Dear Sir

I have to acknowledge the receipt of your favor of May 14, in which you mention that you have finished the 6. first books of Euclid, plane trigonometry, surveying & algebra and ask whether I think a further pursuit of that branch of science would be useful to you. There are some propositions in the latter books of Euclid, & some of Archimedes, which are useful, & I have no doubt you have been made acquainted with them. Trigonometry, so far as this, is most valuable to every man, there is scarcely a day in which he will not resort to it for some of the purposes of common life. The science of calculation also is indispensable as far as the extraction of the square & cube roots; Algebra as far as the quadratic equation & the use of logarithms are often of value in ordinary cases; but all beyond these is but a luxury; a delicious luxury indeed; but not to be indulged in by one who is to have a profession to follow for his subsistence. In this light I view the conic sections, curves of the higher orders, perhaps even spherical trigonometry, Algebraical operations beyond the 2d dimension, and fluxions.

Letter from Thomas Jefferson to William G. Munford, Monticello, June 18, 1799.
1 For 10 days, Romero kept a record of the number of hours he spent listening to music. The information is shown in the table below.

<table>
<thead>
<tr>
<th>Day</th>
<th>1 2 3 4 5 6 7 8 9 10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hours</td>
<td>9 3 2 6 8 6 10 4 5 2</td>
</tr>
</tbody>
</table>

Which scatter plot shows Romero’s data graphically?

2 Throughout history, many people have contributed to the development of mathematics. These mathematicians include Pythagoras, Euclid, Hypatia, Euler, Einstein, Agnesi, Fibonacci, and Pascal. What is the probability that a mathematician’s name selected at random from those listed will start with either the letter E or the letter A?

1) $\frac{2}{8}$
2) $\frac{3}{8}$
3) $\frac{4}{8}$
4) $\frac{6}{8}$

3 Which expression represents $\frac{(2x^3)(8x^5)}{4x^6}$ in simplest form?

1) $x^2$
2) $x^9$
3) $4x^2$
4) $4x^3$

4 Which interval notation represents the set of all numbers from 2 through 7, inclusive?

1) $(2, 7]$ 
2) $(2, 7)$
3) $[2, 7)$
4) $[2, 7]$
5. Which property is illustrated by the equation \( ax + ay = a(x + y) \)?
   1) associative
   2) commutative
   3) distributive
   4) identity

6. The expression \( x^2 - 16 \) is equivalent to
   1) \((x + 2)(x - 8)\)
   2) \((x - 2)(x + 8)\)
   3) \((x + 4)(x - 4)\)
   4) \((x + 8)(x - 8)\)

7. Which situation describes a correlation that is not a causal relationship?
   1) The rooster crows, and the Sun rises.
   2) The more miles driven, the more gasoline needed.
   3) The more powerful the microwave, the faster the food cooks.
   4) The faster the pace of a runner, the quicker the runner finishes.

8. The equations \( 5x + 2y = 48 \) and \( 3x + 2y = 32 \) represent the money collected from school concert ticket sales during two class periods. If \( x \) represents the cost for each adult ticket and \( y \) represents the cost for each student ticket, what is the cost for each adult ticket?
   1) $20
   2) $10
   3) $8
   4) $4

9. The data set 5, 6, 7, 8, 9, 9, 10, 12, 14, 17, 17, 18, 19, 19 represents the number of hours spent on the Internet in a week by students in a mathematics class. Which box-and-whisker plot represents the data?

10. Given:
    Set \( A = \{(-2, -1), (-1, 0), (1, 8)\} \)
    Set \( B = \{(-3, -4), (-2, -1), (-1, 2), (1, 8)\} \).
    What is the intersection of sets \( A \) and \( B \)?
    1) \{(1, 8)\}
    2) \{(-2, -1)\}
    3) \{(-2, -1), (1, 8)\}
    4) \{(-3, -4), (-2, -1), (-1, 2), (-1, 0), (1, 8)\}
11 Tanya runs diagonally across a rectangular field that has a length of 40 yards and a width of 30 yards, as shown in the diagram below.

What is the length of the diagonal, in yards, that Tanya runs?
1) 50
2) 60
3) 70
4) 80

12 A cylindrical container has a diameter of 12 inches and a height of 15 inches, as illustrated in the diagram below.

What is the volume of this container to the nearest tenth of a cubic inch?
1) 6,785.8
2) 4,241.2
3) 2,160.0
4) 1,696.5

13 What is an equation for the line that passes through the coordinates (2,0) and (0,3)?

1) \( y = \frac{3}{2} x + 3 \)
2) \( y = \frac{3}{2} x - 3 \)
3) \( y = \frac{2}{3} x + 2 \)
4) \( y = \frac{2}{3} x - 2 \)
14. Which situation should be analyzed using bivariate data?
   1) Ms. Saleem keeps a list of the amount of time her daughter spends on her social studies homework.
   2) Mr. Benjamin tries to see if his students’ shoe sizes are directly related to their heights.
   3) Mr. DeStefan records his customers’ best video game scores during the summer.
   4) Mr. Chan keeps track of his daughter’s algebra grades for the quarter.

15. An electronics store sells DVD players and cordless telephones. The store makes a $75 profit on the sale of each DVD player \(d\) and a $30 profit on the sale of each cordless telephone \(c\). The store wants to make a profit of at least $255.00 from its sales of DVD players and cordless phones. Which inequality describes this situation?
   1) \(75d + 30c < 255\)
   2) \(75d + 30c \leq 255\)
   3) \(75d + 30c > 255\)
   4) \(75d + 30c \geq 255\)

16. What is the slope of the line containing the points \((3,4)\) and \((-6,10)\)?
   1) \(\frac{1}{2}\)
   2) \(2\)
   3) \(-\frac{2}{3}\)
   4) \(-\frac{3}{2}\)

17. Which type of graph is shown in the diagram below?

18. The expression \(\frac{9x^4 - 27x^6}{3x^4}\) is equivalent to
   1) \(3x(1 - 3x)\)
   2) \(3x(1 - 3x^2)\)
   3) \(3x(1 - 9x^5)\)
   4) \(9x^3(1 - x)\)

19. Daniel’s Print Shop purchased a new printer for $35,000. Each year it depreciates (loses value) at a rate of 5%. What will its approximate value be at the end of the fourth year?
   1) $33,250.00
   2) $30,008.13
   3) $28,507.72
   4) $27,082.33
20 Which inequality is represented by the graph below?

1) \( y < 2x + 1 \)
2) \( y < -2x + 1 \)
3) \( y < \frac{1}{2}x + 1 \)
4) \( y < -\frac{1}{2}x + 1 \)

21 In triangle \( MCT \), the measure of \( \angle T = 90^\circ \), \( MC = 85 \text{ cm} \), \( CT = 84 \text{ cm} \), and \( TM = 13 \text{ cm} \). Which ratio represents the sine of \( \angle C \)?

1) \( \frac{13}{85} \)
2) \( \frac{84}{85} \)
3) \( \frac{13}{84} \)
4) \( \frac{84}{13} \)

22 The diagram below shows the graph of \( y = |x - 3| \).
Which diagram shows the graph of \( y = -|x - 3| \)?

1)
2)
3)
4)
23. The groundskeeper is replacing the turf on a football field. His measurements of the field are 130 yards by 60 yards. The actual measurements are 120 yards by 54 yards. Which expression represents the relative error in the measurement?

1) \( \frac{130(60) - (120)(54)}{(120)(54)} \)
2) \( \frac{(130)(60) - (120)(54)}{(120)(54)} \)
3) \( \frac{130(60) - (120)(54)}{(130)(60)} \)
4) \( \frac{(130)(60) - (120)(54)}{(130)(60)} \)

24. Which value of \( x \) is in the solution set of the inequality \(-2x + 5 > 17\)?

1) \(-8\)
2) \(-6\)
3) \(-4\)
4) \(12\)

25. What is the quotient of \(8.05 \times 10^6\) and \(3.5 \times 10^2\)?

1) \(2.3 \times 10^3\)
2) \(2.3 \times 10^4\)
3) \(2.3 \times 10^8\)
4) \(2.3 \times 10^{12}\)

26. The length of a rectangular window is 5 feet more than its width, \(w\). The area of the window is 36 square feet. Which equation could be used to find the dimensions of the window?

1) \(w^2 + 5w + 36 = 0\)
2) \(w^2 - 5w - 36 = 0\)
3) \(w^2 - 5w + 36 = 0\)
4) \(w^2 + 5w - 36 = 0\)

27. What is the sum of \(\frac{d}{2}\) and \(\frac{2d}{3}\) expressed in simplest form?

1) \(\frac{3d}{5}\)
2) \(\frac{3d}{6}\)
3) \(\frac{7d}{5}\)
4) \(\frac{7d}{6}\)

28. For which value of \(x\) is \(\frac{x-3}{x^2-4}\) undefined?

1) \(-2\)
2) \(0\)
3) \(3\)
4) \(4\)

29. Which verbal expression represents \(2(n - 6)\)?

1) two times \(n\) minus six
2) two times six minus \(n\)
3) two times the quantity \(n\) less than six
4) two times the quantity six less than \(n\)
30 Which graph represents a function?

1)  

2)  

3)  

4)  

31 Express $5\sqrt{72}$ in simplest radical form.

32 Solve for $g$: $3 + 2g = 5g - 9$

33 Serena’s garden is a rectangle joined with a semicircle, as shown in the diagram below. Line segment $AB$ is the diameter of semicircle $P$. Serena wants to put a fence around her garden.

![Diagram of Serena's garden]

Calculate the length of fence Serena needs to the nearest tenth of a foot.

34 Hannah took a trip to visit her cousin. She drove 120 miles to reach her cousin’s house and the same distance back home. It took her 1.2 hours to get halfway to her cousin’s house. What was her average speed, in miles per hour, for the first 1.2 hours of the trip? Hannah’s average speed for the remainder of the trip to her cousin’s house was 40 miles per hour. How long, in hours, did it take her to drive the remaining distance? Traveling home along the same route, Hannah drove at an average rate of 55 miles per hour. After 2 hours her car broke down. How many miles was she from home?

35 A prom ticket at Smith High School is $120. Tom is going to save money for the ticket by walking his neighbor’s dog for $15 per week. If Tom already has saved $22, what is the minimum number of weeks Tom must walk the dog to earn enough to pay for the prom ticket?
36 Mr. Laub has three children: two girls (Sue and Karen) and one boy (David). After each meal, one child is chosen at random to wash dishes. If the same child can be chosen for both lunch and dinner, construct a tree diagram or list a sample space of all the possible outcomes of who will wash dishes after lunch and dinner on Saturday. Determine the probability that one boy and one girl will wash dishes after lunch and dinner on Saturday.

37 The values of 11 houses on Washington St. are shown in the table below.

<table>
<thead>
<tr>
<th>Value per House</th>
<th>Number of Houses</th>
</tr>
</thead>
<tbody>
<tr>
<td>$100,000</td>
<td>1</td>
</tr>
<tr>
<td>$175,000</td>
<td>5</td>
</tr>
<tr>
<td>$200,000</td>
<td>4</td>
</tr>
<tr>
<td>$700,000</td>
<td>1</td>
</tr>
</tbody>
</table>

Find the mean value of these houses in dollars. Find the median value of these houses in dollars. State which measure of central tendency, the mean or the median, best represents the values of these 11 houses. Justify your answer.

38 Solve the following systems of equations graphically, on the set of axes below, and state the coordinates of the point(s) in the solution set.

\[
y = x^2 - 6x + 5
\]

\[
2x + y = 5
\]

39 Solve for \( x \):

\[
\frac{x + 1}{x} = \frac{-7}{x - 12}
\]
1 Which graph represents a linear function?

2 A spinner is divided into eight equal regions as shown in the diagram below.

Which event is most likely to occur in one spin?
1) The arrow will land in a green or white area.
2) The arrow will land in a green or black area.
3) The arrow will land in a yellow or black area.
4) The arrow will land in a yellow or green area.

3 A school wants to add a coed soccer program. To determine student interest in the program, a survey will be taken. In order to get an unbiased sample, which group should the school survey?
1) every third student entering the building
2) every member of the varsity football team
3) every member in Ms. Zimmer’s drama classes
4) every student having a second-period French class

4 Factored, the expression $16x^2 - 25y^2$ is equivalent to
1) $(4x - 5y)(4x + 5y)$
2) $(4x + 5y)(4x - 5y)$
3) $(8x - 5y)(8x + 5y)$
4) $(8x + 5y)(8x - 5y)$
5 There is a negative correlation between the number of hours a student watches television and his or her social studies test score. Which scatter plot below displays this correlation?

1) ![scatter plot 1]
2) ![scatter plot 2]
3) ![scatter plot 3]
4) ![scatter plot 4]

6 Jack bought 3 slices of cheese pizza and 4 slices of mushroom pizza for a total cost of $12.50. Grace bought 3 slices of cheese pizza and 2 slices of mushroom pizza for a total cost of $8.50. What is the cost of one slice of mushroom pizza?
1) $1.50
2) $2.00
3) $3.00
4) $3.50

7 What is the product of $-3x^2y$ and $(5xy^2 + xy)$?
1) $-15x^3y^3 - 3x^3y^2$
2) $-15x^3y^3 - 3x^3y$
3) $-15x^2y^3 - 3x^2y$
4) $-15x^3y^3 + xy$

8 The bowling team at Lincoln High School must choose a president, vice president, and secretary. If the team has 10 members, which expression could be used to determine the number of ways the officers could be chosen?
1) $3P_{10}$
2) $7P_{3}$
3) $10P_{3}$
4) $10P_{7}$

9 Lenny made a cube in technology class. Each edge measured 1.5 cm. What is the volume of the cube in cubic centimeters?
1) 2.25
2) 3.375
3) 9.0
4) 13.5
10 Which ordered pair is a solution to the system of equations $y = x$ and $y = x^2 - 2$?
1) $(-2, -2)$
2) $(-1, 1)$
3) $(0, 0)$
4) $(2, 2)$

11 What are the vertex and the axis of symmetry of the parabola shown in the diagram below?

1) The vertex is $(-2, -3)$, and the axis of symmetry is $x = -2$.
2) The vertex is $(-2, -3)$, and the axis of symmetry is $y = -2$.
3) The vertex is $(-3, -2)$, and the axis of symmetry is $y = -2$.
4) The vertex is $(-3, -2)$, and the axis of symmetry is $x = -2$.

12 Pam is playing with red and black marbles. The number of red marbles she has is three more than twice the number of black marbles she has. She has 42 marbles in all. How many red marbles does Pam have?
1) 13
2) 15
3) 29
4) 33

13 What is half of $2^6$?
1) $1^3$
2) $1^6$
3) $2^3$
4) $2^5$

14 Which equation represents a line that is parallel to the line $y = -4x + 5$?
1) $y = -4x + 3$
2) $y = \frac{1}{4}x + 5$
3) $y = \frac{1}{4}x + 3$
4) $y = 4x + 5$

15 What is the product of $x^2 - 1$ and $\frac{x + 3}{3x - 3}$ expressed in simplest form?
1) $x$
2) $\frac{x}{3}$
3) $x + 3$
4) $\frac{x + 3}{3}$
16. The center pole of a tent is 8 feet long, and a side of the tent is 12 feet long as shown in the diagram below.

If a right angle is formed where the center pole meets the ground, what is the measure of angle \( A \) to the nearest degree?

1) 34
2) 42
3) 48
4) 56

17. Which value of \( x \) makes the expression \( \frac{x + 4}{x - 3} \) undefined?

1) -4
2) -3
3) 3
4) 0

18. Consider the set of integers greater than -2 and less than 6. A subset of this set is the positive factors of 5. What is the complement of this subset?

1) \{0,2,3,4\}
2) \{-1,0,2,3,4\}
3) \{-2,-1,0,2,3,4,6\}
4) \{-2,-1,0,1,2,3,4,5,6\}

19. Which data set describes a situation that could be classified as qualitative?

1) the elevations of the five highest mountains in the world
2) the ages of presidents at the time of their inauguration
3) the opinions of students regarding school lunches
4) the shoe sizes of players on the basketball team

20. What is the slope of the line that passes through the points (-6,1) and (4,-4)?

1) \(-\frac{2}{2}\)
2) 2
3) \(-\frac{1}{2}\)
4) \(\frac{1}{2}\)

21. Students in a ninth grade class measured their heights, \( h \), in centimeters. The height of the shortest student was 155 cm, and the height of the tallest student was 190 cm. Which inequality represents the range of heights?

1) \(155 < h < 190\)
2) \(155 \leq h \leq 190\)
3) \(h \geq 155 \text{ or } h \leq 190\)
4) \(h > 155 \text{ or } h < 190\)
22 The table below shows a cumulative frequency distribution of runners' ages.

<table>
<thead>
<tr>
<th>Age Group</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>20–29</td>
<td>8</td>
</tr>
<tr>
<td>20–39</td>
<td>18</td>
</tr>
<tr>
<td>20–49</td>
<td>25</td>
</tr>
<tr>
<td>20–59</td>
<td>31</td>
</tr>
<tr>
<td>20–69</td>
<td>35</td>
</tr>
</tbody>
</table>

According to the table, how many runners are in their forties?
1) 25
2) 10
3) 7
4) 6

23 Mr. Turner bought $x$ boxes of pencils. Each box holds 25 pencils. He left 3 boxes of pencils at home and took the rest to school. Which expression represents the total number of pencils he took to school?
1) $22x$
2) $25x - 3$
3) $25 - 3x$
4) $25x - 75$

24 Which expression represents $\frac{2x^2 - 12x}{x - 6}$ in simplest form?
1) 0
2) $2x$
3) $4x$
4) $2x + 2$

25 Don placed a ladder against the side of his house as shown in the diagram below.

Which equation could be used to find the distance, $x$, from the foot of the ladder to the base of the house?
1) $x = 20 - 19.5$
2) $x = 20^2 - 19.5^2$
3) $x = \sqrt{20^2 - 19.5^2}$
4) $x = \sqrt{20^2 + 19.5^2}$

26 Which value of $x$ is a solution of $\frac{5}{x} = \frac{x + 13}{6}$?
1) $-2$
2) $-3$
3) $-10$
4) $-15$
27 Mrs. Ayer is painting the outside of her son’s toy box, including the top and bottom. The toy box measures 3 feet long, 1.5 feet wide, and 2 feet high. What is the total surface area she will paint?

1) 9.0 ft²
2) 13.5 ft²
3) 22.5 ft²
4) 27.0 ft²

28 What is $\frac{\sqrt{32}}{4}$ expressed in simplest radical form?

1) $\sqrt{2}$
2) $4\sqrt{2}$
3) $\sqrt{8}$
4) $\frac{\sqrt{8}}{2}$

29 Consider the graph of the equation $y = ax^2 + bx + c$, when $a \neq 0$. If $a$ is multiplied by 3, what is true of the graph of the resulting parabola?

1) The vertex is 3 units above the vertex of the original parabola.
2) The new parabola is 3 units to the right of the original parabola.
3) The new parabola is wider than the original parabola.
4) The new parabola is narrower than the original parabola.

30 Kathy plans to purchase a car that depreciates (loses value) at a rate of 14% per year. The initial cost of the car is $21,000. Which equation represents the value, $v$, of the car after 3 years?

1) $v = 21,000(0.14)^3$
2) $v = 21,000(0.86)^3$
3) $v = 21,000(1.14)^3$
4) $v = 21,000(0.86)(3)$

31 Tom drove 290 miles from his college to home and used 23.2 gallons of gasoline. His sister, Ann, drove 225 miles from her college to home and used 15 gallons of gasoline. Whose vehicle had better gas mileage? Justify your answer.

32 A designer created the logo shown below. The logo consists of a square and four quarter-circles of equal size.

Express, in terms of $\pi$, the exact area, in square inches, of the shaded region.
33 Maureen tracks the range of outdoor temperatures over three days. She records the following information.

- **Day 1:**
  - Temperature range: -20°F to 40°F
- **Day 2:**
  - Temperature range: 0°F to 50°F
- **Day 3:**
  - Temperature range: 23°F to 45°F

Express the intersection of the three sets as an inequality in terms of temperature, \( t \).

34 Peter begins his kindergarten year able to spell 10 words. He is going to learn to spell 2 new words every day. Write an inequality that can be used to determine how many days, \( d \), it takes Peter to be able to spell at least 75 words. Use this inequality to determine the minimum number of whole days it will take for him to be able to spell at least 75 words.

35 The Hudson Record Store is having a going-out-of-business sale. CDs normally sell for $18.00. During the first week of the sale, all CDs will sell for $15.00. Written as a fraction, what is the rate of discount? What is this rate expressed as a percent? Round your answer to the nearest hundredth of a percent. During the second week of the sale, the same CDs will be on sale for 25% off the original price. What is the price of a CD during the second week of the sale?

36 Graph the equation \( y = x^2 - 2x - 3 \) on the accompanying set of axes. Using the graph, determine the roots of the equation \( x^2 - 2x - 3 = 0 \).
38 Sophie measured a piece of paper to be 21.7 cm by 28.5 cm. The piece of paper is actually 21.6 cm by 28.4 cm. Determine the number of square centimeters in the area of the piece of paper using Sophie’s measurements. Determine the number of square centimeters in the actual area of the piece of paper. Determine the relative error in calculating the area. Express your answer as a decimal to the nearest thousandth. Sophie does not think there is a significant amount of error. Do you agree or disagree? Justify your answer.

39 The prices of seven race cars sold last week are listed in the table below.

<table>
<thead>
<tr>
<th>Price per Race Car</th>
<th>Number of Race Cars</th>
</tr>
</thead>
<tbody>
<tr>
<td>$126,000</td>
<td>1</td>
</tr>
<tr>
<td>$140,000</td>
<td>2</td>
</tr>
<tr>
<td>$180,000</td>
<td>1</td>
</tr>
<tr>
<td>$400,000</td>
<td>2</td>
</tr>
<tr>
<td>$819,000</td>
<td>1</td>
</tr>
</tbody>
</table>

What is the mean value of these race cars, in dollars? What is the median value of these race cars, in dollars? State which of these measures of central tendency best represents the value of the seven race cars. Justify your answer.
1 Which value of $p$ is the solution of $5p - 1 = 2p + 20$?

1) \( \frac{19}{7} \)
2) \( \frac{19}{3} \)
3) 3
4) 7

2 The statement $2 + 0 = 2$ is an example of the use of which property of real numbers?

1) associative
2) additive identity
3) additive inverse
4) distributive

3 Mrs. Smith wrote "Eight less than three times a number is greater than fifteen" on the board. If $x$ represents the number, which inequality is a correct translation of this statement?

1) $3x - 8 > 15$
2) $3x - 8 < 15$
3) $8 - 3x > 15$
4) $8 - 3x < 15$

4 Which statement is true about the data set 3, 4, 5, 6, 7, 7, 10?

1) mean = mode
2) mean > mode
3) mean = median
4) mean < median

5 Which value of $x$ is in the solution set of the inequality $-4x + 2 > 10$?

1) $-2$
2) 2
3) 3
4) $-4$

6 Factored completely, the expression $2x^2 + 10x - 12$ is equivalent to

1) $2(x - 6)(x + 1)$
2) $2(x + 6)(x - 1)$
3) $2(x + 2)(x + 3)$
4) $2(x - 2)(x - 3)$
7 The gas tank in a car holds a total of 16 gallons of gas. The car travels 75 miles on 4 gallons of gas. If the gas tank is full at the beginning of a trip, which graph represents the rate of change in the amount of gas in the tank?

8 If $3ax + b = c$, then $x$ equals
   1) $c - b + 3a$
   2) $c + b - 3a$
   3) $\frac{c - b}{3a}$
   4) $\frac{b - c}{3a}$

9 The length of the hypotenuse of a right triangle is 34 inches and the length of one of its legs is 16 inches. What is the length, in inches, of the other leg of this right triangle?
   1) 16
   2) 18
   3) 25
   4) 30

10 Which equation represents a line parallel to the $x$-axis?
   1) $x = 5$
   2) $y = 10$
   3) $x = \frac{1}{3}y$
   4) $y = 5x + 17$

11 Sam and Odel have been selling frozen pizzas for a class fundraiser. Sam has sold half as many pizzas as Odel. Together they have sold a total of 126 pizzas. How many pizzas did Sam sell?
   1) 21
   2) 42
   3) 63
   4) 84
12. Which ordered pair is in the solution set of the system of equations \( y = -x + 1 \) and \( y = x^2 + 5x + 6 \)?
   1) \((-5, -1)\)
   2) \((-5, 6)\)
   3) \((5, -4)\)
   4) \((5, 2)\)

13. A swim team member performs a dive from a 14-foot-high springboard. The parabola below shows the path of her dive.

   Which equation represents the axis of symmetry?
   1) \(x = 3\)
   2) \(y = 3\)
   3) \(x = 23\)
   4) \(y = 23\)

14. Nicole’s aerobics class exercises to fast-paced music. If the rate of the music is 120 beats per minute, how many beats would there be in a class that is 0.75 hour long?
   1) 90
   2) 160
   3) 5,400
   4) 7,200

15. Luis is going to paint a basketball court on his driveway, as shown in the diagram below. This basketball court consists of a rectangle and a semicircle.

   Which expression represents the area of this basketball court, in square feet?
   1) 80
   2) \(80 + 8\pi\)
   3) \(80 + 16\pi\)
   4) \(80 + 64\pi\)

16. John is going to line up his four golf trophies on a shelf in his bedroom. How many different possible arrangements can he make?
   1) 24
   2) 16
   3) 10
   4) 4
17. A rectangle has an area of 24 square units. The width is 5 units less than the length. What is the length, in units, of the rectangle?

1) 6
2) 8
3) 3
4) 19

18. What is the value of the third quartile shown on the box-and-whisker plot below?

1) 6
2) 8.5
3) 10
4) 12

19. When \(3g^2 - 4g + 2\) is subtracted from \(7g^2 + 5g - 1\), the difference is

1) \(-4g^2 - 9g + 3\)
2) \(4g^2 + g + 1\)
3) \(4g^2 + 9g - 3\)
4) \(10g^2 + g + 1\)

20. Which value of \(x\) is the solution of \(\frac{2x}{5} + \frac{1}{3} = \frac{7x - 2}{15}\)?

1) \(\frac{3}{5}\)
2) \(\frac{31}{26}\)
3) 3
4) 7

21. Which expression represents \(\frac{25x - 125}{x^2 - 25}\) in simplest form?

1) \(\frac{5}{x}\)
2) \(-\frac{5}{x}\)
3) \(\frac{25}{x - 5}\)
4) \(\frac{25}{x + 5}\)

22. Which equation most closely represents the line of best fit for the scatter plot below?

1) \(y = x\)
2) \(y = \frac{2}{3}x + 1\)
3) \(y = \frac{3}{2}x + 4\)
4) \(y = \frac{3}{2}x + 1\)
23. In a linear equation, the independent variable increases at a constant rate while the dependent variable decreases at a constant rate. The slope of this line is
1) zero
2) negative
3) positive
4) undefined

24. Which equation could be used to find the measure of one acute angle in the right triangle shown below?

\[ \sin A = \frac{4}{5} \]

25. Which ordered pair is in the solution set of the following system of inequalities?
\[ y < \frac{1}{2} x + 4 \]
\[ y \geq -x + 1 \]
1) \((-5, 3)\)
2) \((0, 4)\)
3) \((3, -5)\)
4) \((4, 0)\)

26. What is the product of \( \frac{4x}{x - 1} \) and \( \frac{x^2 - 1}{3x + 3} \) expressed in simplest form?
1) \( \frac{4x}{3} \)
2) \( \frac{4x^2}{3} \)
3) \( \frac{4x^2}{3(x + 1)} \)
4) \( \frac{4(x + 1)}{3} \)

27. Which expression is equivalent to \( (3x^2)^3 \)?
1) \( 9x^5 \)
2) \( 9x^6 \)
3) \( 27x^5 \)
4) \( 27x^6 \)
28 Ryan estimates the measurement of the volume of a popcorn container to be 282 cubic inches. The actual volume of the popcorn container is 289 cubic inches. What is the relative error of Ryan's measurement to the nearest thousandth?

1) 0.024  
2) 0.025  
3) 0.096  
4) 1.025

29 In the diagram of $\triangle ABC$ shown below, $BC = 10$ and $AB = 16$.

![Diagram of triangle ABC]

To the nearest tenth of a degree, what is the measure of the largest acute angle in the triangle?

1) 32.0  
2) 38.7  
3) 51.3  
4) 90.0

30 The faces of a cube are numbered from 1 to 6. If the cube is tossed once, what is the probability that a prime number or a number divisible by 2 is obtained?

1) $\frac{6}{6}$  
2) $\frac{5}{6}$  
3) $\frac{4}{6}$  
4) $\frac{1}{6}$

31 In a game of ice hockey, the hockey puck took 0.8 second to travel 89 feet to the goal line. Determine the average speed of the puck in feet per second.

32 Brianna is using the two spinners shown below to play her new board game. She spins the arrow on each spinner once. Brianna uses the first spinner to determine how many spaces to move. She uses the second spinner to determine whether her move from the first spinner will be forward or backward.

![Spinners]

Find the probability that Brianna will move fewer than four spaces and backward.
33 Twelve players make up a high school basketball team. The team jerseys are numbered 1 through 12. The players wearing the jerseys numbered 3, 6, 7, 8, and 11 are the only players who start a game. Using set notation, list the complement of this subset.

34 Express the product of \(3\sqrt{20}(2\sqrt{5} - 7)\) in simplest radical form.

35 On the set of axes below, draw the graph of \(y = 2^x\) over the interval \(-1 \leq x \leq 3\). Will this graph ever intersect the x-axis? Justify your answer.

36 Write an equation that represents the line that passes through the points \((5,4)\) and \((-5,0)\).

37 The cost of 3 markers and 2 pencils is $1.80. The cost of 4 markers and 6 pencils is $2.90. What is the cost of each item? Include appropriate units in your answer.

38 Twenty students were surveyed about the number of days they played outside in one week. The results of this survey are shown below.

\[
\{6,5,4,3,0,7,1,5,4,4,3,2,2,3,2,4,3,4,0,7\}
\]

Complete the frequency table below for these data.

<table>
<thead>
<tr>
<th>Interval</th>
<th>Tally</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>0–1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2–3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4–5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6–7</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Complete the cumulative frequency table below using these data.

<table>
<thead>
<tr>
<th>Number of Days Outside</th>
<th>Cumulative Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>0–1</td>
<td></td>
</tr>
<tr>
<td>0–3</td>
<td></td>
</tr>
<tr>
<td>0–5</td>
<td></td>
</tr>
<tr>
<td>0–7</td>
<td></td>
</tr>
</tbody>
</table>

On the grid below, create a cumulative frequency histogram based on the table you made.
39 On the set of axes below, solve the following system of equations graphically and state the coordinates of all points in the solution set.

\[ y = x^2 + 4x - 5 \]

\[ y = x - 1 \]
1 On a certain day in Toronto, Canada, the temperature was 15° Celsius (C). Using the formula $F = \frac{9}{5} C + 32$, Peter converts this temperature to degrees Fahrenheit (F). Which temperature represents 15°C in degrees Fahrenheit?

1) −9
2) 35
3) 59
4) 85

2 What is the speed, in meters per second, of a paper airplane that flies 24 meters in 6 seconds?
1) 144
2) 30
3) 18
4) 4

3 The faces of a cube are numbered from 1 to 6. If the cube is rolled once, which outcome is least likely to occur?
1) rolling an odd number
2) rolling an even number
3) rolling a number less than 6
4) rolling a number greater than 4

4 Tamara has a cell phone plan that charges $0.07 per minute plus a monthly fee of $19.00. She budgets $29.50 per month for total cell phone expenses without taxes. What is the maximum number of minutes Tamara could use her phone each month in order to stay within her budget?
1) 150
2) 271
3) 421
4) 692

5 Antwaan leaves a cup of hot chocolate on the counter in his kitchen. Which graph is the best representation of the change in temperature of his hot chocolate over time?
6. What is the solution of \( \frac{k + 4}{2} = \frac{k + 9}{3} \)?
   1) 1
   2) 5
   3) 6
   4) 14

7. Alex earned scores of 60, 74, 82, 87, 87, and 94 on his first six algebra tests. What is the relationship between the measures of central tendency of these scores?
   1) median < mode < mean
   2) mean < mode < median
   3) mode < median < mean
   4) mean < median < mode

8. The New York Volleyball Association invited 64 teams to compete in a tournament. After each round, half of the teams were eliminated. Which equation represents the number of teams, \( t \), that remained in the tournament after \( r \) rounds?
   1) \( t = 64(r^{0.5}) \)
   2) \( t = 64(-0.5)^r \)
   3) \( t = 64(1.5)^r \)
   4) \( t = 64(0.5)^r \)

9. The expression \( 9x^2 - 100 \) is equivalent to
   1) \( (9x - 10)(x + 10) \)
   2) \( (3x - 10)(3x + 10) \)
   3) \( (3x - 100)(3x - 1) \)
   4) \( (9x - 100)(x + 1) \)

10. What is an equation of the line that passes through the points \( (3, -3) \) and \( (-3, -3) \)?
    1) \( y = 3 \)
    2) \( x = -3 \)
    3) \( y = -3 \)
    4) \( x = y \)

11. If the formula for the perimeter of a rectangle is \( P = 2l + 2w \), then \( w \) can be expressed as
    1) \( w = \frac{2l - P}{2} \)
    2) \( w = \frac{P - 2l}{2} \)
    3) \( w = \frac{P - l}{2} \)
    4) \( w = \frac{P - 2w}{2l} \)

12. In the right triangle shown in the diagram below, what is the value of \( x \) to the nearest whole number?

   ![Diagram of a right triangle with angle 30° and side 24]
13 What is the slope of the line that passes through the points (2, 5) and (7, 3)?

1) \( \frac{5}{2} \)
2) \( \frac{2}{5} \)
3) \( \frac{8}{9} \)
4) \( \frac{9}{8} \)

14 What are the roots of the equation \( x^2 - 10x + 21 = 0 \)?

1) 1 and 21
2) -5 and -5
3) 3 and 7
4) -3 and -7

15 Rhonda has $1.35 in nickels and dimes in her pocket. If she has six more dimes than nickels, which equation can be used to determine \( x \), the number of nickels she has?

1) \( 0.05(x + 6) + 0.10x = 1.35 \)
2) \( 0.05x + 0.10(x + 6) = 1.35 \)
3) \( 0.05 + 0.10(6x) = 1.35 \)
4) \( 0.15(x + 6) = 1.35 \)

16 Which equation represents the axis of symmetry of the graph of the parabola below?

1) \( y = -3 \)
2) \( x = -3 \)
3) \( y = -25 \)
4) \( x = -25 \)

17 The set \{1, 2, 3, 4\} is equivalent to

1) \( \{x | 1 < x < 4, \text{ where } x \text{ is a whole number}\} \)
2) \( \{x | 0 < x < 4, \text{ where } x \text{ is a whole number}\} \)
3) \( \{x | 0 < x \leq 4, \text{ where } x \text{ is a whole number}\} \)
4) \( \{x | 1 < x \leq 4, \text{ where } x \text{ is a whole number}\} \)

18 What is the value of \( x \) in the equation \( \frac{2}{x} - 3 = \frac{26}{x} \)?

1) -8
2) \( \frac{1}{8} \)
3) \( \frac{1}{8} \)
4) 8
19 The diagram below shows right triangle \( \triangle UPC \).

Which ratio represents the sine of \( \angle U \)?

1) \( \frac{15}{8} \)
2) \( \frac{15}{17} \)
3) \( \frac{8}{15} \)
4) \( \frac{8}{17} \)

20 What is \( \sqrt{72} \) expressed in simplest radical form?

1) \( 2\sqrt{18} \)
2) \( 3\sqrt{8} \)
3) \( 6\sqrt{2} \)
4) \( 8\sqrt{3} \)

21 What is \( \frac{6}{2x} - \frac{2}{3x} \) in simplest form?

1) \( \frac{8}{15x^2} \)
2) \( \frac{8}{15x} \)
3) \( \frac{4}{15x} \)
4) \( \frac{4}{2x} \)

22 Which ordered pair is a solution of the system of equations \( y = x^2 - x - 20 \) and \( y = 3x - 15 \)?

1) \( (-5,-30) \)
2) \( (-1,-18) \)
3) \( (0,5) \)
4) \( (5,-1) \)

23 A survey is being conducted to determine which types of television programs people watch. Which survey and location combination would likely contain the most bias?

1) surveying 10 people who work in a sporting goods store
2) surveying the first 25 people who enter a grocery store
3) randomly surveying 50 people during the day in a mall
4) randomly surveying 75 people during the day in a clothing store

24 The length of a rectangular room is 7 less than three times the width, \( w \), of the room. Which expression represents the area of the room?

1) \( 3w - 4 \)
2) \( 3w - 7 \)
3) \( 3w^2 - 4w \)
4) \( 3w^2 - 7w \)

25 The function \( y = \frac{x}{x^2 - 9} \) is undefined when the value of \( x \) is

1) 0 or 3
2) 3 or \(-3\)
3) 3, only
4) \(-3\), only
26. Which equation represents a line that is parallel to the line $y = 3 - 2x$?
   1) $4x + 2y = 5$
   2) $2x + 4y = 1$
   3) $y = 3 - 4x$
   4) $y = 4x - 2$

27. What is the product of $8.4 \times 10^8$ and $4.2 \times 10^3$ written in scientific notation?
   1) $2.0 \times 10^5$
   2) $12.6 \times 10^{11}$
   3) $35.28 \times 10^{11}$
   4) $3.528 \times 10^{12}$

28. Keisha is playing a game using a wheel divided into eight equal sectors, as shown in the diagram below. Each time the spinner lands on orange, she will win a prize.

   If Keisha spins this wheel twice, what is the probability she will win a prize on both spins?
   1) $\frac{1}{64}$
   2) $\frac{1}{56}$
   3) $\frac{1}{16}$
   4) $\frac{1}{4}$
29 A movie theater recorded the number of tickets sold daily for a popular movie during the month of June. The box-and-whisker plot shown below represents the data for the number of tickets sold, in hundreds.

Which conclusion can be made using this plot?
1) The second quartile is 600.
2) The mean of the attendance is 400.
3) The range of the attendance is 300 to 600.
4) Twenty-five percent of the attendance is between 300 and 400.

30 Which graph represents a function?
31 A window is made up of a single piece of glass in the shape of a semicircle and a rectangle, as shown in the diagram below. Tess is decorating for a party and wants to put a string of lights all the way around the outside edge of the window.

To the nearest foot, what is the length of the string of lights that Tess will need to decorate the window?

32 Simplify: \( \frac{27k^5m^3}{(4k^3)(9m^2)} \)

33 The table below represents the number of hours a student worked and the amount of money the student earned.

<table>
<thead>
<tr>
<th>Number of Hours (h)</th>
<th>Dollars Earned (d)</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>$50.00</td>
</tr>
<tr>
<td>15</td>
<td>$93.75</td>
</tr>
<tr>
<td>19</td>
<td>$118.75</td>
</tr>
<tr>
<td>30</td>
<td>$187.50</td>
</tr>
</tbody>
</table>

Write an equation that represents the number of dollars, \( d \), earned in terms of the number of hours, \( h \), worked. Using this equation, determine the number of dollars the student would earn for working 40 hours.

34 Sarah measures her rectangular bedroom window for a new shade. Her measurements are 36 inches by 42 inches. The actual measurements of the window are 36.5 inches and 42.5 inches. Using the measurements that Sarah took, determine the number of square inches in the area of the window. Determine the number of square inches in the actual area of the window. Determine the relative error in calculating the area. Express your answer as a decimal to the nearest thousandth.

35 Perform the indicated operation and simplify:
\[
\frac{3x + 6}{4x + 12} + \frac{x^2 - 4}{x + 3}
\]
36 A soup can is in the shape of a cylinder. The can has a volume of $342 \text{ cm}^3$ and a diameter of 6 cm. Express the height of the can in terms of $\pi$. Determine the maximum number of soup cans that can be stacked on their base between two shelves if the distance between the shelves is exactly 36 cm. Explain your answer.

37 Solve the following system of equations algebraically:

\[
\begin{align*}
3x + 2y &= 4 \\
4x + 3y &= 7
\end{align*}
\]

[Only an algebraic solution can receive full credit.]

38 On the set of axes below, graph the following system of inequalities and state the coordinates of a point in the solution set.

\[
\begin{align*}
2x - y &\geq 6 \\
x &> 2
\end{align*}
\]

39 A restaurant sells kids' meals consisting of one main course, one side dish, and one drink, as shown in the table below.

<table>
<thead>
<tr>
<th>Kids' Meal Choices</th>
</tr>
</thead>
<tbody>
<tr>
<td>Main Course</td>
</tr>
<tr>
<td>hamburger</td>
</tr>
<tr>
<td>chicken nuggets</td>
</tr>
<tr>
<td>turkey sandwich</td>
</tr>
</tbody>
</table>

Draw a tree diagram or list the sample space showing all possible kids' meals. How many different kids' meals can a person order? Jose does not drink juice. Determine the number of different kids' meals that do not include juice. Jose's sister will eat only chicken nuggets for her main course. Determine the number of different kids' meals that include chicken nuggets.
1 It takes Tammy 45 minutes to ride her bike 5 miles. At this rate, how long will it take her to ride 8 miles?
   1) 0.89 hour
   2) 1.125 hours
   3) 48 minutes
   4) 72 minutes

2 What are the roots of the equation $x^2 - 7x + 6 = 0$?
   1) 1 and 7
   2) −1 and 7
   3) −1 and −6
   4) 1 and 6

3 Which expression represents $\frac{27x^{18}y^5}{9x^6y}$ in simplest form?
   1) $3x^{12}y^4$
   2) $3x^3y^5$
   3) $18x^{12}y^4$
   4) $18x^3y^5$

4 Marie currently has a collection of 58 stamps. If she buys $s$ stamps each week for $w$ weeks, which expression represents the total number of stamps she will have?
   1) $58sw$
   2) $58 + sw$
   3) $58s + w$
   4) $58 + s + w$

5 Which data set describes a situation that could be classified as qualitative?
   1) the ages of the students in Ms. Marshall’s Spanish class
   2) the test scores of the students in Ms. Fitzgerald’s class
   3) the favorite ice cream flavor of each of Mr. Hayden’s students
   4) the heights of the players on the East High School basketball team

6 The sign shown below is posted in front of a roller coaster ride at the Wadsworth County Fairgrounds.

   All riders MUST be at least 48 inches tall.

If $h$ represents the height of a rider in inches, what is a correct translation of the statement on this sign?
   1) $h < 48$
   2) $h > 48$
   3) $h \leq 48$
   4) $h \geq 48$

7 Which value of $x$ is the solution of the equation $\frac{2x}{3} + \frac{x}{6} = 5$?
   1) 6
   2) 10
   3) 15
   4) 30
8 Students in Ms. Nazzeer's mathematics class tossed a six-sided number cube whose faces are numbered 1 to 6. The results are recorded in the table below.

<table>
<thead>
<tr>
<th>Result</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3</td>
</tr>
<tr>
<td>2</td>
<td>6</td>
</tr>
<tr>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>4</td>
<td>6</td>
</tr>
<tr>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>6</td>
<td>7</td>
</tr>
</tbody>
</table>

Based on these data, what is the empirical probability of tossing a 4?

1) \(\frac{8}{30}\)
2) \(\frac{6}{30}\)
3) \(\frac{5}{30}\)
4) \(\frac{1}{30}\)

9 What is the value of \(x\), in inches, in the right triangle below?

1) \(\sqrt{15}\)
2) 8
3) \(\sqrt{34}\)
4) 4

10 What is \(\sqrt{32}\) expressed in simplest radical form?

1) \(16\sqrt{2}\)
2) \(4\sqrt{2}\)
3) \(4\sqrt{8}\)
4) \(2\sqrt{8}\)

11 If the speed of sound is 344 meters per second, what is the approximate speed of sound, in meters per hour?

| 60 seconds = 1 minute |
| 60 minutes = 1 hour |

1) 20,640
2) 41,280
3) 123,840
4) 1,238,400

12 The sum of two numbers is 47, and their difference is 15. What is the larger number?

1) 16
2) 31
3) 32
4) 36

13 If \(a + ar = b + r\), the value of \(a\) in terms of \(b\) and \(r\) can be expressed as

1) \(\frac{b}{r} + 1\)
2) \(\frac{1 + b}{r}\)
3) \(\frac{b + r}{1 + r}\)
4) \(\frac{1 + b}{r + b}\)
14 Which value of $x$ is in the solution set of $\frac{4}{3}x + 5 < 17$?
1) 8
2) 9
3) 12
4) 16

15 The box-and-whisker plot below represents students' scores on a recent English test.

What is the value of the upper quartile?
1) 68
2) 76
3) 84
4) 94

16 Which value of $n$ makes the expression $\frac{5n}{2n - 1}$ undefined?
1) 1
2) 0
3) $\frac{1}{2}$
4) $\frac{1}{2}$

17 At Genesee High School, the sophomore class has 60 more students than the freshman class. The junior class has 50 fewer students than twice the students in the freshman class. The senior class is three times as large as the freshman class. If there are a total of 1,424 students at Genesee High School, how many students are in the freshman class?
1) 202
2) 205
3) 235
4) 236

18 What are the vertex and axis of symmetry of the parabola $y = x^2 - 16x + 63$?
1) vertex: (8, -1); axis of symmetry: $x = 8$
2) vertex: (8, 1); axis of symmetry: $x = 8$
3) vertex: (-8, -1); axis of symmetry: $x = -8$
4) vertex: (-8, 1); axis of symmetry: $x = -8$
19 Which statement is true about the relation shown on the graph below?

1) It is a function because there exists one \( x \)-coordinate for each \( y \)-coordinate.
2) It is a function because there exists one \( y \)-coordinate for each \( x \)-coordinate.
3) It is not a function because there are multiple \( y \)-values for a given \( x \)-value.
4) It is not a function because there are multiple \( x \)-values for a given \( y \)-value.

20 Which graph represents the solution of \( 3y - 9 \leq 6x \)?

1) 
2) 
3) 
4)
21 Which expression represents \( \frac{x^2 - 2x - 15}{x^2 + 3x} \) in simplest form?
1) \(-5\)
2) \(\frac{x - 5}{x}\)
3) \(-2x - 5\)
4) \(-2x - 15\)

22 What is an equation of the line that passes through the point \((4, -6)\) and has a slope of \(-3\)?
1) \(y = -3x + 6\)
2) \(y = -3x - 6\)
3) \(y = -3x + 10\)
4) \(y = -3x + 14\)

23 When \(4x^2 + 7x - 5\) is subtracted from \(9x^2 - 2x + 3\), the result is
1) \(5x^2 + 5x - 2\)
2) \(5x^2 - 9x + 8\)
3) \(-5x^2 + 5x - 2\)
4) \(-5x^2 + 9x - 8\)

24 The equation \(y = x^2 + 3x - 18\) is graphed on the set of axes below.

Based on this graph, what are the roots of the equation \(x^2 + 3x - 18 = 0\)?
1) \(-3\) and 6
2) 0 and \(-18\)
3) 3 and \(-6\)
4) 3 and \(-18\)

25 What is the value of the \(y\)-coordinate of the solution to the system of equations \(x + 2y = 9\) and \(x - y = 3\)?
1) 6
2) 2
3) 3
4) 5

26 What is the additive inverse of the expression \(a - b\)?
1) \(a + b\)
2) \(a - b\)
3) \(-a + b\)
4) \(-a - b\)
27 What is the product of 12 and \(4.2 \times 10^6\) expressed in scientific notation?
1) \(50.4 \times 10^6\)
2) \(50.4 \times 10^7\)
3) \(5.04 \times 10^6\)
4) \(5.04 \times 10^7\)

28 To calculate the volume of a small wooden cube, Ezra measured an edge of the cube as 2 cm. The actual length of the edge of Ezra’s cube is 2.1 cm. What is the relative error in his volume calculation to the nearest hundredth?
1) 0.13
2) 0.14
3) 0.15
4) 0.16

29 What is \(\frac{6}{4a} - \frac{2}{3a}\) expressed in simplest form?
1) \(\frac{4}{a}\)
2) \(\frac{5}{6a}\)
3) \(\frac{8}{7a}\)
4) \(\frac{10}{12a}\)

30 The set \(\{11, 12\}\) is equivalent to
1) \(\{x| 11 < x < 12, \text{ where } x \text{ is an integer}\}\)
2) \(\{x| 11 < x \leq 12, \text{ where } x \text{ is an integer}\}\)
3) \(\{x| 10 \leq x < 12, \text{ where } x \text{ is an integer}\}\)
4) \(\{x| 10 < x \leq 12, \text{ where } x \text{ is an integer}\}\)

31 Determine how many three-letter arrangements are possible with the letters \(A, N, G, L,\) and \(E\) if no letter may be repeated.

32 Factor completely: \(4x^3 - 36x\)

33 Some books are laid on a desk. Two are English, three are mathematics, one is French, and four are social studies. Theresa selects an English book and Isabelle then selects a social studies book. Both girls take their selections to the library to read. If Truman then selects a book at random, what is the probability that he selects an English book?

34 In the diagram below, the circumference of circle \(O\) is \(16\pi\) inches. The length of \(BC\) is three-quarters of the length of diameter \(AD\) and \(CE = 4\) inches. Calculate the area, in square inches, of trapezoid \(ABCD\).
35 A bank is advertising that new customers can open a savings account with a $3\frac{3}{4}$% interest rate compounded annually. Robert invests $5,000 in an account at this rate. If he makes no additional deposits or withdrawals on his account, find the amount of money he will have, to the nearest cent, after three years.

36 The table below shows the number of prom tickets sold over a ten-day period.

<table>
<thead>
<tr>
<th>Day (x)</th>
<th>1</th>
<th>2</th>
<th>5</th>
<th>7</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of Prom Tickets Sold (y)</td>
<td>30</td>
<td>35</td>
<td>55</td>
<td>60</td>
<td>70</td>
</tr>
</tbody>
</table>

Plot these data points on the coordinate grid below. Use a consistent and appropriate scale. Draw a reasonable line of best fit and write its equation.

37 A stake is to be driven into the ground away from the base of a 50-foot pole, as shown in the diagram below. A wire from the stake on the ground to the top of the pole is to be installed at an angle of elevation of $52^\circ$.

How far away from the base of the pole should the stake be driven in, to the nearest foot? What will be the length of the wire from the stake to the top of the pole, to the nearest foot?
38 The Fahrenheit temperature readings on 30 April mornings in Stormville, New York, are shown below.

41°, 58°, 61°, 54°, 49°, 46°, 52°, 58°, 67°, 43°, 47°, 60°, 52°, 58°, 48°, 44°, 59°, 66°, 62°, 55°, 44°, 49°, 62°, 61°, 59°, 54°, 57°, 58°, 63°, 60°

Using the data, complete the frequency table below.

<table>
<thead>
<tr>
<th>Interval</th>
<th>Tally</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>40–44</td>
<td></td>
<td></td>
</tr>
<tr>
<td>45–49</td>
<td></td>
<td></td>
</tr>
<tr>
<td>50–54</td>
<td></td>
<td></td>
</tr>
<tr>
<td>55–59</td>
<td></td>
<td></td>
</tr>
<tr>
<td>60–64</td>
<td></td>
<td></td>
</tr>
<tr>
<td>65–69</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

On the grid below, construct and label a frequency histogram based on the table.

39 On the set of axes below, solve the following system of equations graphically for all values of \(x\) and \(y\).

\[
y = x^2 - 6x + 1
\]

\[
y + 2x = 6
\]
1 If $h$ represents a number, which equation is a correct translation of “Sixty more than 9 times a number is 375”?
1) $9h = 375$
2) $9h + 60 = 375$
3) $9h - 60 = 375$
4) $60h + 9 = 375$

2 Which expression is equivalent to $9x^2 - 16$?
1) $(3x + 4)(3x - 4)$
2) $(3x - 4)(3x - 4)$
3) $(3x + 8)(3x - 8)$
4) $(3x - 8)(3x - 8)$

3 Which expression represents $(3x^2y^4)(4xy^2)$ in simplest form?
1) $12x^3y^6$
2) $12x^2y^8$
3) $12x^3y^8$
4) $12x^3y^6$

4 An online music club has a one-time registration fee of $13.95 and charges $0.49 to buy each song. If Emma has $50.00 to join the club and buy songs, what is the maximum number of songs she can buy?
1) 73
2) 74
3) 130
4) 131

5 The local ice cream stand offers three flavors of soft-serve ice cream: vanilla, chocolate, and strawberry; two types of cone: sugar and wafer; and three toppings: sprinkles, nuts, and cookie crumbs. If Dawn does not order vanilla ice cream, how many different choices can she make that have one flavor of ice cream, one type of cone, and one topping?
1) 7
2) 8
3) 12
4) 18

6 Nancy’s rectangular garden is represented in the diagram below.

If a diagonal walkway crosses her garden, what is its length, in feet?
1) 17
2) 22
3) $\sqrt{161}$
4) $\sqrt{529}$
7 The spinner below is divided into eight equal regions and is spun once. What is the probability of not getting red?

![Spinner Image]

1) \(\frac{3}{5}\)
2) \(\frac{3}{8}\)
3) \(\frac{5}{8}\)
4) \(\frac{7}{8}\)

8 Which relationship can best be described as causal?
1) height and intelligence
2) shoe size and running speed
3) number of correct answers on a test and test score
4) number of students in a class and number of students with brown hair

9 Solve for \(x\):
\[
\frac{3}{5} (x + 2) = x - 4
\]
1) 8
2) 13
3) 15
4) 23

10 Erica is conducting a survey about the proposed increase in the sports budget in the Hometown School District. Which survey method would likely contain the most bias?
1) Erica asks every third person entering the Hometown Grocery Store.
2) Erica asks every third person leaving the Hometown Shopping Mall this weekend.
3) Erica asks every fifth student entering Hometown High School on Monday morning.
4) Erica asks every fifth person leaving Saturday’s Hometown High School football game.

11 Which equation represents a line parallel to the \(x\)-axis?
1) \(y = -5\)
2) \(y = -5x\)
3) \(x = 3\)
4) \(x = 3y\)

12 Given:
\[A = \{\text{All even integers from 2 to 20, inclusive}\}\]
\[B = \{10, 12, 14, 16, 18\}\]
What is the complement of set \(B\) within the universe of set \(A\)?
1) \(\{4, 6, 8\}\)
2) \(\{2, 4, 6, 8\}\)
3) \(\{4, 6, 8, 20\}\)
4) \(\{2, 4, 6, 8, 20\}\)

13 Which value of \(x\) is in the solution set of the inequality \(-2(x - 5) < 4\)?
1) 0
2) 2
3) 3
4) 5
14 A tree casts a 25-foot shadow on a sunny day, as shown in the diagram below.

If the angle of elevation from the tip of the shadow to the top of the tree is 32°, what is the height of the tree to the nearest tenth of a foot?
1) 13.2
2) 15.6
3) 21.2
4) 40.0

15 What is the slope of the line that passes through the points (−5,4) and (15,−4)?
1) −\frac{2}{5}
2) 0
3) \frac{5}{2}
4) undefined

16 The equation \( y = -x^2 - 2x + 8 \) is graphed on the set of axes below.

Based on this graph, what are the roots of the equation \( -x^2 - 2x + 8 = 0 \)?
1) 8 and 0
2) 2 and −4
3) 9 and −1
4) 4 and −2

17 What is the sum of \( \frac{3}{2x} \) and \( \frac{4}{3x} \) expressed in simplest form?
1) \frac{12}{6x^2}
2) \frac{17}{6x}
3) \frac{7}{5x}
4) \frac{17}{12x}
18 Which value of \(x\) makes the expression \(\frac{x^2 - 9}{x^2 + 7x + 10}\) undefined?
1) \(-5\)
2) \(2\)
3) \(3\)
4) \(-3\)

19 Which relation is not a function?
1) \{(1,5),(2,6),(3,6),(4,7)\}
2) \{(4,7),(2,1),(-3,6),(3,4)\}
3) \{(-1,6),(1,3),(2,5),(1,7)\}
4) \{(-1,2),(0,5),(5,0),(2,-1)\}

20 What is the value of the \(y\)-coordinate of the solution to the system of equations \(x - 2y = 1\) and \(x + 4y = 7\)?
1) \(1\)
2) \(-1\)
3) \(3\)
4) \(4\)

21 The solution to the equation \(x^2 - 6x = 0\) is
1) \(0,\) only
2) \(6,\) only
3) \(0\) and \(6\)
4) \(\pm\sqrt{6}\)

22 When \(5\sqrt{20}\) is written in simplest radical form, the result is \(k\sqrt{5}\). What is the value of \(k\)?
1) \(20\)
2) \(10\)
3) \(7\)
4) \(4\)

23 What is the value of the expression \(|-5x + 12|\) when \(x = 5\)?
1) \(-37\)
2) \(-13\)
3) \(13\)
4) \(37\)

24 A playground in a local community consists of a rectangle and two semicircles, as shown in the diagram below.

Which expression represents the amount of fencing, in yards, that would be needed to completely enclose the playground?
1) \(15\pi + 50\)
2) \(15\pi + 80\)
3) \(30\pi + 50\)
4) \(30\pi + 80\)
25 Which equation is represented by the graph below?

1) $y = x^2 - 3$
2) $y = (x - 3)^2$
3) $y = |x| - 3$
4) $y = |x - 3|$

26 Carrie bought new carpet for her living room. She calculated the area of the living room to be 174.2 square feet. The actual area was 149.6 square feet. What is the relative error of the area to the nearest ten-thousandth?

1) 0.1412
2) 0.1644
3) 1.8588
4) 2.1644

27 What is an equation of the line that passes through the point $(3, -1)$ and has a slope of 2?

1) $y = 2x + 5$
2) $y = 2x - 1$
3) $y = 2x - 4$
4) $y = 2x - 7$

28 The ages of three brothers are consecutive even integers. Three times the age of the youngest brother exceeds the oldest brother's age by 48 years. What is the age of the youngest brother?

1) 14
2) 18
3) 22
4) 26

29 Cassandra bought an antique dresser for $500. If the value of her dresser increases 6% annually, what will be the value of Cassandra's dresser at the end of 3 years to the nearest dollar?

1) $415$
2) $590$
3) $596$
4) $770$
30. The number of hours spent on math homework each week and the final exam grades for twelve students in Mr. Dylan's algebra class are plotted below.

Based on a line of best fit, which exam grade is the best prediction for a student who spends about 4 hours on math homework each week?

1) 62
2) 72
3) 82
4) 92

31. Chad complained to his friend that he had five equations to solve for homework. Are all of the homework problems equations? Justify your answer.

32. The diagram below represents Joe's two fish tanks.

Joe's larger tank is completely filled with water. He takes water from it to completely fill the small tank. Determine how many cubic inches of water will remain in the larger tank.

33. Clayton has three fair coins. Find the probability that he gets two tails and one head when he flips the three coins.
34 Find algebraically the equation of the axis of symmetry and the coordinates of the vertex of the parabola whose equation is \( y = -2x^2 - 8x + 3 \).

35 At the end of week one, a stock had increased in value from $5.75 a share to $7.50 a share. Find the percent of increase at the end of week one to the nearest tenth of a percent. At the end of week two, the same stock had decreased in value from $7.50 to $5.75. Is the percent of decrease at the end of week two the same as the percent of increase at the end of week one? Justify your answer.

36 The chart below compares two runners.

<table>
<thead>
<tr>
<th>Runner</th>
<th>Distance, in miles</th>
<th>Time, in hours</th>
</tr>
</thead>
<tbody>
<tr>
<td>Greg</td>
<td>11</td>
<td>2</td>
</tr>
<tr>
<td>Dave</td>
<td>16</td>
<td>3</td>
</tr>
</tbody>
</table>

Based on the information in this chart, state which runner has the faster rate. Justify your answer.

37 Express in simplest form: \( \frac{2x^2 - 8x - 42}{6x^2} \div \frac{x^2 - 9}{x^2 - 3x} \)

38 On the grid below, solve the system of equations graphically for \( x \) and \( y \).

\[
\begin{align*}
4x - 2y &= 10 \\
y &= -2x - 1
\end{align*}
\]

39 The test scores from Mrs. Gray’s math class are shown below.

72, 73, 66, 71, 82, 85, 95, 85, 86, 89, 91, 92

Construct a box-and-whisker plot to display these data.
1 The box-and-whisker plot below represents the math test scores of 20 students.

What percentage of the test scores are less than 72?
1) 25
2) 50
3) 75
4) 100

2 A bag contains eight green marbles, five white marbles, and two red marbles. What is the probability of drawing a red marble from the bag?
1) \( \frac{1}{15} \)
2) \( \frac{2}{15} \)
3) \( \frac{2}{13} \)
4) \( \frac{13}{15} \)

3 Julia went to the movies and bought one jumbo popcorn and two chocolate chip cookies for $5.00. Marvin went to the same movie and bought one jumbo popcorn and four chocolate chip cookies for $6.00. How much does one chocolate chip cookie cost?
1) $0.50
2) $0.75
3) $1.00
4) $2.00

4 Given:
\( Q = \{0, 2, 4, 6\} \)
\( W = \{0, 1, 2, 3\} \)
\( Z = \{1, 2, 3, 4\} \)
What is the intersection of sets \( Q \), \( W \), and \( Z \)?
1) \{2\}
2) \{0, 2\}
3) \{1, 2, 3\}
4) \{0, 1, 2, 3, 4, 6\}

5 Roger is having a picnic for 78 guests. He plans to serve each guest at least one hot dog. If each package, \( p \), contains eight hot dogs, which inequality could be used to determine how many packages of hot dogs Roger will need to buy?
1) \( p \geq \frac{7}{8} \)
2) \( 8p \geq 78 \)
3) \( 8 + p \geq 78 \)
4) \( 78 - p \geq 8 \)
6 In a science fiction novel, the main character found a mysterious rock that decreased in size each day. The table below shows the part of the rock that remained at noon on successive days.

<table>
<thead>
<tr>
<th>Day</th>
<th>Fractional Part of the Rock Remaining</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>(\frac{1}{2})</td>
</tr>
<tr>
<td>3</td>
<td>(\frac{1}{4})</td>
</tr>
<tr>
<td>4</td>
<td>(\frac{1}{8})</td>
</tr>
</tbody>
</table>

Which fractional part of the rock will remain at noon on day 7?

1) \(\frac{1}{128}\)
2) \(\frac{1}{64}\)
3) \(\frac{1}{14}\)
4) \(\frac{1}{12}\)

7 In the diagram below, what is the slope of the line passing through points \(A\) and \(B\)?

1) \(-\frac{2}{2}\)
2) \(2\)
3) \(-\frac{1}{2}\)
4) \(\frac{1}{2}\)

8 Which equation shows a correct trigonometric ratio for angle \(A\) in the right triangle below?

1) \(\sin A = \frac{15}{17}\)
2) \(\tan A = \frac{8}{17}\)
3) \(\cos A = \frac{15}{17}\)
4) \(\tan A = \frac{5}{8}\)
9 Debbie solved the linear equation $3(x + 4) - 2 = 16$ as follows:

She made an error between lines
1) 1 and 2
2) 2 and 3
3) 3 and 4
4) 4 and 5

10 The value of the expression $-|a - b|$ when $a = 7$ and $b = -3$ is
1) $-10$
2) 10
3) $-4$
4) 4

11 Which expression represents $\frac{12x^3 - 6x^2 + 2x}{2x}$ in simplest form?
1) $6x^2 - 3x$
2) $10x^2 - 4x$
3) $6x^2 - 3x + 1$
4) $10x^2 - 4x + 1$

12 Which ordered pair is a solution of the system of equations shown in the graph below?

1) $(-3, 1)$
2) $(-3, 5)$
3) $(0, -1)$
4) $(0, -4)$

13 Which equation represents the line that passes through the points $(-3, 7)$ and $(3, 3)$?
1) $y = \frac{2}{3}x + 1$
2) $y = \frac{2}{3}x + 9$
3) $y = -\frac{2}{3}x + 5$
4) $y = -\frac{2}{3}x + 9$
14 Which data table represents univariate data?

<table>
<thead>
<tr>
<th>Side Length of a Square</th>
<th>Area of Square</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>4</td>
</tr>
<tr>
<td>3</td>
<td>9</td>
</tr>
<tr>
<td>4</td>
<td>16</td>
</tr>
<tr>
<td>5</td>
<td>25</td>
</tr>
</tbody>
</table>

1)  

<table>
<thead>
<tr>
<th>Hours Worked</th>
<th>Pay</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>$160</td>
</tr>
<tr>
<td>25</td>
<td>$200</td>
</tr>
<tr>
<td>30</td>
<td>$240</td>
</tr>
<tr>
<td>35</td>
<td>$280</td>
</tr>
</tbody>
</table>

2)  

<table>
<thead>
<tr>
<th>Age Group</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>20–29</td>
<td>9</td>
</tr>
<tr>
<td>30–39</td>
<td>7</td>
</tr>
<tr>
<td>40–49</td>
<td>10</td>
</tr>
<tr>
<td>50–59</td>
<td>4</td>
</tr>
</tbody>
</table>

3)  

<table>
<thead>
<tr>
<th>People</th>
<th>Number of Fingers</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>20</td>
</tr>
<tr>
<td>3</td>
<td>30</td>
</tr>
<tr>
<td>4</td>
<td>40</td>
</tr>
<tr>
<td>5</td>
<td>50</td>
</tr>
</tbody>
</table>

4)  

15 What is the equation of the axis of symmetry of the parabola shown in the diagram below?

1)  $x = -0.5$
2)  $x = 2$
3)  $x = 4.5$
4)  $x = 13$

16 The members of the senior class are planning a dance. They use the equation $r = pn$ to determine the total receipts. What is $n$ expressed in terms of $r$ and $p$?

1)  $n = r + p$
2)  $n = r - p$
3)  $n = \frac{p}{r}$
4)  $n = \frac{r}{p}$
17 The graph of the equation $y = |x|$ is shown in the diagram below.

Which diagram could represent a graph of the equation $y = a|x|$ when $-1 < a < 0$?

18 Which relation represents a function?

1) $\{(0,3),(2,4),(0,6)\}$
2) $\{(-7,5),(-7,1),(-10,3),(-4,3)\}$
3) $\{(2,0),(6,2),(6,-2)\}$
4) $\{(-6,5),(-3,2),(1,2),(6,5)\}$
19 Which scatter plot shows the relationship between \( x \) and \( y \) if \( x \) represents a student score on a test and \( y \) represents the number of incorrect answers a student received on the same test?

1) \( x \) vs. \( y \)
2) \( y \) vs. \( x \)
3) \( x \) vs. \( y \) (reversed)
4) \( y \) vs. \( x \) (reversed)

20 Which expression is equivalent to \( 3^3 \cdot 3^4 \)?
1) \( 9^{12} \)
2) \( 9^7 \)
3) \( 3^{12} \)
4) \( 3^7 \)

21 Which point is on the line \( 4y - 2x = 0 \)?
1) \((-2, -1)\)
2) \((-2, 1)\)
3) \((-1, -2)\)
4) \((1, 2)\)

22 If Ann correctly factors an expression that is the difference of two perfect squares, her factors could be
1) \((2x + y)(x - 2y)\)
2) \((2x + 3y)(2x - 3y)\)
3) \((x - 4)(x - 4)\)
4) \((2y - 5)(y - 5)\)

23 Which ordered pair is in the solution set of the following system of linear inequalities?
\[
\begin{align*}
y &< 2x + 2 \\
y &\geq -x - 1
\end{align*}
\]
1) \((0, 3)\)
2) \((2, 0)\)
3) \((-1, 0)\)
4) \((-1, -4)\)

24 The expression \(6\sqrt{50} + 6\sqrt{2}\) written in simplest radical form is
1) \(6\sqrt{52}\)
2) \(12\sqrt{52}\)
3) \(17\sqrt{2}\)
4) \(36\sqrt{2}\)
25 What is the sum of $\frac{3x^2}{x-2}$ and $\frac{x^2}{x-2}$?

1) $\frac{3x^4}{(x-2)^2}$

2) $\frac{3x^4}{x-2}$

3) $\frac{4x^2}{(x-2)^2}$

4) $\frac{4x^2}{x-2}$

26 Which equation represents a line parallel to the graph of $2x - 4y = 16$?

1) $y = \frac{1}{2}x - 5$

2) $y = -\frac{1}{2}x + 4$

3) $y = -2x + 6$

4) $y = 2x + 8$

27 An example of an algebraic expression is

1) $\frac{2x + 3}{7} = \frac{13}{x}$

2) $(2x + 1)(x - 7)$

3) $4x - 1 = 4$

4) $x = 2$

28 What is the solution set of $\frac{x + 2}{x - 2} = \frac{-3}{x}$?

1) $\{-2, 3\}$

2) $\{-3, -2\}$

3) $\{-1, 6\}$

4) $\{-6, 1\}$

29 How many square inches of wrapping paper are needed to entirely cover a box that is 2 inches by 3 inches by 4 inches?

1) 18

2) 24

3) 26

4) 52

30 Which situation describes a correlation that is not a causal relationship?

1) the length of the edge of a cube and the volume of the cube

2) the distance traveled and the time spent driving

3) the age of a child and the number of siblings the child has

4) the number of classes taught in a school and the number of teachers employed

31 Angela wants to purchase carpeting for her living room. The dimensions of her living room are 12 feet by 12 feet. If carpeting is sold by the square yard, determine how many square yards of carpeting she must purchase.

32 In right triangle $ABC$, $AB = 20$, $AC = 12$, $BC = 16$, and $m\angle C = 90$. Find, to the nearest degree, the measure of $\angle A$. 

7
33 Jon is buying tickets for himself for two concerts. For the jazz concert, 4 tickets are available in the front row, and 32 tickets are available in the other rows. For the orchestra concert, 3 tickets are available in the front row, and 23 tickets are available in the other rows. Jon is randomly assigned one ticket for each concert. Determine the concert for which he is more likely to get a front-row ticket. Justify your answer.

34 Find the roots of the equation \(x^2 - x = 6\) algebraically.

35 Ms. Mosher recorded the math test scores of six students in the table below.

<table>
<thead>
<tr>
<th>Student</th>
<th>Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>Andrew</td>
<td>72</td>
</tr>
<tr>
<td>John</td>
<td>80</td>
</tr>
<tr>
<td>George</td>
<td>85</td>
</tr>
<tr>
<td>Amber</td>
<td>93</td>
</tr>
<tr>
<td>Betty</td>
<td>78</td>
</tr>
<tr>
<td>Roberto</td>
<td>80</td>
</tr>
</tbody>
</table>

Determine the mean of the student scores, to the nearest tenth. Determine the median of the student scores. Describe the effect on the mean and the median if Ms. Mosher adds 5 bonus points to each of the six students’ scores.

36 Using his ruler, Howell measured the sides of a rectangular prism to be 5 cm by 8 cm by 4 cm. The actual measurements are 5.3 cm by 8.2 cm by 4.1 cm. Find Howell’s relative error in calculating the volume of the prism, to the nearest thousandth.

37 A password consists of three digits, 0 through 9, followed by three letters from an alphabet having 26 letters. If repetition of digits is allowed, but repetition of letters is not allowed, determine the number of different passwords that can be made. If repetition is not allowed for digits or letters, determine how many fewer different passwords can be made.

38 Graph the solution set for the inequality \(4x - 3y > 9\) on the set of axes below. Determine if the point \((1, -3)\) is in the solution set. Justify your answer.

39 Find three consecutive positive even integers such that the product of the second and third integers is twenty more than ten times the first integer. [Only an algebraic solution can receive full credit.]
1) Given: Set $U = \{S, O, P, H, I, A\}$

Set $B = \{A, I, O\}$

If set $B$ is a subset of set $U$, what is the complement of set $B$?

1) $\{O, P, S\}$
2) $\{I, P, S\}$
3) $\{A, H, P\}$
4) $\{H, P, S\}$

2) How many different sandwiches consisting of one type of cheese, one condiment, and one bread choice can be prepared from five types of cheese, two condiments, and three bread choices?

1) 10
2) 13
3) 15
4) 30

3) The sum of $4x^3 + 6x^2 + 2x - 3$ and $3x^3 + 3x^2 - 5x - 5$ is

1) $7x^3 + 3x^2 - 3x - 8$
2) $7x^3 + 3x^2 + 7x + 2$
3) $7x^3 + 9x^2 - 3x - 8$
4) $7x^6 + 9x^4 - 3x^2 - 8$

4) What is the slope of the line that passes through the points $(3, 5)$ and $(-2, 2)$?

1) $\frac{1}{5}$
2) $\frac{3}{5}$
3) $\frac{5}{3}$
4) 5

5) What are the vertex and axis of symmetry of the parabola shown in the diagram below?

1) vertex: $(1, -4)$; axis of symmetry: $x = 1$
2) vertex: $(1, -4)$; axis of symmetry: $x = -4$
3) vertex: $(-4, 1)$; axis of symmetry: $x = 1$
4) vertex: $(-4, 1)$; axis of symmetry: $x = -4$
Three high school juniors, Reese, Matthew, and Chris, are running for student council president. A survey is taken a week before the election asking 40 students which candidate they will vote for in the election. The results are shown in the table below.

<table>
<thead>
<tr>
<th>Candidate's Name</th>
<th>Number of Students Supporting Candidate</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reese</td>
<td>15</td>
</tr>
<tr>
<td>Matthew</td>
<td>13</td>
</tr>
<tr>
<td>Chris</td>
<td>12</td>
</tr>
</tbody>
</table>

Based on the table, what is the probability that a student will vote for Reese?

1) \( \frac{1}{3} \)
2) \( \frac{3}{5} \)
3) \( \frac{3}{8} \)
4) \( \frac{5}{8} \)

Which linear equation represents a line containing the point \((1,3)\)?

1) \( x + 2y = 5 \)
2) \( x - 2y = 5 \)
3) \( 2x + y = 5 \)
4) \( 2x - y = 5 \)

The expression \( \sqrt{72} - 3\sqrt{2} \) written in simplest radical form is

1) \( 5\sqrt{2} \)
2) \( 3\sqrt{6} \)
3) \( 3\sqrt{2} \)
4) \( \sqrt{6} \)

In \( \triangle ABC \), the measure of \( \angle B = 90^\circ \), \( AC = 50 \), \( AB = 48 \), and \( BC = 14 \). Which ratio represents the tangent of \( \angle A \)?

1) \( \frac{14}{50} \)
2) \( \frac{14}{48} \)
3) \( \frac{48}{50} \)
4) \( \frac{48}{14} \)

Which ordered pair is in the solution set of the system of linear inequalities graphed below?

1) \( (1, -4) \)
2) \( (-5, 7) \)
3) \( (5, 3) \)
4) \( (-7, -2) \)
11 Which table does \textit{not} show bivariate data?

1) \begin{tabular}{|c|c|} \hline Height & Weight \\ \hline (inches) & (pounds) \\ \hline 39 & 50 \\ 48 & 70 \\ 60 & 90 \\ \hline \end{tabular}

2) \begin{tabular}{|c|c|} \hline Gallons & Miles Driven \\ \hline 15 & 300 \\ 20 & 400 \\ 25 & 500 \\ \hline \end{tabular}

3) \begin{tabular}{|c|c|} \hline Quiz Average & Frequency \\ \hline 70 & 12 \\ 80 & 15 \\ 90 & 6 \\ \hline \end{tabular}

4) \begin{tabular}{|c|c|} \hline Speed (mph) & Distance (miles) \\ \hline 40 & 80 \\ 50 & 120 \\ 55 & 150 \\ \hline \end{tabular}

12 What is the solution of the system of equations \( c + 3d = 8 \) and \( c = 4d - 6 \)?

1) \( c = -14, d = -2 \)

2) \( c = -2, d = 2 \)

3) \( c = 2, d = 2 \)

4) \( c = 14, d = -2 \)

13 Which graph represents a function?

1) \begin{tabular}{|c|c|} \hline \end{tabular}

2) \begin{tabular}{|c|c|} \hline \end{tabular}

3) \begin{tabular}{|c|c|} \hline \end{tabular}

4) \begin{tabular}{|c|c|} \hline \end{tabular}

14 The algebraic expression \( \frac{x - 2}{x^2 - 9} \) is undefined when \( x \) is

1) 0

2) 2

3) 3

4) 9
15 The graphs of the equations $y = 2x - 7$ and $y - kx = 7$ are parallel when $k$ equals
1) $-2$
2) $2$
3) $-7$
4) $7$

16 Which verbal expression is represented by $\frac{1}{2}(n - 3)$?
1) one-half $n$ decreased by 3
2) one-half $n$ subtracted from 3
3) the difference of one-half $n$ and 3
4) one-half the difference of $n$ and 3

17 The freshman class held a canned food drive for 12 weeks. The results are summarized in the table below.

<table>
<thead>
<tr>
<th>Week</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
<th>12</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cans</td>
<td>20</td>
<td>35</td>
<td>32</td>
<td>45</td>
<td>58</td>
<td>46</td>
<td>28</td>
<td>23</td>
<td>31</td>
<td>79</td>
<td>65</td>
<td>62</td>
</tr>
</tbody>
</table>

Which number represents the second quartile of the number of cans of food collected?
1) 29.5
2) 30.5
3) 40
4) 60

18 Which expression represents $\frac{-14a^2c^8}{7a^4c^2}$ in simplest form?
1) $-2ac^4$
2) $-2ac^6$
3) $\frac{-2c^4}{a}$
4) $\frac{-2c^6}{a}$

19 Which value of $x$ is the solution of $\frac{x}{3} + \frac{x + 1}{2} = x$?
1) 1
2) $-1$
3) 3
4) $-3$

20 When 36 is subtracted from the square of a number, the result is five times the number. What is the positive solution?
1) 9
2) 6
3) 3
4) 4

21 Which interval notation represents the set of all numbers greater than or equal to 5 and less than 12?
1) $[5, 12)$
2) $(5, 12]$ 
3) $(5, 12)$ 
4) $[5, 12]$
22 Four hundred licensed drivers participated in the math club's survey on driving habits. The table below shows the number of drivers surveyed in each age group.

<table>
<thead>
<tr>
<th>Age Group</th>
<th>Number of Drivers</th>
</tr>
</thead>
<tbody>
<tr>
<td>16-25</td>
<td>150</td>
</tr>
<tr>
<td>26-35</td>
<td>129</td>
</tr>
<tr>
<td>36-45</td>
<td>33</td>
</tr>
<tr>
<td>46-55</td>
<td>57</td>
</tr>
<tr>
<td>56-65</td>
<td>31</td>
</tr>
</tbody>
</table>

Which statement best describes a conclusion based on the data in the table?
1) It may be biased because no one younger than 16 was surveyed.
2) It would be fair because many different age groups were surveyed.
3) It would be fair because the survey was conducted by the math club students.
4) It may be biased because the majority of drivers surveyed were in the younger age intervals.

23 A formula used for calculating velocity is \( v = \frac{1}{2}at^2 \). What is \( a \) expressed in terms of \( v \) and \( t \)?
1) \( a = \frac{2v}{t} \)
2) \( a = \frac{2v}{t^2} \)
3) \( a = \frac{v}{t} \)
4) \( a = \frac{v}{2t^2} \)

24 What is the sum of \( \frac{-x + 7}{2x + 4} \) and \( \frac{2x + 5}{2x + 4} \)?
1) \( \frac{x + 12}{2x + 4} \)
2) \( \frac{3x + 12}{2x + 4} \)
3) \( \frac{x + 12}{4x + 8} \)
4) \( \frac{3x + 12}{4x + 8} \)

25 Steve ran a distance of 150 meters in \( \frac{1}{2} \) minutes. What is his speed in meters per hour?
1) 6
2) 60
3) 100
4) 6,000

26 How many different three-letter arrangements can be formed using the letters in the word \( ABC\) if each letter is used only once?
1) 56
2) 112
3) 168
4) 336

27 Factored completely, the expression \( 3x^2 - 3x - 18 \) is equivalent to
1) \( 3(x^2 - x - 6) \)
2) \( 3(x - 3)(x + 2) \)
3) \( (3x - 9)(x + 2) \)
4) \( (3x + 6)(x - 3) \)

28 Which quadrant will be completely shaded in the graph of the inequality \( y \leq 2x \)?
1) Quadrant I
2) Quadrant II
3) Quadrant III
4) Quadrant IV
29 A figure is made up of a rectangle and a semicircle as shown in the diagram below.

What is the area of the figure, to the nearest tenth of a square centimeter?
1) 39.4
2) 44.1
3) 48.8
4) 58.3

30 The value, $y$, of a $15,000 investment over $x$ years is represented by the equation $y = 15000(1.2)^{\frac{x}{3}}$. What is the profit (interest) on a 6-year investment?
1) $6,600
2) $10,799
3) $21,600
4) $25,799

31 Alexis calculates the surface area of a gift box as 600 square inches. The actual surface area of the gift box is 592 square inches. Find the relative error of Alexis’ calculation expressed as a decimal to the nearest thousandth.

32 Perform the indicated operation: $-6(a - 7)$
State the name of the property used.

33 A communications company is building a 30-foot antenna to carry cell phone transmissions. As shown in the diagram below, a 50-foot wire from the top of the antenna to the ground is used to stabilize the antenna.

Find, to the nearest degree, the measure of the angle that the wire makes with the ground.

34 Given: $A = \{18, 6, -3, -12\}$
Determine all elements of set $A$ that are in the solution of the inequality $\frac{2}{3}x + 3 < -2x - 7$. 

35 Graph and label the following equations on the set of axes below.

\[ y = |x| \]
\[ y = \frac{1}{2}x \]

Explain how decreasing the coefficient of \( x \) affects the graph of the equation \( y = |x| \).

36 Megan and Bryce opened a new store called the Donut Pit. Their goal is to reach a profit of $20,000 in their 18th month of business. The table and scatter plot below represent the profit, \( P \), in thousands of dollars, that they made during the first 12 months.

<table>
<thead>
<tr>
<th>( t ) (months)</th>
<th>( P ) (profit, in thousands of dollars)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3.0</td>
</tr>
<tr>
<td>2</td>
<td>2.5</td>
</tr>
<tr>
<td>3</td>
<td>4.0</td>
</tr>
<tr>
<td>4</td>
<td>5.0</td>
</tr>
<tr>
<td>5</td>
<td>6.5</td>
</tr>
<tr>
<td>6</td>
<td>5.5</td>
</tr>
<tr>
<td>7</td>
<td>7.0</td>
</tr>
<tr>
<td>8</td>
<td>6.0</td>
</tr>
<tr>
<td>9</td>
<td>7.5</td>
</tr>
<tr>
<td>10</td>
<td>7.0</td>
</tr>
<tr>
<td>11</td>
<td>9.0</td>
</tr>
<tr>
<td>12</td>
<td>9.5</td>
</tr>
</tbody>
</table>

Draw a reasonable line of best fit. Using the line of best fit, predict whether Megan and Bryce will reach their goal in the 18th month of their business. Justify your answer.

37 Express in simplest form:

\[
\frac{x^2 + 9x + 14}{x^2 - 49} + \frac{3x + 6}{x^2 + x - 56}
\]
38 The diagram below shows a cumulative frequency histogram of the students' test scores in Ms. Wedow's algebra class.

Determine the total number of students in the class. Determine how many students scored higher than 70. State which ten-point interval contains the median. State which two ten-point intervals contain the same frequency.

39 On the set of axes below, solve the following system of equations graphically for all values of x and y.

\[ y = -x^2 - 4x + 12 \]
\[ y = -2x + 4 \]
1 The school store did a study comparing the cost of a sweatshirt with the number of sweatshirts sold. The price was changed several times and the numbers of sweatshirts sold were recorded. The data are shown in the table below.

<table>
<thead>
<tr>
<th>Cost of Sweatshirt (in dollars)</th>
<th>$10</th>
<th>$25</th>
<th>$15</th>
<th>$20</th>
<th>$5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number Sold</td>
<td>9</td>
<td>6</td>
<td>15</td>
<td>11</td>
<td>14</td>
</tr>
</tbody>
</table>

Which scatter plot represents the data?

1)  

2)  

3)  

4) 

What is the solution of $3(2m − 1) \leq 4m + 7$?

1) $m \leq 5$
2) $m \geq 5$
3) $m \leq 4$
4) $m \geq 4$

Which set represents the intersection of sets A, B, and C shown in the diagram below?

1) \{3, 4, 5, 6, 7\}
2) \{2\}
3) \{2, 3, 4, 5, 6, 7\}
4) \{1, 2, 3, 4, 5, 6, 7, 8, 9\}
4 The end of a dog's leash is attached to the top of a 5-foot-tall fence post, as shown in the diagram below. The dog is 7 feet away from the base of the fence post.

How long is the leash, to the nearest tenth of a foot?
1) 4.9
2) 8.6
3) 9.0
4) 12.0

5 What is the slope of the line passing through the points A and B, as shown on the graph below?

6 The quotient of \((9.2 \times 10^6)\) and \((2.3 \times 10^2)\) expressed in scientific notation is
1) 4,000
2) 40,000
3) \(4 \times 10^3\)
4) \(4 \times 10^4\)

7 In a recent town election, 1,860 people voted for either candidate A or candidate B for the position of supervisor. If candidate A received 55% of the votes, how many votes did candidate B receive?
1) 186
2) 837
3) 1,023
4) 1,805

8 Which expression is equivalent to \(121 - x^2\)?
1) 
2) 
3) 
4) 

9 Given: \(U = \{1,2,3,4,5,6,7,8\}\)

\(B = \{2,3,5,6\}\)

Set B is a subset of set U. What is the complement of set B?
1) \{\}
2) \{2,3,5,6\}
3) \{1,4,7,8\}
4) \{1,2,3,4,5,6,7,8\}
10 Which graph can be used to find the solution of the following system of equations?

\[ y = x^2 + 2x + 3 \]
\[ 2y - 2x = 10 \]

1) 2) 3) 4)

11 The width of a rectangle is 3 less than twice the length, \( x \). If the area of the rectangle is 43 square feet, which equation can be used to find the length, in feet?

1) \( 2x(x - 3) = 43 \)
2) \( x(3 - 2x) = 43 \)
3) \( 2x + 2(2x - 3) = 43 \)
4) \( x(2x - 3) = 43 \)

12 Which value of \( x \) is the solution of \( \frac{2x - 3}{x - 4} = \frac{2}{3} \)?

1) \( \frac{1}{4} \)
2) \( \frac{1}{4} \)
3) \( -4 \)
4) 4

13 What is the perimeter of a regular pentagon with a side whose length is \( x + 4 \)?

1) \( x^2 + 16 \)
2) \( 4x + 16 \)
3) \( 5x + 4 \)
4) \( 5x + 20 \)

14 Which equation represents a line parallel to the \( y \)-axis?

1) \( x = y \)
2) \( x = 4 \)
3) \( y = 4 \)
4) \( y = x + 4 \)
15 The diagram below shows the graph of \( y = -x^2 - c \).

![Graph of \( y = -x^2 - c \)](image)

Which diagram shows the graph of \( y = x^2 - c \)?

1) ![Diagram 1](image)
2) ![Diagram 2](image)
3) ![Diagram 3](image)
4) ![Diagram 4](image)

16 Which point lies on the line whose equation is \( 2x - 3y = 9 \)?

1) \((-1, -3)\)
2) \((-1, 3)\)
3) \((0, 3)\)
4) \((0, -3)\)

17 Which phrase best describes the relationship between the number of miles driven and the amount of gasoline used?

1) causal, but not correlated
2) correlated, but not causal
3) both correlated and causal
4) neither correlated nor causal

18 The height, \( y \), of a ball tossed into the air can be represented by the equation \( y = -x^2 + 10x + 3 \), where \( x \) is the elapsed time. What is the equation of the axis of symmetry of this parabola?

1) \( y = 5 \)
2) \( y = -5 \)
3) \( x = 5 \)
4) \( x = -5 \)
19 In the diagram below, \(MATH\) is a rectangle, \(GB = 4.6, MH = 6,\) and \(HT = 15.\)

\[
\begin{array}{c}
\text{M} \\
\text{G} \\
\text{B} \\
\text{H} \\
\text{T}
\end{array}
\]

What is the area of polygon \(MBATH?\)
1) 34.5
2) 55.5
3) 90.0
4) 124.5

20 This year, John played in 10 baseball games. In these games he had hit the ball 2, 3, 0, 1, 3, 2, 4, 0, 2, and 3 times. In the first 10 games he plays next year, John wants to increase his average (mean) hits per game by 0.5. What is the total number of hits John needs over the first 10 games next year to achieve his goal?
1) 5
2) 2
3) 20
4) 25

21 What is the value of the \(y\)-coordinate of the solution to the system of equations \(2x + y = 8\) and \(x - 3y = -3?\)
1) \(-2\)
2) 2
3) 3
4) \(-3\)

22 Which set-builder notation describes \(\{-3, -2, -1, 0, 1, 2\}\)?
1) \(\{x | -3 \leq x < 2, \text{ where } x \text{ is an integer}\}\)
2) \(\{x | -3 < x \leq 2, \text{ where } x \text{ is an integer}\}\)
3) \(\{x | -3 < x < 2, \text{ where } x \text{ is an integer}\}\)
4) \(\{x | -3 \leq x \leq 2, \text{ where } x \text{ is an integer}\}\)

23 Corinne calculated the area of a paper plate to be 50.27 square inches. If the actual area of the plate is 55.42 square inches, what is the relative error in calculating the area, to the nearest thousandth?
1) 0.092
2) 0.093
3) 0.102
4) 0.103

24 The probability that it will snow on Sunday is \(\frac{3}{5}\). The probability that it will snow on both Sunday and Monday is \(\frac{3}{10}\). What is the probability that it will snow on Monday, if it snowed on Sunday?
1) \(\frac{9}{50}\)
2) 2
3) \(\frac{1}{2}\)
4) \(\frac{9}{10}\)
25 Which graph represents an exponential equation?

1) 

2) 

3) 

4) 

26 Right triangle $ABC$ has legs of 8 and 15 and a hypotenuse of 17, as shown in the diagram below.

The value of the tangent of $\angle B$ is

1) 0.4706
2) 0.5333
3) 0.8824
4) 1.8750

27 What is $\frac{2+x}{5x} - \frac{x-2}{5x}$ expressed in simplest form?

1) 0
2) $\frac{2}{5}$
3) $\frac{4}{5x}$
4) $\frac{2x+4}{5x}$

28 How many different four-letter arrangements are possible with the letters $G, A, R, D, E, N$ if each letter may be used only once?

1) 15
2) 24
3) 360
4) 720
29 What is an equation of the line that passes through the points (1,3) and (8,5)?

1) \( y + 1 = \frac{2}{7} (x + 3) \)

2) \( y - 5 = \frac{2}{7} (x - 8) \)

3) \( y - 1 = \frac{2}{7} (x + 3) \)

4) \( y + 5 = \frac{2}{7} (x - 8) \)

30 An example of an algebraic expression is

1) \( x + 2 \)

2) \( y = x + 2 \)

3) \( y < x + 2 \)

4) \( y = x^2 + 2x \)

31 Express in simplest form: \( \frac{45a^4b^3 - 90a^3b}{15a^2b} \)

32 Joseph typed a 1,200-word essay in 25 minutes. At this rate, determine how many words he can type in 45 minutes.

33 Express \(-3\sqrt{48}\) in simplest radical form.

34 The number of songs fifteen students have on their MP3 players is:

120, 124, 132, 145, 200, 255, 260, 292, 308, 314, 342, 407, 421, 435, 452

State the values of the minimum, 1st quartile, median, 3rd quartile, and maximum. Using these values, construct a box-and-whisker plot using an appropriate scale on the line below.

35 Find the volume, in cubic centimeters, and the surface area, in square centimeters, of the rectangular prism shown below.

36 Find the roots of the equation \( x^2 = 30 - 13x \) algebraically.
37 On the set of axes below, solve the following system of inequalities graphically.

\[ y < 2x + 1 \]
\[ y \geq -\frac{1}{3}x + 4 \]

State the coordinates of a point in the solution set.

38 Each of the hats shown below has colored marbles placed inside. Hat A contains five green marbles and four red marbles. Hat B contains six blue marbles and five red marbles. Hat C contains five green marbles and five blue marbles.

![Hats A, B, C]

If a student were to randomly pick one marble from each of these three hats, determine from which hat the student would most likely pick a green marble. Justify your answer. Determine the fewest number of marbles, if any, and the color of these marbles that could be added to each hat so that the probability of picking a green marble will be one-half in each of the three hats.

39 A hot-air balloon is tied to the ground with two taut (straight) ropes, as shown in the diagram below. One rope is directly under the balloon and makes a right angle with the ground. The other rope forms an angle of 50° with the ground.

![Diagram of hot-air balloon and ropes]

Determine the height, to the nearest foot, of the balloon directly above the ground. Determine the distance, to the nearest foot, on the ground between the two ropes.