordered from greatest to least by average rate of change over the interval $0 \leq x \leq 3$ is
1) $f(x)$, $g(x)$, $h(x)$
2) $h(x)$, $g(x)$, $f(x)$
3) $g(x)$, $f(x)$, $h(x)$
4) $h(x)$, $f(x)$, $g(x)$

145 Joe has a rectangular patio that measures 10 feet by 12 feet. He wants to increase the area by 50% and plans to increase each dimension by equal lengths, $x$. Which equation could be used to determine $x$?
1) $(10+x)(12+x) = 120$
2) $(10+x)(12+x) = 180$
3) $(15+x)(18+x) = 180$
4) $(15)(18) = 120 + x^2$
146 When directed to solve a quadratic equation by completing the square, Sam arrived at the equation \( \left( x - \frac{5}{2} \right)^2 = \frac{13}{4} \). Which equation could have been the original equation given to Sam?

1) \( x^2 + 5x + 7 = 0 \)
2) \( x^2 + 5x + 3 = 0 \)
3) \( x^2 - 5x + 7 = 0 \)
4) \( x^2 - 5x + 3 = 0 \)

147 When solving the equation \( 4(3x^2 + 2) - 9 = 8x^2 + 7 \), Emily wrote \( 4(3x^2 + 2) = 8x^2 + 16 \) as her first step. Which property justifies Emily's first step?

1) addition property of equality
2) commutative property of addition
3) multiplication property of equality
4) distributive property of multiplication over addition

148 Some banks charge a fee on savings accounts that are left inactive for an extended period of time. The equation \( y = 5000(0.98)^x \) represents the value, \( y \), of one account that was left inactive for a period of \( x \) years. What is the \( y \)-intercept of this equation and what does it represent?

1) 0.98, the percent of money in the account initially
2) 0.98, the percent of money in the account after \( x \) years
3) 5000, the amount of money in the account initially
4) 5000, the amount of money in the account after \( x \) years

149 The country of Benin in West Africa has a population of 9.05 million people. The population is growing at a rate of 3.1% each year. Which function can be used to find the population 7 years from now?

1) \( f(t) = (9.05 \times 10^6)(1 - 0.31)^7 \)
2) \( f(t) = (9.05 \times 10^6)(1 + 0.31)^7 \)
3) \( f(t) = (9.05 \times 10^6)(1 + 0.031)^7 \)
4) \( f(t) = (9.05 \times 10^6)(1 - 0.031)^7 \)

150 Which statement is not always true?

1) The sum of two rational numbers is rational.
2) The product of two irrational numbers is rational.
3) The sum of a rational number and an irrational number is irrational.
4) The product of a nonzero rational number and an irrational number is irrational.

151 Which inequality is represented in the graph below?

1) \( y \geq -3x + 4 \)
2) \( y \leq -3x + 4 \)
3) \( y \geq -4x - 3 \)
4) \( y \leq -4x - 3 \)
152 The table below represents the residuals for a line of best fit.

<table>
<thead>
<tr>
<th>x</th>
<th>2</th>
<th>3</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Residual</td>
<td>2</td>
<td>1</td>
<td>-1</td>
<td>-2</td>
<td>-5</td>
<td>-2</td>
<td>-1</td>
<td>2</td>
<td>0</td>
</tr>
</tbody>
</table>

Plot these residuals on the set of axes below.

Using the plot, assess the fit of the line for these residuals and justify your answer.

153 Factor the expression $x^4 + 6x^2 - 7$ completely.

154 Solve the equation for $y$: $(y - 3)^2 = 4y - 12$

155 Determine the smallest integer that makes $-3x + 7 - 5x < 15$ true.

156 The vertex of the parabola represented by $f(x) = x^2 - 4x + 3$ has coordinates $(2, -1)$. Find the coordinates of the vertex of the parabola defined by $g(x) = f(x - 2)$. Explain how you arrived at your answer. [The use of the set of axes below is optional.]

157 In the equation $x^2 + 10x + 24 = (x + a)(x + b)$, $b$ is an integer. Find algebraically all possible values of $b$.

158 Dylan invested $600 in a savings account at a 1.6% annual interest rate. He made no deposits or withdrawals on the account for 2 years. The interest was compounded annually. Find, to the nearest cent, the balance in the account after 2 years.
159 On the set of axes below, graph the inequality \( 2x + y > 1 \).

160 If the difference \((3x^2 - 2x + 5) - (x^2 + 3x - 2)\) is multiplied by \(\frac{1}{2}x^2\), what is the result, written in standard form?

161 Rhonda deposited $3000 in an account in the Merrick National Bank, earning 4.2% interest, compounded annually. She made no deposits or withdrawals. Write an equation that can be used to find \(B\), her account balance after \(t\) years.

162 Subtract \(5x^2 + 2x - 11\) from \(3x^2 + 8x - 7\). Express the result as a trinomial.

163 A toy rocket is launched from the ground straight upward. The height of the rocket above the ground, in feet, is given by the equation 
\[h(t) = -16t^2 + 64t,\]
where \(t\) is the time in seconds. Determine the domain for this function in the given context. Explain your reasoning.

164 The function, \(t(x)\), is shown in the table below.

<table>
<thead>
<tr>
<th>(x)</th>
<th>(t(x))</th>
</tr>
</thead>
<tbody>
<tr>
<td>-3</td>
<td>10</td>
</tr>
<tr>
<td>-1</td>
<td>7.5</td>
</tr>
<tr>
<td>1</td>
<td>5</td>
</tr>
<tr>
<td>3</td>
<td>2.5</td>
</tr>
<tr>
<td>5</td>
<td>0</td>
</tr>
</tbody>
</table>

Determine whether \(t(x)\) is linear or exponential. Explain your answer.

165 Solve the inequality below to determine and state the smallest possible value for \(x\) in the solution set.
\[3(x + 3) \leq 5x - 3\]

166 A landscaper is creating a rectangular flower bed such that the width is half of the length. The area of the flower bed is 34 square feet. Write and solve an equation to determine the width of the flower bed, to the nearest tenth of a foot.

167 How many real solutions does the equation 
\[x^2 - 2x + 5 = 0\] have? Justify your answer.
168 On the set of axes below, graph the function represented by $y = \sqrt[3]{x - 2}$ for the domain $-6 \leq x \leq 10$.

169 A gardener is planting two types of trees:
Type $A$ is three feet tall and grows at a rate of 15 inches per year.
Type $B$ is four feet tall and grows at a rate of 10 inches per year.
Algebraically determine exactly how many years it will take for these trees to be the same height.

170 Each day Toni records the height of a plant for her science lab. Her data are shown in the table below.

The plant continues to grow at a constant daily rate. Write an equation to represent $h(n)$, the height of the plant on the $n$th day.

171 Solve $8m^2 + 20m = 12$ for $m$ by factoring.

172 A high school drama club is putting on their annual theater production. There is a maximum of 800 tickets for the show. The costs of the tickets are $6 before the day of the show and $9 on the day of the show. To meet the expenses of the show, the club must sell at least $5,000 worth of tickets.
a) Write a system of inequalities that represent this situation.
b) The club sells 440 tickets before the day of the show. Is it possible to sell enough additional tickets on the day of the show to at least meet the expenses of the show? Justify your answer.

173 Emma recently purchased a new car. She decided to keep track of how many gallons of gas she used on five of her business trips. The results are shown in the table below.

Write the linear regression equation for these data where miles driven is the independent variable. (Round all values to the nearest hundredth.)

174 Solve the equation $4x^2 - 12x = 7$ algebraically for $x$. 
175 The residual plots from two different sets of bivariate data are graphed below.

![Graph A](image1)

![Graph B](image2)

Explain, using evidence from graph A and graph B, which graph indicates that the model for the data is a good fit.

176 Jackson is starting an exercise program. The first day he will spend 30 minutes on a treadmill. He will increase his time on the treadmill by 2 minutes each day. Write an equation for \( T(d) \), the time, in minutes, on the treadmill on day \( d \). Find \( T(6) \), the minutes he will spend on the treadmill on day 6.

177 The function \( f \) has a domain of \( \{1, 3, 5, 7\} \) and a range of \( \{2, 4, 6\} \). Could \( f \) be represented by \( \{(1,2),(3,4),(5,6),(7,2)\} \)? Justify your answer.

178 Express the product of \( 2x^2 + 7x - 10 \) and \( x + 5 \) in standard form.

179 Graph the function \( y = |x - 3| \) on the set of axes below.

![Graph C](image3)

Explain how the graph of \( y = |x - 3| \) has changed from the related graph \( y = |x| \).

180 The cost of belonging to a gym can be modeled by \( C(m) = 50m + 79.50 \), where \( C(m) \) is the total cost for \( m \) months of membership. State the meaning of the slope and \( y \)-intercept of this function with respect to the costs associated with the gym membership.

181 The number of carbon atoms in a fossil is given by the function \( y = 5100(0.95)^x \), where \( x \) represents the number of years since being discovered. What is the percent of change each year? Explain how you arrived at your answer.
182 Alex is selling tickets to a school play. An adult ticket costs $6.50 and a student ticket costs $4.00. Alex sells \( x \) adult tickets and 12 student tickets. Write a function, \( f(x) \), to represent how much money Alex collected from selling tickets.

183 Write an exponential equation for the graph shown below.

184 Jacob and Jessica are studying the spread of dandelions. Jacob discovers that the growth over \( t \) weeks can be defined by the function \( f(t) = (8) \cdot 2^t \). Jessica finds that the growth function over \( t \) weeks is \( g(t) = 2^t + 3 \). Calculate the number of dandelions that Jacob and Jessica will each have after 5 weeks. Based on the growth from both functions, explain the relationship between \( f(t) \) and \( g(t) \).

185 John and Sarah are each saving money for a car. The total amount of money John will save is given by the function \( f(x) = 60 + 5x \). The total amount of money Sarah will save is given by the function \( g(x) = x^2 + 46 \). After how many weeks, \( x \), will they have the same amount of money saved? Explain how you arrived at your answer.

186 On the set of axes below, draw the graph of the equation \( y = \frac{3}{4}x + 3 \).

187 Given that \( a > b \), solve for \( x \) in terms of \( a \) and \( b \):

\[
b(x - 3) \geq ax + 7b
\]
188 Let \( f \) be the function represented by the graph below.

Let \( g \) be a function such that \( g(x) = -\frac{1}{2}x^2 + 4x + 3 \).
Determine which function has the larger maximum value. Justify your answer.

189 A statistics class surveyed some students during one lunch period to obtain opinions about television programming preferences. The results of the survey are summarized in the table below.

<table>
<thead>
<tr>
<th>Programming Preferences</th>
<th>Comedy</th>
<th>Drama</th>
</tr>
</thead>
<tbody>
<tr>
<td>Male</td>
<td>70</td>
<td>35</td>
</tr>
<tr>
<td>Female</td>
<td>48</td>
<td>42</td>
</tr>
</tbody>
</table>

Based on the sample, predict how many of the school's 351 males would prefer comedy. Justify your answer.

190 Ryker is given the graph of the function \( y = \frac{1}{2}x^2 - 4 \). He wants to find the zeros of the function, but is unable to read them exactly from the graph.

Find the zeros in simplest radical form.

191 Donna wants to make trail mix made up of almonds, walnuts and raisins. She wants to mix one part almonds, two parts walnuts, and three parts raisins. Almonds cost $12 per pound, walnuts cost $9 per pound, and raisins cost $5 per pound. Donna has $15 to spend on the trail mix. Determine how many pounds of trail mix she can make. [Only an algebraic solution can receive full credit.]
192 Draw the graph of \( y = \sqrt{x} - 1 \) on the set of axes below.

193 Marcel claims that the graph below represents a function.

State whether Marcel is correct. Justify your answer.

194 A driver leaves home for a business trip and drives at a constant speed of 60 miles per hour for 2 hours. Her car gets a flat tire, and she spends 30 minutes changing the tire. She resumes driving and drives at 30 miles per hour for the remaining one hour until she reaches her destination. On the set of axes below, draw a graph that models the driver’s distance from home.

195 A student was given the equation \( x^2 + 6x - 13 = 0 \) to solve by completing the square. The first step that was written is shown below.

\[
x^2 + 6x = 13
\]

The next step in the student’s process was \( x^2 + 6x + c = 13 + c \). State the value of \( c \) that creates a perfect square trinomial. Explain how the value of \( c \) is determined.

196 Given \( 2x + ax - 7 > -12 \), determine the largest integer value of \( a \) when \( x = -1 \).
Rachel and Marc were given the information shown below about the bacteria growing in a Petri dish in their biology class.

<table>
<thead>
<tr>
<th>Number of Hours, $x$</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of Bacteria, $B(x)$</td>
<td>220</td>
<td>280</td>
<td>350</td>
<td>440</td>
<td>550</td>
<td>690</td>
<td>860</td>
<td>1070</td>
<td>1340</td>
<td>1680</td>
</tr>
</tbody>
</table>

Rachel wants to model this information with a linear function. Marc wants to use an exponential function. Which model is the better choice? Explain why you chose this model.

The graph below shows the variation in the average temperature of Earth’s surface from 1950-2000, according to one source.

During which years did the temperature variation change the most per unit time? Explain how you determined your answer.

Guy and Jim work at a furniture store. Guy is paid $185 per week plus 3% of his total sales in dollars, $x$, which can be represented by $g(x) = 185 + 0.03x$. Jim is paid $275 per week plus 2.5% of his total sales in dollars, $x$, which can be represented by $f(x) = 275 + 0.025x$. Determine the value of $x$, in dollars, that will make their weekly pay the same.

The breakdown of a sample of a chemical compound is represented by the function $p(t) = 300(0.5)^t$, where $p(t)$ represents the number of milligrams of the substance and $t$ represents the time, in years. In the function $p(t)$, explain what 0.5 and 300 represent.

Jacob and Zachary go to the movie theater and purchase refreshments for their friends. Jacob spends a total of $18.25 on two bags of popcorn and three drinks. Zachary spends a total of $27.50 for four bags of popcorn and two drinks. Write a system of equations that can be used to find the price of one bag of popcorn and the price of one drink. Using these equations, determine and state the price of a bag of popcorn and the price of a drink, to the nearest cent.
202 The graph of an inequality is shown below.

![Graph of an inequality]

a) Write the inequality represented by the graph.
b) On the same set of axes, graph the inequality $x + 2y < 4$.
c) The two inequalities graphed on the set of axes form a system. Oscar thinks that the point (2, 1) is in the solution set for this system of inequalities. Determine and state whether you agree with Oscar. Explain your reasoning.

203 Robin collected data on the number of hours she watched television on Sunday through Thursday nights for a period of 3 weeks. The data are shown in the table below.

<table>
<thead>
<tr>
<th></th>
<th>Sun</th>
<th>Mon</th>
<th>Tues</th>
<th>Wed</th>
<th>Thurs</th>
</tr>
</thead>
<tbody>
<tr>
<td>Week 1</td>
<td>4</td>
<td>3</td>
<td>3.5</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>Week 2</td>
<td>4.5</td>
<td>5</td>
<td>2.5</td>
<td>3</td>
<td>1.5</td>
</tr>
<tr>
<td>Week 3</td>
<td>4</td>
<td>3</td>
<td>1</td>
<td>1.5</td>
<td>2.5</td>
</tr>
</tbody>
</table>

Using an appropriate scale on the number line below, construct a box plot for the 15 values.

204 Graph the following function on the set of axes below.

$$f(x) = \begin{cases} 
|x|, & -3 \leq x < 1 \\
4, & 1 \leq x \leq 8 
\end{cases}$$

205 Jacob and Zachary go to the movie theater and purchase refreshments for their friends. Jacob spends a total of $18.25 on two bags of popcorn and three drinks. Zachary spends a total of $27.50 for four bags of popcorn and two drinks. Write a system of equations that can be used to find the price of one bag of popcorn and the price of one drink. Using these equations, determine and state the price of a bag of popcorn and the price of a drink, to the nearest cent.
Algebra I Common Core State Standards 4 Point Regents Exam Questions

206 Write an equation that defines \( m(x) \) as a trinomial where \( m(x) = (3x - 1)(3 - x) + 4x^2 + 19 \). Solve for \( x \) when \( m(x) = 0 \).

207 An application developer released a new app to be downloaded. The table below gives the number of downloads for the first four weeks after the launch of the app.

<table>
<thead>
<tr>
<th>Number of Weeks</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of Downloads</td>
<td>120</td>
<td>180</td>
<td>270</td>
<td>405</td>
</tr>
</tbody>
</table>

Write an exponential equation that models these data. Use this model to predict how many downloads the developer would expect in the 26th week if this trend continues. Round your answer to the nearest download. Would it be reasonable to use this model to predict the number of downloads past one year? Explain your reasoning.

208 David has two jobs. He earns $8 per hour babysitting his neighbor’s children and he earns $11 per hour working at the coffee shop. Write an inequality to represent the number of hours, \( x \), babysitting and the number of hours, \( y \), working at the coffee shop that David will need to work to earn a minimum of $200. David worked 15 hours at the coffee shop. Use the inequality to find the number of full hours he must babysit to reach his goal of $200.

209 a) Given the function \( f(x) = -x^2 + 8x + 9 \), state whether the vertex represents a maximum or minimum point for the function. Explain your answer.

b) Rewrite \( f(x) \) in vertex form by completing the square.

210 Max purchased a box of green tea mints. The nutrition label on the box stated that a serving of three mints contains a total of 10 Calories. On the axes below, graph the function, \( C(x) \), where \( C(x) \) represents the number of Calories in \( x \) mints.

Write an equation that represents \( C(x) \). A full box of mints contains 180 Calories. Use the equation to determine the total number of mints in the box.

211 Let \( h(t) = -16t^2 + 64t + 80 \) represent the height of an object above the ground after \( t \) seconds. Determine the number of seconds it takes to achieve its maximum height. Justify your answer. State the time interval, in seconds, during which the height of the object decreases. Explain your reasoning.
212 Graph \( f(x) = x^2 \) and \( g(x) = 2^x \) for \( x \geq 0 \) on the set of axes below.

State which function, \( f(x) \) or \( g(x) \), has a greater value when \( x = 20 \). Justify your reasoning.

213 Caitlin has a movie rental card worth $175. After she rents the first movie, the card’s value is $172.25. After she rents the second movie, its value is $169.50. After she rents the third movie, the card is worth $166.75. Assuming the pattern continues, write an equation to define \( A(n) \), the amount of money on the rental card after \( n \) rentals. Caitlin rents a movie every Friday night. How many weeks in a row can she afford to rent a movie, using her rental card only? Explain how you arrived at your answer.

214 On the axes below, graph \( f(x) = |3x| \).

If \( g(x) = f(x) - 2 \), how is the graph of \( f(x) \) translated to form the graph of \( g(x) \)? If \( h(x) = f(x - 4) \), how is the graph of \( f(x) \) translated to form the graph of \( h(x) \)?

215 An animal shelter spends $2.35 per day to care for each cat and $5.50 per day to care for each dog. Pat noticed that the shelter spent $89.50 caring for cats and dogs on Wednesday. Write an equation to represent the possible numbers of cats and dogs that could have been at the shelter on Wednesday. Pat said that there might have been 8 cats and 14 dogs at the shelter on Wednesday. Are Pat’s numbers possible? Use your equation to justify your answer. Later, Pat found a record showing that there were a total of 22 cats and dogs at the shelter on Wednesday. How many cats were at the shelter on Wednesday?
216 During a snowstorm, a meteorologist tracks the amount of accumulating snow. For the first three hours of the storm, the snow fell at a constant rate of one inch per hour. The storm then stopped for two hours and then started again at a constant rate of one-half inch per hour for the next four hours.

a) On the grid below, draw and label a graph that models the accumulation of snow over time using the data the meteorologist collected.

b) If the snowstorm started at 6 p.m., how much snow had accumulated by midnight?

217 The equation to determine the weekly earnings of an employee at The Hamburger Shack is given by

\[ w(x) = \begin{cases} 10x, & 0 \leq x \leq 40 \\
15(x - 40) + 400, & x > 40 \end{cases} \]

Determine the difference in salary, in dollars, for an employee who works 52 hours versus one who works 38 hours. Determine the number of hours an employee must work in order to earn $445. Explain how you arrived at this answer.

218 The table below lists the total cost for parking for a period of time on a street in Albany, N.Y. The total cost is for any length of time up to and including the hours parked. For example, parking for up to and including 1 hour would cost $1.25; parking for 3.5 hours would cost $5.75.

<table>
<thead>
<tr>
<th>Hours Parked</th>
<th>Total Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.25</td>
</tr>
<tr>
<td>2</td>
<td>2.50</td>
</tr>
<tr>
<td>3</td>
<td>4.00</td>
</tr>
<tr>
<td>4</td>
<td>5.75</td>
</tr>
<tr>
<td>5</td>
<td>7.75</td>
</tr>
<tr>
<td>6</td>
<td>10.00</td>
</tr>
</tbody>
</table>

Graph the step function that represents the cost for the number of hours parked.

Explain how the cost per hour to park changes over the six-hour period.
219 A nutritionist collected information about different brands of beef hot dogs. She made a table showing the number of Calories and the amount of sodium in each hot dog.

<table>
<thead>
<tr>
<th>Calories per Beef Hot Dog</th>
<th>Milligrams of Sodium per Beef Hot Dog</th>
</tr>
</thead>
<tbody>
<tr>
<td>186</td>
<td>495</td>
</tr>
<tr>
<td>181</td>
<td>477</td>
</tr>
<tr>
<td>176</td>
<td>425</td>
</tr>
<tr>
<td>149</td>
<td>322</td>
</tr>
<tr>
<td>184</td>
<td>482</td>
</tr>
<tr>
<td>190</td>
<td>587</td>
</tr>
<tr>
<td>158</td>
<td>370</td>
</tr>
<tr>
<td>139</td>
<td>322</td>
</tr>
</tbody>
</table>

a) Write the correlation coefficient for the line of best fit. Round your answer to the nearest hundredth.

b) Explain what the correlation coefficient suggests in the context of this problem.

220 The volume of a large can of tuna fish can be calculated using the formula $V = \pi r^2 h$. Write an equation to find the radius, $r$, in terms of $V$ and $h$. Determine the diameter, to the nearest inch, of a large can of tuna fish that has a volume of 66 cubic inches and a height of 3.3 inches.

222 A rectangular garden measuring 12 meters by 16 meters is to have a walkway installed around it with a width of $x$ meters, as shown in the diagram below. Together, the walkway and the garden have an area of 396 square meters.

Write an equation that can be used to find $x$, the width of the walkway. Describe how your equation models the situation. Determine and state the width of the walkway, in meters.

223 The table below shows the attendance at a museum in select years from 2007 to 2013.

<table>
<thead>
<tr>
<th>Attendance at Museum</th>
<th>2007</th>
<th>2008</th>
<th>2009</th>
<th>2011</th>
<th>2013</th>
</tr>
</thead>
<tbody>
<tr>
<td>Year</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Attendance (millions)</td>
<td>8.3</td>
<td>8.5</td>
<td>8.5</td>
<td>8.8</td>
<td>9.3</td>
</tr>
</tbody>
</table>

State the linear regression equation represented by the data table when $x = 0$ is used to represent the year 2007 and $y$ is used to represent the attendance. Round all values to the nearest hundredth. State the correlation coefficient to the nearest hundredth and determine whether the data suggest a strong or weak association.

221 A school is building a rectangular soccer field that has an area of 6000 square yards. The soccer field must be 40 yards longer than its width. Determine algebraically the dimensions of the soccer field, in yards.
224 Erica, the manager at Stellarbeans, collected data on the daily high temperature and revenue from coffee sales. Data from nine days this past fall are shown in the table below.

<table>
<thead>
<tr>
<th>High Temperature, t</th>
<th>Day 1</th>
<th>Day 2</th>
<th>Day 3</th>
<th>Day 4</th>
<th>Day 5</th>
<th>Day 6</th>
<th>Day 7</th>
<th>Day 8</th>
<th>Day 9</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>54</td>
<td>50</td>
<td>62</td>
<td>67</td>
<td>70</td>
<td>58</td>
<td>52</td>
<td>46</td>
<td>48</td>
</tr>
<tr>
<td>Coffee Sales, f(t)</td>
<td>$2900</td>
<td>$3080</td>
<td>$2500</td>
<td>$2380</td>
<td>$2200</td>
<td>$2700</td>
<td>$3000</td>
<td>$3620</td>
<td>$3720</td>
</tr>
</tbody>
</table>

State the linear regression function, \( f(t) \), that estimates the day's coffee sales with a high temperature of \( t \). Round all values to the nearest integer. State the correlation coefficient, \( r \), of the data to the nearest hundredth. Does \( r \) indicate a strong linear relationship between the variables? Explain your reasoning.

225 On the set of axes below, graph the function \( y = |x + 1| \).

State the range of the function. State the domain over which the function is increasing.

226 Solve for \( x \) algebraically:
\[ 7x - 3(4x - 8) \leq 6x + 12 - 9x \]
If \( x \) is a number in the interval [4,8], state all integers that satisfy the given inequality. Explain how you determined these values.

227 The formula for the area of a trapezoid is
\[ A = \frac{1}{2} h(b_1 + b_2) \]. Express \( b_1 \) in terms of \( A, h, \) and \( b_2 \). The area of a trapezoid is 60 square feet, its height is 6 ft, and one base is 12 ft. Find the number of feet in the other base.

228 Fred's teacher gave the class the quadratic function \( f(x) = 4x^2 + 16x + 9 \).
   a) State two different methods Fred could use to solve the equation \( f(x) = 0 \).
   b) Using one of the methods stated in part a, solve \( f(x) = 0 \) for \( x \), to the nearest tenth.
229 Albert says that the two systems of equations shown below have the same solutions.

<table>
<thead>
<tr>
<th>First System</th>
<th>Second System</th>
</tr>
</thead>
<tbody>
<tr>
<td>$8x + 9y = 48$</td>
<td>$8x + 9y = 48$</td>
</tr>
<tr>
<td>$12x + 5y = 21$</td>
<td>$-8.5y = -51$</td>
</tr>
</tbody>
</table>

Determine and state whether you agree with Albert. Justify your answer.

230 The graph of an inequality is shown below.

a) Write the inequality represented by the graph.

b) On the same set of axes, graph the inequality $x + 2y < 4$.

c) The two inequalities graphed on the set of axes form a system. Oscar thinks that the point $(2,1)$ is in the solution set for this system of inequalities. Determine and state whether you agree with Oscar. Explain your reasoning.

231 Use the data below to write the regression equation ($y = ax + b$) for the raw test score based on the hours tutored. Round all values to the nearest hundredth.

<table>
<thead>
<tr>
<th>Tutor Hours, $x$</th>
<th>Raw Test Score</th>
<th>Residual (Actual – Predicted)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>30</td>
<td>1.3</td>
</tr>
<tr>
<td>2</td>
<td>37</td>
<td>1.9</td>
</tr>
<tr>
<td>3</td>
<td>35</td>
<td>-6.4</td>
</tr>
<tr>
<td>4</td>
<td>47</td>
<td>-0.7</td>
</tr>
<tr>
<td>5</td>
<td>56</td>
<td>2.0</td>
</tr>
<tr>
<td>6</td>
<td>67</td>
<td>6.6</td>
</tr>
<tr>
<td>7</td>
<td>62</td>
<td>-4.7</td>
</tr>
</tbody>
</table>

Equation: ___________________________

Create a residual plot on the axes below, using the residual scores in the table above.

Based on the residual plot, state whether the equation is a good fit for the data. Justify your answer.
232 An on-line electronics store must sell at least $2500 worth of printers and computers per day. Each printer costs $50 and each computer costs $500. The store can ship a maximum of 15 items per day. On the set of axes below, graph a system of inequalities that models these constraints.

Determine a combination of printers and computers that would allow the electronics store to meet all of the constraints. Explain how you obtained your answer.

233 A contractor has 48 meters of fencing that he is going to use as the perimeter of a rectangular garden. The length of one side of the garden is represented by $x$, and the area of the garden is 108 square meters. Determine, algebraically, the dimensions of the garden in meters.

234 About a year ago, Joey watched an online video of a band and noticed that it had been viewed only 843 times. One month later, Joey noticed that the band’s video had 1708 views. Joey made the table below to keep track of the cumulative number of views the video was getting online.

<table>
<thead>
<tr>
<th>Months Since First Viewing</th>
<th>Total Views</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>843</td>
</tr>
<tr>
<td>1</td>
<td>1708</td>
</tr>
<tr>
<td>2</td>
<td>forgot to record</td>
</tr>
<tr>
<td>3</td>
<td>7124</td>
</tr>
<tr>
<td>4</td>
<td>14,664</td>
</tr>
<tr>
<td>5</td>
<td>29,787</td>
</tr>
<tr>
<td>6</td>
<td>62,581</td>
</tr>
</tbody>
</table>

a) Write a regression equation that best models these data. Round all values to the nearest hundredth. Justify your choice of regression equation. b) As shown in the table, Joey forgot to record the number of views after the second month. Use the equation from part a to estimate the number of full views of the online video that Joey forgot to record.
A nutritionist collected information about different brands of beef hot dogs. She made a table showing the number of Calories and the amount of sodium in each hot dog.

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<td>322</td>
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a) Write the correlation coefficient for the line of best fit. Round your answer to the nearest hundredth.

b) Explain what the correlation coefficient suggests in the context of this problem.

Let \( f(x) = -2x^2 \) and \( g(x) = 2x - 4 \). On the set of axes below, draw the graphs of \( y = f(x) \) and \( y = g(x) \).

Using this graph, determine and state all values of \( x \) for which \( f(x) = g(x) \).
At an office supply store, if a customer purchases fewer than 10 pencils, the cost of each pencil is $1.75. If a customer purchases 10 or more pencils, the cost of each pencil is $1.25. Let \( c \) be a function for which \( c(x) \) is the cost of purchasing \( x \) pencils, where \( x \) is a whole number.

\[
c(x) = \begin{cases} 
1.75x, & \text{if } 0 \leq x \leq 9 \\
1.25x, & \text{if } x \geq 10
\end{cases}
\]

Create a graph of \( c \) on the axes below.

A customer brings 8 pencils to the cashier. The cashier suggests that the total cost to purchase 10 pencils would be less expensive. State whether the cashier is correct or incorrect. Justify your answer.
238 Edith babysits for $x$ hours a week after school at a job that pays $4$ an hour. She has accepted a job that pays $8$ an hour as a library assistant working $y$ hours a week. She will work both jobs. She is able to work no more than $15$ hours a week, due to school commitments. Edith wants to earn at least $80$ a week, working a combination of both jobs. Write a system of inequalities that can be used to represent the situation. Graph these inequalities on the set of axes below.

239 A local business was looking to hire a landscaper to work on their property. They narrowed their choices to two companies. Flourish Landscaping Company charges a flat rate of $120$ per hour. Green Thumb Landscapers charges $70$ per hour plus a $1600$ equipment fee. Write a system of equations representing how much each company charges. Determine and state the number of hours that must be worked for the cost of each company to be the same. [The use of the grid below is optional.] If it is estimated to take at least $35$ hours to complete the job, which company will be less expensive? Justify your answer.
240 The Reel Good Cinema is conducting a mathematical study. In its theater, there are 200 seats. Adult tickets cost $12.50 and child tickets cost $6.25. The cinema's goal is to sell at least $1500 worth of tickets for the theater. Write a system of linear inequalities that can be used to find the possible combinations of adult tickets, \( x \), and child tickets, \( y \), that would satisfy the cinema's goal. Graph the solution to this system of inequalities on the set of axes below. Label the solution with an \( S \). Marta claims that selling 30 adult tickets and 80 child tickets will result in meeting the cinema's goal. Explain whether she is correct or incorrect, based on the graph drawn.
241 A football player attempts to kick a football over a goal post. The path of the football can be modeled by the function \( h(x) = -\frac{1}{225} x^2 + \frac{2}{3} x \), where \( x \) is the horizontal distance from the kick, and \( h(x) \) is the height of the football above the ground, when both are measured in feet. On the set of axes below, graph the function \( y = h(x) \) over the interval \( 0 \leq x \leq 150 \).

Determine the vertex of \( y = h(x) \). Interpret the meaning of this vertex in the context of the problem. The goal post is 10 feet high and 45 yards away from the kick. Will the ball be high enough to pass over the goal post? Justify your answer.

242 A company is considering building a manufacturing plant. They determine the weekly production cost at site \( A \) to be \( A(x) = 3x^2 \) while the production cost at site \( B \) is \( B(x) = 8x + 3 \), where \( x \) represents the number of products, in hundreds, and \( A(x) \) and \( B(x) \) are the production costs, in hundreds of dollars. Graph the production cost functions on the set of axes below and label them site \( A \) and site \( B \).

State the positive value(s) of \( x \) for which the production costs at the two sites are equal. Explain how you determined your answer. If the company plans on manufacturing 200 products per week, which site should they use? Justify your answer.
243 A rectangular picture measures 6 inches by 8 inches. Simon wants to build a wooden frame for the picture so that the framed picture takes up a maximum area of 100 square inches on his wall. The pieces of wood that he uses to build the frame all have the same width. Write an equation or inequality that could be used to determine the maximum width of the pieces of wood for the frame Simon could create. Explain how your equation or inequality models the situation. Solve the equation or inequality to determine the maximum width of the pieces of wood used for the frame to the nearest tenth of an inch.

244 New Clarendon Park is undergoing renovations to its gardens. One garden that was originally a square is being adjusted so that one side is doubled in length, while the other side is decreased by three meters. The new rectangular garden will have an area that is 25% more than the original square garden. Write an equation that could be used to determine the length of a side of the original square garden. Explain how your equation models the situation. Determine the area, in square meters, of the new rectangular garden.

245 Next weekend Marnie wants to attend either carnival A or carnival B. Carnival A charges $6 for admission and an additional $1.50 per ride. Carnival B charges $2.50 for admission and an additional $2 per ride.

a) In function notation, write \( A(x) \) to represent the total cost of attending carnival A and going on \( x \) rides. In function notation, write \( B(x) \) to represent the total cost of attending carnival B and going on \( x \) rides.

b) Determine the number of rides Marnie can go on such that the total cost of attending each carnival is the same. [Use of the set of axes below is optional.]

c) Marnie wants to go on five rides. Determine which carnival would have the lower total cost. Justify your answer.
Algebra I Common Core State Standards Multiple Choice Regents Exam Questions
Answer Section

1  ANS:  2
   \[ 0 = -16t^2 + 144 \]
   \[ 16t^2 = 144 \]
   \[ t^2 = 9 \]
   \[ t = 3 \]

REF:  081423ai  NAT:  F.IF.5  TOP:  Domain and Range

2  ANS:  2
   \[(x + 4)(x + 6) = 0\]
   \[x^2 + 10x + 24 = 0\]

REF:  spr1303ai  NAT:  A.APR.3  TOP:  Zeros of Polynomials

3  ANS:  1

REF:  011524ai  NAT:  A.APR.3  TOP:  Zeros of Polynomials

4  ANS:  4
   \[3(x^2 - 4x + 4) - 2x + 2 = 3x^2 - 12x + 12 - 2x + 2 = 3x^2 - 14x + 14\]

REF:  081524ai  NAT:  A.APR.1  TOP:  Operations with Polynomials
   KEY:  multiplication

5  ANS:  2
   \[x^2 - 2x - 8 = \frac{1}{4}x - 1\]
   \[4x^2 - 8x - 32 = x - 4\]
   \[4x^2 - 9x - 28 = 0\]
   \[(4x + 7)(x - 4) = 0\]
   \[x = \frac{-7}{4}, 4\]

REF:  081517ai  NAT:  A.REI.11  TOP:  Quadratic-Linear Systems

6  ANS:  3
   REF:  061522ai  NAT:  F.BF.2  TOP:  Sequences

7  ANS:  3
   REF:  081410ai  NAT:  F.LE.2  TOP:  Families of Functions
   KEY:  bimodalgraph

8  ANS:  2
   REF:  061517ai  NAT:  A.SSE.1  TOP:  Modeling Exponential Functions

9  ANS:  2
   \[2(3x - y = 4)\]
   \[6x - 2y = 8\]

REF:  061414ai  NAT:  A.REI.5  TOP:  Solving Linear Systems
10 ANS: 1
\[ V = \frac{1}{3} \pi r^2 h \]
\[ 3V = \pi r^2 h \]
\[ \frac{3V}{\pi h} = r^2 \]
\[ \sqrt{\frac{3V}{\pi h}} = r \]

REF: 061423ai NAT: A.CED.4 TOP: Transforming Formulas

11 ANS: 2
\[ f(0 + 1) = -2f(0) + 3 = -2(2) + 3 = -1 \]
\[ f(1 + 1) = -2f(1) + 3 = -2(-1) + 3 = 5 \]

KEY: bimodalgraph

12 ANS: 3
\[ a + p = 165 \quad 1.75(165 - p) + 2.5p = 337.5 \]
\[ 1.75a + 2.5p = 337.5 \quad 288.75 - 1.75p + 2.5p = 337.5 \]
\[ 0.75p = 48.75 \]
\[ p = 65 \]

REF: 061506ai NAT: A.CED.3 TOP: Modeling Linear Systems

13 ANS: 3
\[ x^2 + 6x = 7 \]
\[ x^2 + 6x + 9 = 7 + 9 \]
\[ (x + 3)^2 = 16 \]

REF: 011517ai NAT: A.REI.4 TOP: Solving Quadratics
KEY: completing the square

14 ANS: 4
\[ x = (x - 3)(x + 2)(x - 1) \]

REF: 061512ai NAT: A.APR.3 TOP: Zeros of Polynomials
17 ANS: 1
\[ 2x^2 - 4x - 6 = 0 \]
\[ 2(x^2 - 2x - 3) = 0 \]
\[ 2(x - 3)(x + 1) = 0 \]
\[ x = 3, -1 \]

REF: 011609ai  NAT: A.SSE.3  TOP: Solving Quadratics
KEY: zeros of polynomials

18 ANS: 2  REF: 061403ai  NAT: A.APR.1  TOP: Operations with Polynomials
KEY: subtraction

19 ANS: 3
\[ 119.67(0.61)^5 - 119.67(0.61)^3 \approx 17.06 \]

REF: 011603ai  NAT: F.IF.2  TOP: Evaluating Functions

20 ANS: 1
\[ 4x - 5(0) = 40 \]
\[ 4x = 40 \]
\[ x = 10 \]

REF: 081408ai  NAT: F.IF.4  TOP: Graphing Linear Functions

21 ANS: 3  REF: 011522ai  NAT: A.SSE.2  TOP: Factoring the Difference of Perfect Squares

22 ANS: 2  REF: 061404ai  NAT: A.REI.12  TOP: Graphing Systems of Linear Inequalities
KEY: bimodalgraph | graph

23 ANS: 3
\[ \sqrt{16} + \sqrt{9} = \frac{7}{1} \] may be expressed as the ratio of two integers.

REF: 061413ai  NAT: N.RN.3  TOP: Classifying Numbers

24 ANS: 3  REF: 081403ai  NAT: A.REI.4  TOP: Solving Quadratics
KEY: taking square roots

25 ANS: 1  REF: 081401ai  NAT: N.RN.3  TOP: Classifying Numbers

26 ANS: 3  REF: 081509ai  NAT: A.SSE.2  TOP: Factoring Polynomials

27 ANS: 2  REF: 011506ai  NAT: F.IF.5  TOP: Domain and Range

28 ANS: 3  REF: 061409ai  NAT: F.IF.4  TOP: Graphing Quadratic Functions

29 ANS: 2  REF: 011512ai  NAT: F.BF.3  TOP: Graphing Quadratic Functions

30 ANS: 1  REF: 061507ai  NAT: F.IF.7  TOP: Graphing Step Functions
KEY: bimodalgraph

31 ANS: 3  REF: 061407ai  NAT: F.LE.5  TOP: Modeling Linear Functions

32 ANS: 1
\[ A: \bar{x} = 6; \sigma_x = 3.16 \]
\[ B: \bar{x} = 6.875; \sigma_x = 3.06 \]

REF: 081519ai  NAT: S.ID.2  TOP: Central Tendency and Dispersion

33 ANS: 2  REF: 061424ai  NAT: F.LE.2  TOP: Sequences
34 ANS: 2
\[ x^2 + 4x = 16 \]
\[ x^2 + 4x + 4 = 16 + 4 \]
\[ (x + 2)^2 = 20 \]
\[ x + 2 = \pm \sqrt{4 \cdot 5} \]
\[ = -2 \pm 2\sqrt{5} \]

REF: 061410ai NAT: A.REI.4 TOP: Solving Quadratics
KEY: completing the square

35 ANS: 1
REF: 061521ai NAT: A.REI.4 TOP: Solving Quadratics
KEY: taking square roots

36 ANS: 1
REF: 011604ai NAT: N.RN.3 TOP: Classifying Numbers

37 ANS: 3
\[ \sqrt{\frac{2 \left( \frac{1}{2} \right) + 3}{6 \left( \frac{1}{2} \right) - 5}} = \frac{\sqrt{4}}{-2} = \frac{2}{-2} = -1 \]

REF: 081512ai NAT: F.IF.2 TOP: Functional Notation

38 ANS: 4
\[ (x + 2)^2 - 25 = 0 \]
\[ ((x + 2) + 5)((x + 2) - 5) = 0 \]
\[ x = -7, 3 \]

REF: 081418ai NAT: A.APR.3 TOP: Zeros of Polynomials

39 ANS: 2
REF: 081501ai NAT: F.BF.3 TOP: Graphing Linear Functions

40 ANS: 3
For a residual plot, there should be no observable pattern and a similar distribution of residuals above and below the x-axis.

REF: 011624ai NAT: S.ID.6 TOP: Correlation Coefficient and Residuals

41 ANS: 4
\[ y + 3 = 6(0) \]
\[ y = -3 \]

REF: 011509ai NAT: F.IF.4 TOP: Graphing Linear Functions

42 ANS: 1
REF: 081417ai NAT: F.BF.3 TOP: Graphing Quadratic Functions

43 ANS: 3
REF: 011618ai NAT: F.LE.2 TOP: Sequences

44 ANS: 1
REF: 011504ai NAT: F.BF.1 TOP: Modeling Exponential Functions

45 ANS: 2
REF: 011605ai NAT: A.REI.12 TOP: Graphing Linear Inequalities

46 ANS: 4
REF: 081508ai NAT: A.CED.3 TOP: Modeling Linear Equations
47 ANS: 1  REF: 081514ai  NAT: F.LE.2  TOP: Sequences

48 ANS: 4

\[ 16^{2t} = n^{4t} \]
\[ 16^2 = n^4 \]
\[ 256 = n^4 \]
\[ 4 = n \]

REF: 011519ai  NAT: A.SSE.3  TOP: Exponential Equations

49 ANS: 1

\[ x^2 - 6x = 19 \]
\[ x^2 - 6x + 9 = 19 + 9 \]
\[ (x - 3)^2 = 28 \]
\[ x - 3 = \pm \sqrt{4 \cdot 7} \]
\[ x = 3 \pm 2\sqrt{7} \]

REF: fall1302ai  NAT: A.REI.4  TOP: Solving Quadratics
KEY: quadratic formula

50 ANS: 3
Median remains at 1.4.

REF: 061520ai  NAT: S.ID.3  TOP: Central Tendency and Dispersion
KEY: outliers

51 ANS: 2

\[ P(x) = -0.5x^2 + 800x - 100 - (300x + 250) = -0.5x^2 + 500x - 350 \]

REF: 081406ai  NAT: A.APR.1  TOP: Operations with Polynomials
KEY: functional notation

52 ANS: 4  REF: 061509ai  NAT: F.IF.2  TOP: Domain and Range
KEY: graph

53 ANS: 1  REF: 081504ai  NAT: A.APR.3  TOP: Zeros of Polynomials

54 ANS: 2  REF: 061503ai  NAT: A.SSE.2  TOP: Factoring the Difference of Perfect Squares
55 ANS: 3

\[ h(x) = -x^2 + x + 6 \quad \text{Maximum of } f(x) = 9 \quad k(x) = -5x^2 - 12x + 4 \quad \text{Maximum of } g(x) < 5 \]

\[ x = \frac{-1}{2(-1)} = \frac{1}{2} \quad \quad \quad x = \frac{12}{2(-5)} = -\frac{6}{5} \]

\[ y = -\left(\frac{1}{2}\right)^2 + \frac{1}{2} + 6 \quad \quad \quad y = -5\left(-\frac{6}{5}\right)^2 - 12\left(-\frac{6}{5}\right) + 4 \]

\[ = \frac{1}{4} + \frac{2}{4} + 6 \quad \quad \quad = \frac{36}{5} + \frac{72}{5} + \frac{20}{5} \]

\[ = 6\frac{1}{4} \quad \quad \quad = 11\frac{1}{5} \]

REF: 061514ai NAT: F.IF.9 TOP: Comparing Functions

56 ANS: 4

\[ f(1) = 3; f(2) = -5; f(3) = 11; f(4) = -21; f(5) = 43 \]

REF: 081424ai NAT: F.IF.3 TOP: Sequences

57 ANS: 3

<table>
<thead>
<tr>
<th>Semester 1</th>
<th>Mean</th>
<th>Q1</th>
<th>Median</th>
<th>Q3</th>
<th>IQR</th>
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<tr>
<td></td>
<td>86.8</td>
<td>80.5</td>
<td>88</td>
<td>92.5</td>
<td>12</td>
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<tr>
<td>Semester 2</td>
<td>87</td>
<td>80</td>
<td>88</td>
<td>92</td>
<td>12</td>
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</table>

REF: 061419ai NAT: S.ID.2 TOP: Central Tendency and Dispersion

58 ANS: 2

REF: 061416ai NAT: A.CED.1 TOP: Modeling Linear Equations

59 ANS: 3

REF: 081523ai NAT: A.REI.4 TOP: Solving Quadratics

KEY: taking square roots

60 ANS: 3

REF: 061501ai NAT: F.LE.5 TOP: Modeling Linear Functions

61 ANS: 4

REF: 061422ai NAT: A.CED.3 TOP: Modeling Linear Equations

62 ANS: 1

\[ \frac{0.8(10^2) - 0.8(5^2)}{10 - 5} = \frac{80 - 20}{5} = 12 \]

REF: 011521ai NAT: F.IF.6 TOP: Rate of Change

63 ANS: 2

(4,3) is on the boundary of \( y > -\frac{1}{2} x + 5 \), so (4,3) is not a solution of the system.

REF: fall1301ai NAT: A.REI.12 TOP: Graphing Systems of Linear Inequalities

KEY: solution set

64 ANS: 4

REF: 061417ai NAT: F.IF.2 TOP: Domain and Range

KEY: real domain, linear

65 ANS: 3

REF: 061412ai NAT: A.SSE.3 TOP: Solving Quadratics

KEY: zeros of polynomials
1) \( \frac{g(1)-g(-1)}{1-(-1)} = \frac{4-6}{2} = \frac{-2}{2} = -1 \)

2) \( g(0) = 6 \)

3) \( x = \frac{-(1)}{2(-1)} = \frac{-1}{2} \)

4) \( n(1) - n(-1) = \frac{9-5}{2} = \frac{4}{2} = 2 \)

\( x = 1; n(1) = 9 \)

4) \( g: S = \frac{-(1)}{-1} = -1 \)

\( n: S = -2 + 4 = 2 \)

A correlation coefficient close to –1 or 1 indicates a good fit. For a residual plot, there should be no observable pattern and a similar distribution of residuals above and below the \( x \)-axis.
\[
\frac{750 + 2.25p}{p} > 2.75 \quad \frac{750 + 2.25p}{p} < 3.25
\]
\[
750 + 2.25p > 2.75p \quad 750 + 2.25p < 3.25p
\]
\[
750 > 50p \quad 750 < p
\]
\[
1500 > p
\]

ANS: 4

\[
d = \frac{1}{2}at^2
\]
\[
2d = at^2
\]
\[
\frac{2d}{a} = t^2
\]
\[
\sqrt{\frac{2d}{a}} = t
\]

ANS: 2

\[
(1) \quad \frac{6 - 1}{1971 - 1898} = \frac{5}{73} \approx .07
\]
\[
(2) \quad \frac{14 - 6}{1985 - 1971} = \frac{8}{14} \approx .57
\]
\[
(3) \quad \frac{24 - 14}{2006 - 1985} = \frac{10}{21} \approx .48
\]
\[
(4) \quad \frac{35 - 24}{2012 - 2006} = \frac{11}{6} \approx 1.83
\]

ANS: 4

\[
\frac{110 - 40}{2 - 1} > \frac{350 - 230}{8 - 6}
\]
\[
70 > 60
\]

ANS: 1

\[
f(2) = 0
\]
\[
f(6) = 8
\]

ANS: 1

\[
110 - 40 > 350 - 230
\]
\[
2 - 1 > 8 - 6
\]
\[
70 > 60
\]

ANS: 1

\[
f(2) = 0
\]
\[
f(6) = 8
\]

ANS: 2

\[
f(2) = 0
\]
\[
f(6) = 8
\]
83  \[ \frac{36.6 - 15}{4 - 0} = \frac{21.6}{4} = 5.4 \]

REF: 061511ai  NAT: F.IF.6  TOP: Rate of Change

84  \[ \frac{1}{\sqrt{4}} + \frac{1}{\sqrt{9}} = \frac{1}{2} + \frac{1}{3} = \frac{5}{6} \]

REF: 081522ai  NAT: N.RN.3  TOP: Classifying Numbers

85  \[ f(-1) < g(-1) \]
\[ 3^{-1} < 2(-1) + 5 \]
\[ \frac{1}{3} < 3 \]

REF: 061515ai  NAT: F.LE.3  TOP: Families of Functions

86  \[ 5x^2 - (4x^2 - 12x + 9) = x^2 + 12x - 9 \]

REF: 011610ai  NAT: A.APR.1  TOP: Operations with Polynomials
KEY: multiplication

87  ANS: 4  REF: 081419ai  NAT: A.CED.3  TOP: Modeling Linear Systems

88  ANS: 2  REF: 061513ai  NAT: F.LE.2  TOP: Families of Functions

89  ANS: 1  REF: 061420ai  NAT: F.IF.2  TOP: Functional Notation

90  ANS: 3  REF: 061504ai  NAT: F.IF.1  TOP: Defining Functions
KEY: ordered pairs

91  ANS: 2  REF: 081511ai  NAT: F.IF.1  TOP: Defining Functions
KEY: mixed

92  ANS: 1
\[ \frac{7}{3} \left( x + \frac{9}{28} \right) = 20 \]
\[ \frac{7}{3} x + \frac{3}{4} = \frac{80}{4} \]
\[ \frac{7}{3} x = \frac{77}{4} \]
\[ x = \frac{33}{4} = 8.25 \]

REF: 061405ai  NAT: A.REI.3  TOP: Solving Linear Equations
KEY: fractional expressions

93  ANS: 4  REF: 081505ai  NAT: A.CED.1  TOP: Modeling Linear Inequalities
\[ m = \frac{11 - 1}{3 - (-2)} = \frac{10}{5} = 2 \quad y = mx + b \quad y = 2x + 5 \]
\[ 11 = 2(3) + b \quad 9 = 2(2) + 5 \]
\[ 5 = b \]

**ANS:** 4
**REF:** 011511ai  **NAT:** A.REI.10  **TOP:** Identifying Solutions

**ANS:** 2  **REF:** 011502ai  **NAT:** N.Q.1  **TOP:** Conversions
**KEY:** dimensional analysis

There are no negative or fractional cars.

**ANS:** 4  **REF:** 061402ai  **NAT:** F.IF.5  **TOP:** Domain and Range

**ANS:** 4  **REF:** 011523ai  **NAT:** F.BF.1  **TOP:** Modeling Linear Functions

**ANS:** 3  **REF:** 081412ai  **NAT:** F.LE.1  **TOP:** Families of Functions

**ANS:** 2  **REF:** 081422ai  **NAT:** F.IF.7  **TOP:** Graphing Piecewise-Defined Functions

**ANS:** 2
\[ x^2 - 8x = 7 \]
\[ x^2 - 8x + 16 = 7 + 16 \]
\[ (x - 4)^2 = 23 \]

**ANS:** 4  **REF:** 011614ai  **NAT:** A.REI.4  **TOP:** Solving Quadratics
**KEY:** completing the square

\[ \frac{1}{2} x + 3 = |x| \quad -\frac{1}{2} x - 3 = x \]
\[ \frac{1}{2} x + 3 = x \quad -x - 6 = 2x \]
\[ x + 6 = 2x \quad -2 = x \]
\[ 6 = x \]

**ANS:** 1  **REF:** 011617ai  **NAT:** A.REI.11  **TOP:** Other Systems

**ANS:** 4  **REF:** 081421ai  **NAT:** S.ID.6  **TOP:** Regression
**KEY:** linear

**ANS:** 4  **REF:** 061421ai  **NAT:** F.BF.2  **TOP:** Sequences
104 ANS: 4
\[ y - 34 = x^2 - 12x \]
\[ y = x^2 - 12x + 34 \]
\[ y = x^2 - 12x + 36 - 2 \]
\[ y = (x - 6)^2 - 2 \]

REF: 011607ai NAT: A.REI.4 TOP: Solving Quadratics
KEY: completing the square

105 ANS: 3
\[ x^2 - 8x + 16 = 24 + 16 \]
\[ (x - 4)^2 = 40 \]
\[ x - 4 = \pm \sqrt{40} \]
\[ x = 4 \pm 2\sqrt{10} \]

REF: 061523ai NAT: A.REI.4 TOP: Solving Quadratics
KEY: completing the square

106 ANS: 1
\[ x^2 - 13x - 30 = 0 \]
\[ (x - 15)(x + 2) = 0 \]
\[ x = 15, -2 \]

REF: 061510ai NAT: A.APR.3 TOP: Zeros of Polynomials

107 ANS: 4
\[ L + S = 20 \]
\[ 27.98L + 10.98(20 - L) = 355.60 \]
\[ 27.98L + 219.60 - 10.98L = 355.60 \]
\[ 17L = 136 \]
\[ L = 8 \]

REF: 081510ai NAT: A.CED.3 TOP: Modeling Linear Systems

108 ANS: 2
REF: 081416ai NAT: F.LE.2 TOP: Sequences

109 ANS: 4
REF: 081405ai NAT: A.REI.10 TOP: Identifying Solutions

110 ANS: 1
REF: 011615ai NAT: F.IF.5 TOP: Domain and Range

111 ANS: 1
REF: 011620ai NAT: F.BF.3 TOP: Transformations with Functions
KEY: bimodalgraph

112 ANS: 2
REF: 011619ai NAT: F.IF.2 TOP: Domain and Range
KEY: real domain, exponential

113 ANS: 3
REF: 061411ai NAT: S.ID.8 TOP: Correlation Coefficient

114 ANS: 2
REF: 081413ai NAT: A.CED.2 TOP: Graphing Linear Functions
KEY: bimodalgraph
116 116 ANS: 4
\[3x^2 - 3x - 6 = 0\]
\[3(x^2 - x - 2) = 0\]
\[3(x - 2)(x + 1) = 0\]
\[x = 2, -1\]

REF: 081513ai NAT: A.SSE.3 TOP: Solving Quadratics
KEY: zeros of polynomials

117 ANS: 4 REF: spr1304ai NAT: A.CED.1 TOP: Geometric Applications of Quadratics
118 ANS: 2 REF: 011501ai NAT: F.LE.5 TOP: Modeling Linear Functions
119 ANS: 3
15 > 5

REF: 081502ai NAT: A.REI.6 TOP: Graphing Linear Systems

120 ANS: 2 REF: 011602ai NAT: A.CED.2 TOP: Graphing Linear Functions
121 ANS: 1
25,000(0.86)^2 - 25,000(0.86)^3 = 18,490 - 15,901.40 = 2,588.60

REF: 011508ai NAT: F.IF.2 TOP: Functional Notation

122 ANS: 3 REF: 011513ai NAT: A.CED.1 TOP: Modeling Linear Inequalities
123 ANS: 4 REF: 011503ai NAT: A.SSE.3 TOP: Solving Quadratics
KEY: factoring
124 ANS: 2 REF: 011510ai NAT: A.APR.1 TOP: Operations with Polynomials
KEY: multiplication
125 ANS: 2
\[x^2 - 6x = 12\]
\[x^2 - 6x + 9 = 12 + 9\]
\[(x - 3)^2 = 21\]

REF: 061408ai NAT: A.REI.4 TOP: Solving Quadratics
KEY: completing the square

126 ANS: 3 REF: 011505ai NAT: F.LE.1 TOP: Families of Functions
127 ANS: 3 REF: 081409ai NAT: A.CED.1 TOP: Modeling Quadratics
128 ANS: 3 REF: spr1302ai NAT: A.APR.3 TOP: Zeros of Polynomials
129 ANS: 1
\[7 - \frac{2}{3} x < x - 8\]
\[15 < \frac{5}{3} x\]
\[9 < x\]

REF: 011507ai NAT: A.REI.3 TOP: Solving Linear Inequalities

130 ANS: 4 REF: 011608ai NAT: A.SSE.1 TOP: Modeling Exponential Functions
131 ANS: 3     REF: 011606ai     NAT: A.CED.4     TOP: Transforming Formulas
132 ANS: 1     REF: 081407ai     NAT: A.REI.12     TOP: Graphing Systems of Linear Inequalities
133 ANS: 4     REF: 011616ai     NAT: F.LE.2     TOP: Families of Functions
134 ANS: 3     REF: 081506ai     NAT: A.REI.12     TOP: Graphing Systems of Linear Inequalities
135 ANS: 4     REF: 081503ai     NAT: A.SSE.1     TOP: Modeling Expressions
136 ANS: 4     REF: 011514ai     NAT: S.ID.2     TOP: Central Tendency and Dispersion
137 ANS: 3     

<table>
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<tr>
<th>x</th>
<th>$A = 5000x + 10000$</th>
<th>$B = 500(2)^{x-1}$</th>
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<tr>
<td>6</td>
<td>40,000</td>
<td>16,000</td>
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<tr>
<td>7</td>
<td>45,000</td>
<td>32,000</td>
</tr>
<tr>
<td>8</td>
<td>50,000</td>
<td>64,000</td>
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138 ANS: 3     

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<td>8,000</td>
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<tr>
<td>4</td>
<td>mean age</td>
<td>28.25</td>
</tr>
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</table>

139 ANS: 4     

140 ANS: 4     

141 ANS: 4

$\frac{4.7 - 2.3}{20 - 80} = \frac{2.4}{-60} = -0.04.$

142 ANS: 3     

143 ANS: 3     

144 ANS: 4

Over the interval $0 \leq x \leq 3$, the average rate of change for $h(x) = \frac{9 - 2}{3 - 0} = \frac{7}{3}$, $f(x) = \frac{7 - 1}{3 - 0} = \frac{6}{3} = 2$, and $g(x) = \frac{3 - 0}{3 - 0} = \frac{3}{3} = 1$.

145 ANS: 2     

REF: 011611ai     NAT: A.CED.1     TOP: Geometric Applications of Quadratics
\[ x^2 - 5x = -3 \]

\[ x^2 - 5x + \frac{25}{4} = -\frac{12}{4} + \frac{25}{4} \]

\[ \left(x - \frac{5}{2}\right)^2 = \frac{13}{4} \]

REF: 061518ai  NAT: A.REI.4  TOP: Solving Quadratics
KEY: completing the square

147 ANS: 1  REF: 061401ai  NAT: A.REI.1  TOP: Identifying Properties
148 ANS: 3  REF: 011515ai  NAT: F.IF.8  TOP: Modeling Exponential Functions
149 ANS: 3  REF: 081507ai  NAT: F.LE.2  TOP: Modeling Exponential Functions
150 ANS: 2  REF: 061508ai  NAT: N.RN.3  TOP: Classifying Numbers
151 ANS: 1  REF: 061505ai  NAT: A.REI.12  TOP: Graphing Linear Inequalities
Algebra I Common Core State Standards 2 Point Regents Exam Questions
Answer Section

152 ANS:

The line is a poor fit because the residuals form a pattern.

REF: 081431ai   NAT: S.ID.6   TOP: Correlation Coefficient and Residuals

153 ANS:

\[ x^4 + 6x^2 - 7 \]
\[ (x^2 + 7)(x^2 - 1) \]
\[ (x^2 + 7)(x + 1)(x - 1) \]

REF: 061431ai   NAT: A.SSE.2   TOP: Factoring Polynomials

154 ANS:

\[ y^2 - 6y + 9 = 4y - 12 \]
\[ y^2 - 10y + 21 = 0 \]
\[ (y - 7)(y - 3) = 0 \]
\[ y = 7, 3 \]

REF: 011627ai   NAT: A.REI.4   TOP: Solving Quadratics
KEY: factoring

155 ANS:

\[ -3x + 7 - 5x < 15 \]
\[ -8x < 8 \]
\[ x > -1 \]

REF: 061530ai   NAT: A.REI.3   TOP: Interpreting Solutions
156 ANS:

(4, 1). \( f(x - 2) \) is a horizontal shift two units to the right.

REF: 061428ai NAT: F.BF.3 TOP: Graphing Quadratic Functions

157 ANS:

\[ x^2 + 10x + 24 = (x + 4)(x + 6) = (x + 6)(x + 4). \] 6 and 4

REF: 081425ai NAT: A.SSE.3 TOP: Solving Quadratics
KEY: factoring

158 ANS:

\[ A = 600(1.016)^2 \approx 619.35 \]

REF: 061529ai NAT: A.CED.1 TOP: Modeling Exponential Functions

159 ANS:

REF: 081526ai NAT: A.REI.12 TOP: Graphing Linear Inequalities

160 ANS:

\[
(3x^2 - 2x + 5) - (x^2 + 3x - 2) = 2x^2 - 5x + 7
\]

\[
\frac{1}{2} x^2(2x^2 - 5x + 7) = x^4 - \frac{5}{2} x^3 + \frac{7}{2} x^2
\]

REF: 061528ai NAT: A.APR.1 TOP: Operations with Polynomials
KEY: multiplication

161 ANS:

\[ B = 3000(1.042)^t \]

REF: 081426ai NAT: F.BF.1 TOP: Modeling Exponential Functions
162 ANS: 
\[-2x^2 + 6x + 4\]

REF: 011528ai NAT: A.APR.1 TOP: Operations with Polynomials
KEY: subtraction

163 ANS: 
\[-16t^2 + 64t = 0 \quad 0 \leq t \leq 4\] The rocket launches at \(t = 0\) and lands at \(t = 4\)
\[-16(t - 4) = 0\]
\[t = 0, 4\]

REF: 081531ai NAT: F.IF.4 TOP: Graphing Quadratic Functions

164 ANS: 
Linear, because the function has a constant rate of change.

REF: 011625ai NAT: F.LE.1 TOP: Families of Functions

165 ANS: 
6. \(3x + 9 \leq 5x - 3\)
\[12 \leq 2x\]
\[6 \leq x\]

REF: 081430ai NAT: A.REI.3 TOP: Interpreting Solutions

166 ANS: 
\[34 = l \left( \frac{1}{2} l \right)\]
\[68 = l^2\]
\[8.2 \approx l\]
\[4.1 \approx w\]

REF: 061532ai NAT: A.CED.1 TOP: Geometric Applications of Quadratics

167 ANS: 
\[b^2 - 4ac = (-2)^2 - 4(1)(5) = 4 - 20 = -16\] None

REF: 081529ai NAT: A.REI.4 TOP: Using the Discriminant

168 ANS: 

REF: fall1304ai NAT: F.IF.7 TOP: Graphing Root Functions
169 ANS:
\[15x + 36 = 10x + 48\]
\[5x = 12\]
\[x = 2.4\]

REF: 011531ai  NAT: A.CED.1  TOP: Modeling Linear Equations

170 ANS:
\[h(n) = 1.5(n - 1) + 3\]

REF: 081525ai  NAT: F.BF.1  TOP: Modeling Linear Functions

171 ANS:
\[8m^2 + 20m - 12 = 0\]
\[4(2m^2 + 5m - 3) = 0\]
\[(2m - 1)(m + 3) = 0\]
\[m = \frac{1}{2}, -3\]

REF: fall1305ai  NAT: A.SSE.3  TOP: Solving Quadratics
KEY: factoring

172 ANS:
a) \[p + d \leq 800\]
b) \[6(440) + 9d \geq 5000\]
Since \(440 + 263 \leq 800\), it is possible.
\[6p + 9d \geq 5000\]
\[2640 + 9d \geq 5000\]
\[9d \geq 2360\]
\[d \geq 262.2\]

REF: spr1306ai  NAT: A.CED.3  TOP: Modeling Systems of Linear Inequalities

173 ANS:
\[y = 0.05x - 0.92\]

REF: fall1307ai  NAT: S.ID.6  TOP: Regression  KEY: linear

174 ANS:
\[4x^2 - 12x - 7 = 0\]
\[(4x^2 - 14x) + (2x - 7) = 0\]
\[2x(2x - 7) + (2x - 7) = 0\]
\[(2x + 1)(2x - 7) = 0\]
\[x = -\frac{1}{2}, \frac{7}{2}\]

REF: 011529ai  NAT: A.REI.4  TOP: Solving Quadratics
KEY: factoring
Graph A is a good fit because it does not have a clear pattern, whereas Graph B does.

\[ T(d) = 2d + 28 \quad T(6) = 2(6) + 28 = 40 \]

Yes, because every element of the domain is assigned one unique element in the range.

\[(2x^2 + 7x - 10)(x + 5)\]

\[2x^3 + 7x^2 - 10x + 10x^2 + 35x - 50\]

\[2x^3 + 17x^2 + 25x - 50\]

The graph has shifted three units to the right.

The slope represents the amount paid each month and the \(y\)-intercept represents the initial cost of membership.

\[ f(x) = 6.50x + 4(12) \]
ANS:
y = 0.25(2)^x. I inputted the four integral values from the graph into my graphing calculator and determined the exponential regression equation.

REF: 011532ai    NAT: S.ID.6    TOP: Regression    KEY: exponential

ANS:
\[ f(5) = (8) \cdot 2^5 = 256 \quad f(t) = g(t) \]
\[ g(5) = 2^{5+3} = 256 \quad (8) \cdot 2^t = 2^{t+3} \]
\[ 2^3 \cdot 2^t = 2^{t+3} \]
\[ 2^{t+3} = 2^{t+3} \]

REF: 011632ai    NAT: A.SSE.3    TOP: Exponential Equations

ANS:
\[ x^2 + 46 = 60 + 5x \quad \text{John and Sarah will have the same amount of money saved at 7 weeks.} \]
\[ x^2 - 5x - 14 = 0 \]
\[ (x - 7)(x + 2) = 0 \]
\[ x = 7 \]
expressions representing their savings equal to each other and solved for the positive value of \( x \) by factoring.

REF: 061527ai    NAT: A.REI.11    TOP: Quadratic-Linear Systems

ANS:
\[ b(x - 3) \geq ax + 7b \]
\[ bx - 3b \geq ax + 7b \]
\[ bx - ax \geq 10b \]
\[ x(b - a) \geq 10b \]
\[ x \leq \frac{10b}{b-a} \]

REF: 011631ai    NAT: A.REI.3    TOP: Solving Linear Inequalities
g. The maximum of \( f \) is 6. For \( g \), the maximum is 11. \( x = \frac{-b}{2a} = \frac{-4}{2 \left( \frac{1}{2} \right)} = \frac{-4}{-1} = 4 \)

\[ y = \frac{1}{2} (4)^2 + 4(4) + 3 = -8 + 16 + 3 = 11 \]

189 ANS:

\[
\frac{m}{351} = \frac{70}{70 + 35}
\]

105\( m \) = 24570

\[ m = 234 \]

190 ANS:

\[
\frac{1}{2} x^2 - 4 = 0
\]

\[ x^2 - 8 = 0 \]

\[ x^2 = 8 \]

\[ x = \pm 2\sqrt{2} \]

191 ANS:

\[ 12x + 9(2x) + 5(3x) = 15 \left( \frac{1}{3} \right) = 2 \text{ pounds} \]

45\( x \) = 15

\[ x = \frac{1}{3} \]

192 ANS:

[Graph of a function that is not described in the text]
193 ANS:
No, because the relation does not pass the vertical line test.

REF: 011626ai NAT: F.IF.1 TOP: Defining Functions
KEY: graphs

194 ANS:

REF: 081528ai NAT: F.IF.4 TOP: Relating Graphs to Events

195 ANS:
Since \((x + p)^2 = x^2 + 2px + p^2\), \(p\) is half the coefficient of \(x\), and the constant term is equal to \(p^2\). \(\left(\frac{6}{2}\right)^2 = 9\)

REF: 081432ai NAT: A.REI.4 TOP: Solving Quadratics
KEY: completing the square

196 ANS:
\[2(-1) + a(-1) - 7 > -12 \quad a = 2\]
\[-a - 9 > -12\]
\[-a > -3\]
\[a < 3\]

REF: 061427ai NAT: A.REI.3 TOP: Interpreting Solutions

197 ANS:
Exponential, because the function does not grow at a constant rate.

REF: 081527ai NAT: F.LE.1 TOP: Families of Functions

198 ANS:
During 1960-1965 the graph has the steepest slope.

REF: 011628ai NAT: F.IF.6 TOP: Rate of Change

199 ANS:
\[185 + 0.03x = 275 + 0.025x\]
\[0.005x = 90\]
\[x = 18000\]

REF: 081427ai NAT: A.REI.6 TOP: Solving Linear Systems
KEY: substitution
200 ANS:
0.5 represents the rate of decay and 300 represents the initial amount of the compound.

REF: 061426ai NAT: F.LE.5 TOP: Modeling Exponential Functions
201 ANS:
2p + 3d = 18.25 4p + 6d = 36.50 4p + 2(2.25) = 27.50
4p + 2d = 27.50 4p + 2d = 27.50 4p = 23
4d = 9 p = 5.75
d = 2.25

REF: 011533ai NAT: A.CED.3 TOP: Modeling Linear Systems
202 ANS:
y ≥ 2x − 3. Oscar is wrong. (2) + 2(1) < 4 is not true.

REF: 011534ai NAT: A.REI.12 TOP: Graphing Systems of Linear Inequalities
KEY: graph
203 ANS:

REF: 061432ai NAT: S.ID.1 TOP: Box Plots KEY: represent
204 ANS:

REF: 011530ai NAT: F.IF.7 TOP: Graphing Piecewise-Defined Functions
ANS:

\[ 2p + 3d = 18.25 \quad 4p + 6d = 36.50 \quad 4p + 2(2.25) = 27.50 \]

\[ 4p + 2d = 27.50 \quad 4p + 2d = 27.50 \quad 4p = 23 \]

\[ 4d = 9 \quad p = 5.75 \]

\[ d = 2.25 \]

REF: 011533ai      NAT: A.CED.3      TOP: Modeling Linear Systems
Algebra I Common Core State Standards 4 Point Regents Exam Questions
Answer Section

206 ANS:
\[ m(x) = (3x - 1)(3 - x) + 4x^2 + 19 \quad x^2 + 10x + 16 = 0 \]
\[ m(x) = 9x - 3x^2 - 3 + x + 4x^2 + 19 \quad (x + 8)(x + 2) = 0 \]
\[ m(x) = x^2 + 10x + 16 \quad x = -8, -2 \]

REF: 061433ai NAT: A.REI.4 TOP: Solving Quadratics
KEY: factoring

207 ANS:
y = 80(1.5)^x \quad 80(1.5)^{26} = 3,030,140. No, because the prediction at \( x = 52 \) is already too large.

REF: 061536ai NAT: S.ID.6 TOP: Regression KEY: exponential

208 ANS:
\[ 8x + 11y \geq 200 \quad 8x + 11(15) \geq 200 \]
\[ 8x + 165 \geq 200 \]
\[ 8x \geq 35 \]
\[ x \geq 4.375 \]
\[ 5 \text{ hours} \]

REF: fall1309ai NAT: A.CED.3 TOP: Modeling Linear Inequalities

209 ANS:
The vertex represents a maximum since \( a < 0 \).
\[ f(x) = -x^2 + 8x + 9 \]
\[ = -(x^2 - 8x - 9) \]
\[ = -(x^2 - 8x + 16) + 9 + 16 \]
\[ = -(x - 4)^2 + 25 \]

REF: 011536ai NAT: F.IF.8 TOP: Vertex Form of a Quadratic
210 ANS:

\[ C(x) = \frac{10}{3}x \]
\[ 180 = \frac{10}{3}x \]
\[ 540 = 10x \]
\[ 54 = x \]

REF: fall1308ai  NAT: A.CED.2  TOP: Graphing Linear Functions

211 ANS:

\[ t = \frac{-b}{2a} = \frac{-64}{2(-16)} = \frac{-64}{-32} = 2 \text{ seconds}. \]
The height decreases after reaching its maximum at \( t = 2 \) until it lands at
\[ t = 5 \]
\[ -16t^2 + 64t + 80 = 0 \]
\[ t^2 - 4t - 5 = 0 \]
\[ (t - 5)(t + 1) = 0 \]
\[ t = 5 \]

REF: 011633ai  NAT: F.IF.4  TOP: Graphing Quadratic Functions

212 ANS:

\[ g(x) \text{ has a greater value: } 2^{20} > 2^2 \]

REF: 081533ai  NAT: F.LE.3  TOP: Families of Functions

213 ANS:

\[ A(n) = 175 - 2.75n \]
\[ 0 = 175 - 2.75n \]
\[ 2.75n = 175 \]
\[ n = 63.6 \]

REF: 061435ai  NAT: F.BF.1  TOP: Modeling Linear Functions
214 ANS:

\[
\text{2 down. 4 right.}
\]

REF: 081433ai  NAT: F.BF.3  TOP: Graphing Absolute Value Functions

215 ANS:

\[
c + d = 22
\]

\[
18.80 + 77.00 \neq 89.50 \quad 2.35c + 5.50(22 - c) = 89.50
\]

\[
95.80 \neq 89.50 \quad 2.35c + 121 - 5.50c = 89.50
\]

\[
-3.15c = -31.50
\]

\[
c = 10
\]

REF: 061436ai  NAT: A.CED.3  TOP: Modeling Linear Systems

216 ANS:

\[
\text{At 6 hours, } \frac{31}{2} \text{ inches of snow have fallen.}
\]

REF: spr1307ai  NAT: F.IF.4  TOP: Relating Graphs to Events

217 ANS:

\[
w(52) - w(38) = 445\quad 15(x - 40) + 400 = 445 \quad \text{Since } w(x) > 400, x > 40. \quad \text{I substituted 445 for } w(x) \text{ and solved}
\]

\[
15(52 - 40) + 400 - 10(38) = 45
\]

\[
180 + 400 - 380 = x - 40 = 3
\]

\[
200 = x = 43
\]

for x.

REF: 061534ai  NAT: F.IF.2  TOP: Functional Notation
The cost for each additional hour increases after the first 2 hours.

REF:  fall1311ai    NAT:  F.IF.7    TOP:  Graphing Step Functions

219 ANS:

$r \approx 0.94$. The correlation coefficient suggests that as calories increase, so does sodium.

REF:  011535ai    NAT:  S.ID.8    TOP:  Correlation Coefficient

220 ANS:

\[
\frac{V}{\pi h} = \frac{\pi r^2 h}{\pi h} = d = 2\sqrt{\frac{66}{3.3\pi}} \approx 5
\]

\[
\frac{V}{\pi h} = r^2
\]

\[
\sqrt{\frac{V}{\pi h}} = r
\]

REF:  081535ai    NAT:  A.CED.4    TOP:  Transforming Formulas

221 ANS:

\[
w(w + 40) = 6000
\]

\[
w^2 + 40w - 6000 = 0
\]

\[(w + 100)(w - 60) = 0
\]

\[w = 60, l = 100
\]

REF:  081436ai    NAT:  A.CED.1    TOP:  Geometric Applications of Quadratics
222 ANS:
$(2x + 16)(2x + 12) = 396$. The length, $2x + 16$, and the width, $2x + 12$, are multiplied and set equal to the area.

$(2x + 16)(2x + 12) = 396$

$4x^2 + 24x + 32x + 192 = 396$

$4x^2 + 56x - 204 = 0$

$x^2 + 14x - 51 = 0$

$(x + 17)(x - 3) = 0$

$x = 3 = \text{width}$

REF: 061434ai NAT: A.CED.1 TOP: Geometric Applications of Quadratics

223 ANS:
$y = 0.16x + 8.27 \quad r = 0.97$, which suggests a strong association.

REF: 081536ai NAT: S.ID.6 TOP: Regression KEY: linear

224 ANS:
$f(t) = -58t + 6182 \quad r = -0.94$ This indicates a strong linear relationship because $r$ is close to -1.

REF: 011635ai NAT: S.ID.6 TOP: Regression KEY: linear

225 ANS:

Range: $y \geq 0$. The function is increasing for $x > -1$.

REF: fall1310ai NAT: F.IF.7 TOP: Graphing Absolute Value Functions

226 ANS:
$7x - 3(4x - 8) \leq 6x + 12 - 9x \quad 6, 7, 8$ are the numbers greater than or equal to 6 in the interval.

$7x - 12x + 24 \leq -3x + 12$

$-5x + 24 \leq -3x + 12$

$12 \leq 2x$

$6 \leq x$

REF: 081534ai NAT: A.REI.3 TOP: Interpreting Solutions
ANS: \[ A = \frac{1}{2} h(b_1 + b_2), \quad b_1 = \frac{2(60)}{6} - 12 = 20 - 12 = 8 \]
\[ \frac{24}{h} = b_1 + b_2 \]
\[ \frac{24}{h} - b_2 = b_1 \]

REF: 081434ai  NAT: A.CED.4  TOP: Transforming Formulas

ANS: Two of the following: quadratic formula, complete the square, factor by grouping or graphically.
\[ x = \frac{-16 \pm \sqrt{16^2 - 4(4)(9)}}{2(4)} = \frac{-16 \pm \sqrt{112}}{8} \approx -0.7, -3.3 \]

REF: 011634ai  NAT: A.REI.4  TOP: Solving Quadratics
KEY: quadratic formula

ANS: \[
\begin{align*}
24x + 27y &= 144 \\
-8.5y &= -51
\end{align*}
\]
Agree, as both systems have the same solution.
\[
\begin{align*}
24x + 10y &= 42 \\
17y &= 102 \\
x + 9(6) &= 48 \\
y &= 6 \\
8x &= -6 \\
8x + 9(6) &= 48 \\
x &= \frac{3}{4} \\
8x &= -6 \\
x &= \frac{3}{4}
\end{align*}
\]

REF: 061533ai  NAT: A.REI.5  TOP: Solving Linear Systems

ANS: \[
\begin{align*}
y &\geq 2x - 3.
\end{align*}
\]
Oscar is wrong. \((2) + 2(1) < 4\) is not true.

REF: 011534ai  NAT: A.REI.12  TOP: Graphing Systems of Linear Inequalities
KEY: graph
231 ANS:

\[ y = 6.32x + 22.43 \]

Based on the residual plot, the equation is a good fit for the data because the residual values are scattered without a pattern and are fairly evenly distributed above and below the x-axis.

REF: fall1314ai NAT: S.ID.6 TOP: Correlation Coefficient and Residuals

232 ANS:

A combination of 2 printers and 10 computers meets all the constraints because (2, 10) is in the solution set of the graph.

REF: 061535ai NAT: A.CED.3 TOP: Modeling Systems of Linear Inequalities

233 ANS:

\[ 108 = x(24 - x) \quad 18 \times 6 \]

\[ 108 = 24x - x^2 \]

\[ x^2 - 24x + 108 = 0 \]

\[ (x - 18)(x - 6) = 0 \]

\[ x = 18, 6 \]

REF: 011636ai NAT: A.CED.1 TOP: Geometric Applications of Quadratics

234 ANS:

\[ y = 836.47(2.05)^x \]

The data appear to grow at an exponential rate. \[ y = 836.47(2.05)^2 \approx 3515. \]

REF: fall1313ai NAT: S.ID.6 TOP: Regression KEY: choose model
235 ANS:
\[ r \approx 0.94. \] The correlation coefficient suggests that as calories increase, so does sodium.

REF: 011535ai NAT: S.ID.8 TOP: Correlation Coefficient

236 ANS:
\[ x = -2, 1 \]

REF: 081435ai NAT: A.REI.7 TOP: Quadratic-Linear Systems KEY: graphically

237 ANS:
Since according to the graph, 8 pencils cost $14 and 10 pencils cost $12.50, the cashier is correct.

REF: fall1312ai NAT: F.IF.7 TOP: Graphing Piecewise-Defined Functions
Algebra 1 Common Core State Standards 6 Point Regents Exam Questions
Answer Section

238 ANS:

\[ x + y \leq 15 \quad \text{One hour at school and eleven hours at the library.} \]
\[ 4x + 8y \geq 80 \]

REF: 081437ai  NAT: A.CED.3  TOP: Modeling Systems of Linear Inequalities

239 ANS:

\[ y = 120x \quad \text{and} \quad y = 70x + 1600 \]
\[ 120x = 70x + 1600 \]
\[ 50x = 1600 \]
\[ x = 32 \]

\[ y = 120(35) = 4200 \quad \text{Green Thumb is less expensive.} \]
\[ y = 70(35) + 1600 = 4050 \]

REF: fall1315ai  NAT: A.REI.6  TOP: Graphing Linear Systems
ANS: 

\[ x + y \leq 200 \quad \text{Marta is incorrect because} \quad 12.5(30) + 6.25(80) < 1500 \]

\[ 12.5x + 6.25y \geq 1500 \quad 375 + 500 < 1500 \]

\[ 875 < 1500 \]

(75,25) represents the horizontal distance (75) where the football is at its greatest height (25). No, because the ball is less than 10 feet high. 

\[ y = \frac{1}{225}(135)^2 + \frac{2}{3}(135) = -81 + 90 = 9 \]
The graphs of the production costs intersect at $x = 3$. The company should use Site $A$, because the cost of Site $A$ is lower at $x = 2$.

REF: 061437ai  NAT: A.REI.7  TOP: Quadratic-Linear Systems
KEY: graphically

(2x + 8)(2x + 6) = 100  The frame has two parts added to each side, so 2x must be added to the length and width.

$4x^2 + 28x + 48 = 100$

$x^2 + 7x - 13 = 0$

Multiply length and width to find area and set equal to 100. $x = \frac{-7 \pm \sqrt{7^2 - 4(1)(-13)}}{2(1)} = \frac{-7 + \sqrt{101}}{2} \approx 1.5$

REF: 081537ai  NAT: A.CED.1  TOP: Geometric Applications of Quadratics

$(x - 3)(2x) = 1.25x^2$  Because the original garden is a square, $x^2$ represents the original area, $x - 3$ represents the side decreased by 3 meters, $2x$ represents the doubled side, and $1.25x^2$ represents the new garden with an area 25% larger. $(x - 3)(2x) = 1.25x^2  \quad 1.25(8)^2 = 80$

$2x^2 - 6x = 1.25x^2$

$.75x^2 - 6x = 0$

$x^2 - 8x = 0$

$x(x - 8) = 0$

$x = 8$

REF: 011537ai  NAT: A.CED.1  TOP: Geometric Applications of Quadratics
ANS:
a) \( A(x) = 1.50x + 6 \)  b) \( 1.50x + 6 = 2x + 2.50 \)  c) \( A(x) = 1.50(5) + 6 = 13.50 \) Carnival \( B \) has a lower cost.

\[ B(x) = 2x + 2.50 \]
\[ .50x = 3.50 \]
\[ B(x) = 2(5) + 2.50 = 12.50 \]
\[ x = 7 \]

Carnival \( B \) has a lower cost.

REF: spr1308ai  NAT: A.REI.6  TOP: Graphing Linear Systems